

On Deeply Virtual Compton Scattering at Next to Leading Order

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Light Cone 2013



In collaboration with : P. Kroll, B. Pire,
F. Sabatié, L. Szymanowski and J. Wagner.

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Definition.

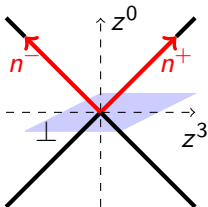
Matrix elements of twist-2 bilocal operators.

$$F^q = \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q} \left(-\frac{z}{2} \right) \gamma^+ q \left(\frac{z}{2} \right) | p \rangle_{z^+=0, z_\perp=0}$$

$$= \frac{1}{2P^+} \left[\textcolor{red}{H}^q \bar{u}(p') \gamma^+ u(p) + \textcolor{red}{E}^q \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right]$$

$$\tilde{F}^q = \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q} \left(-\frac{z}{2} \right) \gamma^+ \gamma_5 q \left(\frac{z}{2} \right) | p \rangle_{z^+=0, z_\perp=0}$$

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References

Müller *et al.*, Fortschr. Phys. **42** (1994) 101
 Ji, Phys. Rev. Lett. **78** (1997) 610
 Radyushkin, Phys. Lett. B **380** (1996) 417

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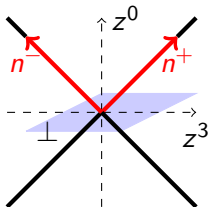
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See D. Müller's lecture next thursday!

- Partons with a **light-like** separation.
- **Quarks** and **gluon** GPDs.
- $\text{GPD}^{q,g} = \text{GPD}^{q,g}(x, \xi, t)$.

Motivations.

3D imaging of nucleon's partonic content but also...

- Correlation of the **longitudinal momentum** and the **transverse position** of a parton in the nucleon.
- Insights on:
 - **Spin** structure,
 - **Energy-momentum** structure.
- **Probabilistic interpretation** of Fourier transform of $\text{GPD}(x, \xi = 0, t)$ in **transverse plane**.

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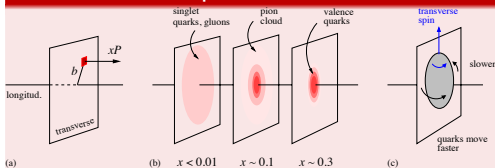
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Obtain this 3d picture from exclusive measurements ?

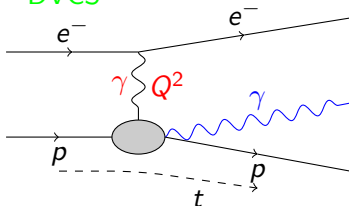


Weiss, AIP
Conf. Proc.
1149, 150
(2009)

Timelike and spacelike Compton Scattering.

Scattering amplitudes and their partonic interpretation.

DVCS



Compton Form Factors

- Parametrize amplitudes.

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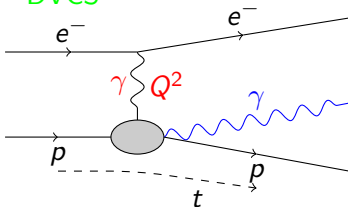
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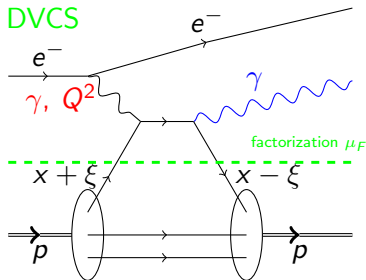
DVCS



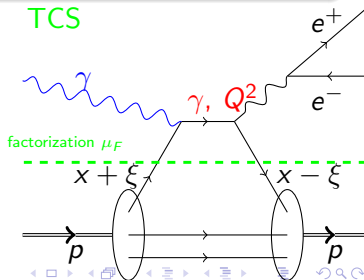
Compton Form Factors

- Parametrize amplitudes.
- Evaluation at LO.

DVCS



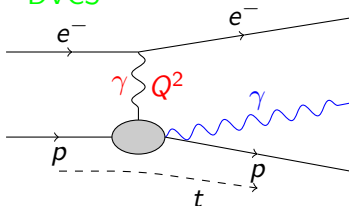
TCS



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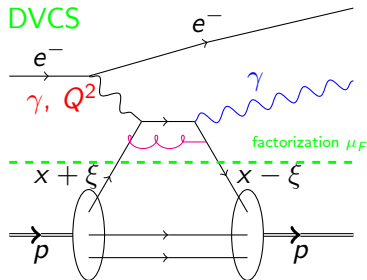
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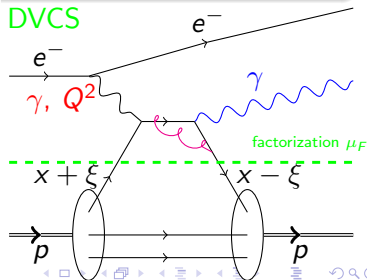
Compton Form Factors

- Parametrize amplitudes.
- Evaluation at LO.
- Evaluation at **NLO**.

DVCS



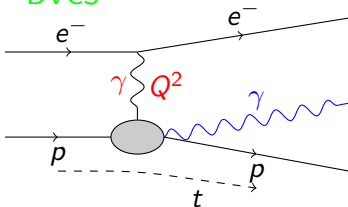
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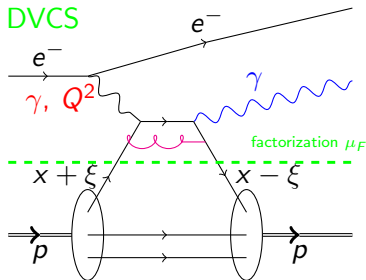
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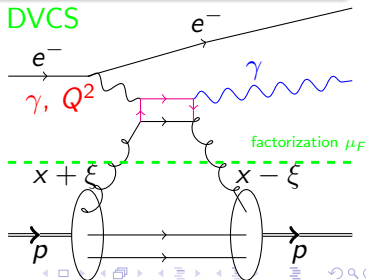
Compton Form Factors

- Parametrize amplitudes.
- Evaluation at LO.
- Evaluation at **NLO**.
- Other diagrams at NLO, including **gluon GPDs**.

DVCS



DVCS



Explicit expressions of Compton Form Factors.

Quark and gluon contributions to the CFF $\mathcal{H}$ at LO and NLO (at fixed t).

- Convolution of singlet GPD $H_q^+(x) \equiv H_q(x) - H_q(-x)$:

$$\begin{aligned} \mathcal{H}_q(\xi, Q^2) &= \int_{-1}^{+1} dx H_q^+(x, \xi, \mu_F) T_q \left(x, \xi, \alpha_S(\mu_F), \frac{Q}{\mu_F} \right) \\ &+ \int_{-1}^{+1} dx H_g(x, \xi, \mu_F) T_g \left(x, \xi, \alpha_S(\mu_F), \frac{Q}{\mu_F} \right) \end{aligned}$$

Belitsky and Müller, Phys. Lett. **B417**, 129 (1998)

Pire *et al*, Phys. Rev. **D83**, 034009 (2011)

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Belitsky and Müller, Phys. Lett. **B417**, 129 (1998)

Pire *et al*, Phys. Rev. **D83**, 034009 (2011)

- Integration yields **imaginary** parts to $\mathcal{H}$:

$$\text{Im}\mathcal{H}_q(\xi, Q^2) \stackrel{\text{LO}}{=} \pi H_q^+(\xi, \xi, \mu_F)$$

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$$\text{Im} \mathcal{H}_q(\xi, Q^2) \stackrel{\text{NLO}}{=} \mathcal{I}(\xi) H_q^+(\xi, \xi, \mu_F) \\ + \int_{-1}^{+1} dx \mathcal{T}^q(x) \left(H_q^+(x, \xi, \mu_F) - H_q^+(\xi, \xi, \mu_F) \right) \\ + \text{gluon contributions.}$$

Explicit expressions of Compton Form Factors.

Compton Scattering at NLO.

Imaginary part of Compton Form Factor $\mathcal{H}_q$ at NLO:

$$\begin{aligned} \text{Im}\mathcal{H}_q(\xi, Q^2) &\stackrel{\text{NLO}}{=} \mathcal{I}(\xi)H_q^+(\xi, \xi, \mu_F) \\ &+ \int_{-1}^{+1} dx \mathcal{T}^q(x) \left(H_q^+(x, \xi, \mu_F) - H_q^+(\xi, \xi, \mu_F) \right) \\ &+ \text{gluon contributions.} \end{aligned}$$

Due to $\mathcal{O}(\alpha_S(\mu_F))$ corrections:

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- **No more direct link** to H_q even in valence region where $H_q(-\xi, \xi)$ is expected to be small.

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Question: What is the size of these $\mathcal{O}(\alpha_S(\mu_F))$ corrections?

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Double Distribution models of the GPD H .

Kroll - Goloskokov model.

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Conclusions

- **Factorized Ansatz.** For $i = g, \text{ sea or val}$:

$$H_i(x, \xi, t) = \int_{|\alpha|+|\beta|\leq 1} d\beta d\alpha \delta(\beta + \xi\alpha - x) f_i(\beta, \alpha, t)$$

$$f_i(\beta, \alpha, t) = e^{b_i t} \frac{1}{|\beta|^{\alpha' t}} h_i(\beta) \pi_{n_i}(\beta, \alpha)$$

$$\pi_{n_i}(\beta, \alpha) = \frac{\Gamma(2n_i + 2)}{2^{2n_i+1} \Gamma^2(n_i + 1)} \frac{(1 - |\beta|)^2 - \alpha^2]^{n_i}}{(1 - |\beta|)^{2n_i+1}}$$

- Expressions for h_i and n_i :

$$h_g(\beta) = |\beta| g(|\beta|) \quad n_g = 2$$

$$h_{\text{sea}}^q(\beta) = q_{\text{sea}}(|\beta|) \text{sign}(\beta) \quad n_{\text{sea}} = 2$$

$$h_{\text{val}}^q(\beta) = q_{\text{val}}(\beta) \Theta(\beta) \quad n_{\text{val}} = 1$$

Goloskokov and Kroll, Eur. Phys. J. **C42**, 281 (2005)

- Comparison to **existing DVCS measurements** at LO.

Kroll *et al.*, Eur. Phys. J. **C73**, 2278 (2013)

Double Distribution models of the GPD H .

MSTW08 based model with classical Radyushkin's factorized Ansatz.

- Use MSTW08 Parton Distribution Functions.

Martin *et al.*, Eur. Phys. J. C. **63** (2009) 189.

- Assume factorized t -dependence:

$$H(x, \xi, t) = \int_{|\alpha|+|\beta|\leq 1} d\beta d\alpha \delta(\beta + \xi\alpha - x) \pi(\beta, \alpha) f(\beta, t)$$

- u and d quarks:

$$f_u(\beta, \alpha, t) = \frac{1}{2} F_1^u(t) u(\beta) \pi(\beta, \alpha)$$

$$f_d(\beta, \alpha, t) = F_1^d(t) d(\beta) \pi(\beta, \alpha)$$

with F_1^u and F_1^d the u and d quark contributions to the proton form factor F_1 .

- s quark and gluons: dipole Ansatz.
- Add D-term from Chiral Quark Soliton Model.

Goeke *et al.*, Prog.Part.Nucl.Phys. **47** (2001) 401

Definition of DVCS observables (1/3).

Single and double asymmetries.

- Combined beam-spin and charge asymmetries :

$$d\sigma^{h_e, Q_e}(\phi) = d\sigma_{UU}(\phi) [1 + h_e A_{LU, DVCS}(\phi) + Q_e h_e A_{LU, I}(\phi) + Q_e A_C(\phi)]$$

- Single beam-spin asymmetry :

$$A_{LU}^{Q_e}(\phi) = \frac{d\sigma^{\rightarrow Q_e} - d\sigma^{\leftarrow Q_e}}{d\sigma^{\rightarrow Q_e} + d\sigma^{\leftarrow Q_e}}$$

- Relation between observables :

$$A_{LU}^{Q_e}(\phi) = \frac{Q_e A_{LU, I}(\phi) + A_{LU, DVCS}(\phi)}{1 + Q_e A_C(\phi)}$$

- Compute Fourier coefficients of asymmetries.

Definition of DVCS observables (2/3).

Combined cross sections.

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- COMPASS **combined beam-spin and charge** cross sections:

$$S_{CS,U} = d\sigma^{\rightarrow} + d\sigma^{\leftarrow} = 2d\sigma_{UU}(1 - A_{LU,I})$$

$$D_{CS,U} = d\sigma^{\rightarrow} - d\sigma^{\leftarrow} = 2d\sigma_{UU}(A_C - A_{LU,DVCS})$$

$$A_{CS,U} = \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} = \frac{A_C - A_{LU,DVCS}}{1 - A_{LU,I}}$$

- JLab Hall A **beam-polarized** cross sections:

$$\Delta\sigma = d\sigma^{\rightarrow} - d\sigma^{\leftarrow}$$

$$\Sigma\sigma = d\sigma^{\rightarrow} + d\sigma^{\leftarrow}$$

- Compute Fourier coefficients of cross sections.

Definition of DVCS observables (3/3).

What are the probed combinations of CFFs ?

Typical kinematics

Experiment	Kinematics		
	x_B	Q^2 [GeV ²]	t [GeV ²]
HERA	0.001	8.00	-0.30
COMPASS	0.05	2.00	-0.20
HERMES	0.09	2.50	-0.12
CLAS	0.19	1.25	-0.19
HALL A	0.36	2.30	-0.23

Definition of DVCS observables (3/3).

What are the probed combinations of CFFs ?

Typical kinematics

Experiment	Kinematics			
	x_B	Q^2 [GeV ²]	t [GeV ²]	$-t/Q^2$
HERA	0.001	8.00	-0.30	0.04
COMPASS	0.05	2.00	-0.20	0.10
HERMES	0.09	2.50	-0.12	0.05
CLAS	0.19	1.25	-0.19	0.15
HALL A	0.36	2.30	-0.23	0.10

Definition of DVCS observables (3/3).

What are the probed combinations of CFFs ?

Selection of observables

Experiment	Observable	Normalized CFF dependence
HERMES	$A_C^{\cos 0\phi}$	$\text{Re}\mathcal{H} + 0.06\text{Re}\mathcal{E} + 0.24\text{Re}\tilde{\mathcal{H}}$
	$A_C^{\cos \phi}$	$\text{Re}\mathcal{H} + 0.05\text{Re}\mathcal{E} + 0.15\text{Re}\tilde{\mathcal{H}}$
	$A_{\text{LU},\text{I}}^{\sin \phi}$	$\text{Im}\mathcal{H} + 0.05\text{Im}\mathcal{E} + 0.12\text{Im}\tilde{\mathcal{H}}$
	$A_{\text{UL}}^{+,\sin \phi}$	$\text{Im}\tilde{\mathcal{H}} + 0.10\text{Im}\mathcal{H} + 0.01\text{Im}\mathcal{E}$
CLAS	$A_{\text{LU}}^{-,\sin \phi}$	$\text{Im}\mathcal{H} + 0.06\text{Im}\mathcal{E} + 0.21\text{Im}\tilde{\mathcal{H}}$
	$A_{\text{UL}}^{-,\sin \phi}$	$\text{Im}\tilde{\mathcal{H}} + 0.12\text{Im}\mathcal{H} + 0.04\text{Im}\mathcal{E}$
HALL A	$\sigma^{\cos 0\phi}$	$1 + 0.05\text{Re}\mathcal{H} + 0.007\mathcal{H}\mathcal{H}^*$
	$\sigma^{\cos \phi}$	$1 + 0.12\text{Re}\mathcal{H} + 0.05\text{Re}\tilde{\mathcal{H}}$

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Kinematic region of existing DVCS measurements.

Looking for the Bjorken regime.

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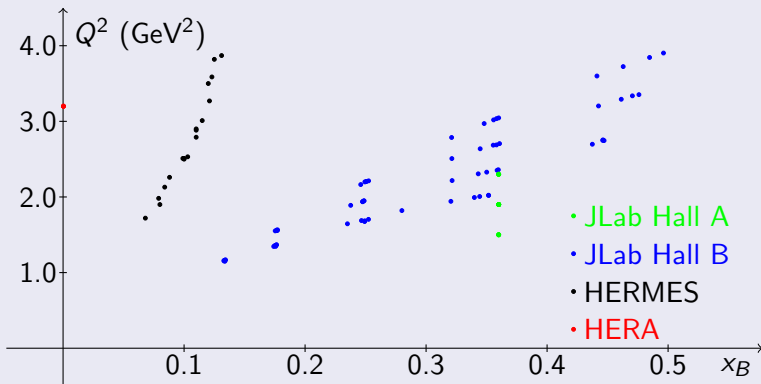
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What is large Q^2 ?

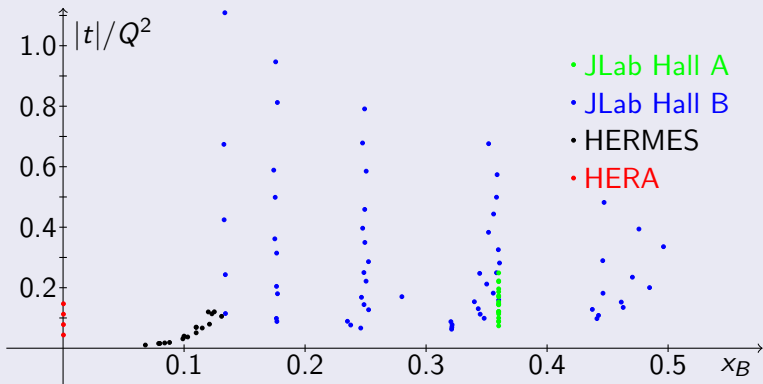


- World data cover **complementary kinematic regions**.

Kinematic region of existing DVCS measurements.

Looking for the Bjorken regime.

What is large Q^2 ?

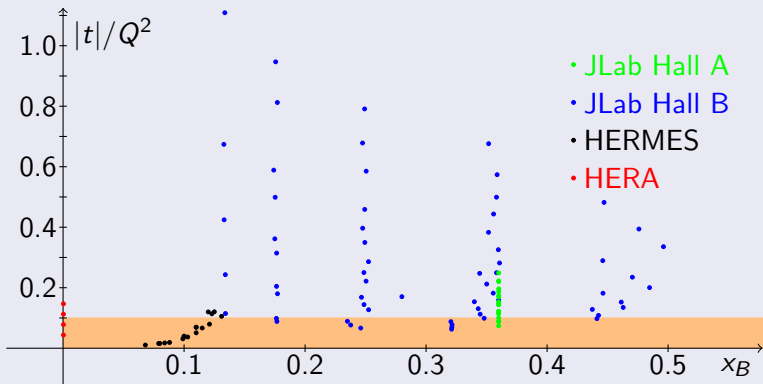


- World data cover **complementary kinematic regions**.
- Q^2 is **not so large** for most of the data.

Kinematic region of existing DVCS measurements.

Looking for the Bjorken regime.

What is large Q^2 ?

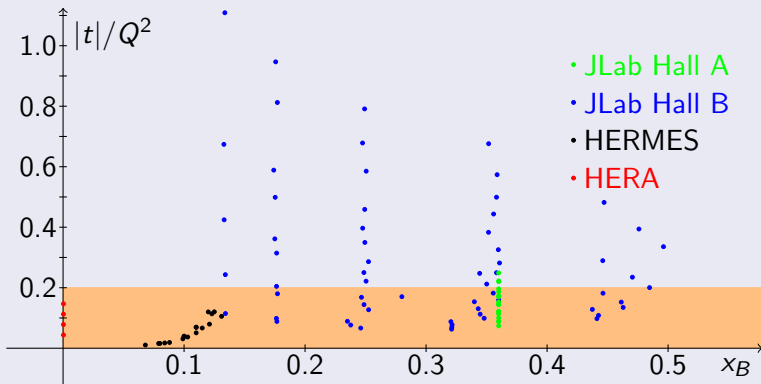


- World data cover **complementary kinematic regions**.
- Q^2 is **not so large** for most of the data.
- Higher twists, finite- t and target mass corrections ?

Kinematic region of existing DVCS measurements.

Looking for the Bjorken regime.

What is large Q^2 ?



- World data cover **complementary kinematic regions**.
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- Higher twists, finite- t and target mass corrections ?

Approximations.

First systematic study of DVCS polarized and unpolarized observables.

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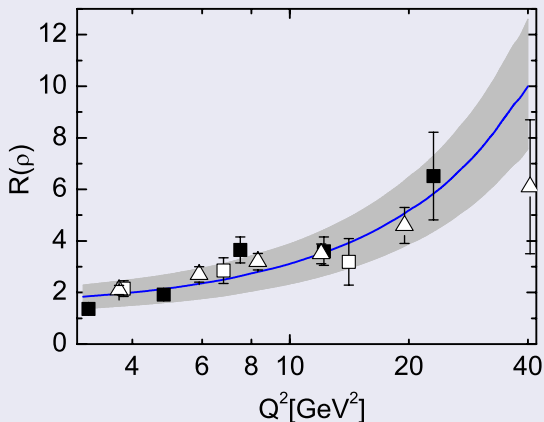
Unless explicitly stated

- Work at twist 2 accuracy.
- Use LO expression of kernel $C(x, \xi)$.
- No finite- t or target mass corrections (higher twist).

Goloskokov-Kroll (GK) model on DVMP.

The GK model **was tuned** to analyse DVMP.

σ_L/σ_T for ρ^0 at $W = 90$ GeV



Goloskokov and Kroll, Eur. Phys. J. C **53** (2005) 281

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Goloskokov-Kroll (GK) model on DVCS.

No parameter of the GK model **was tuned** to analyse DVCS.

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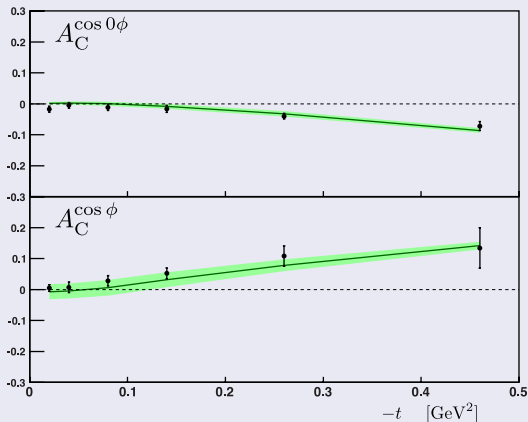
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Beam Charge Asymmetry, HERMES



Kroll *et al.*, Eur. Phys. J C **73** (2013) 2278

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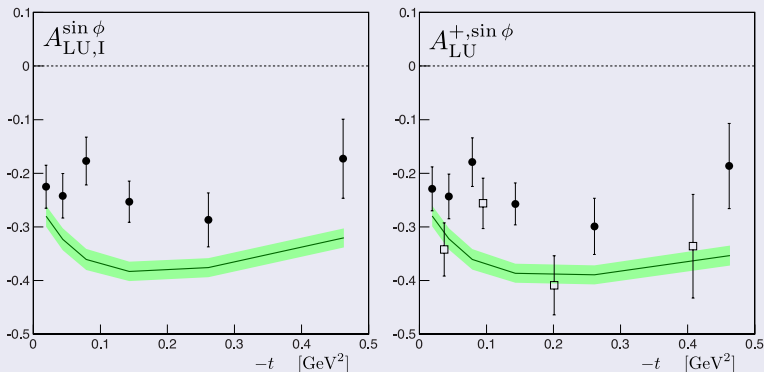
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Beam Spin Asymmetry, HERMES



Kroll *et al.*, Eur. Phys. J C73 (2013) 2278

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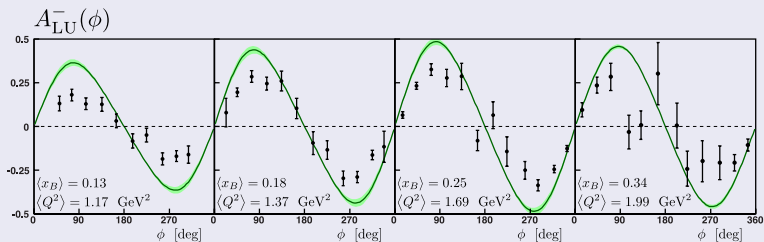
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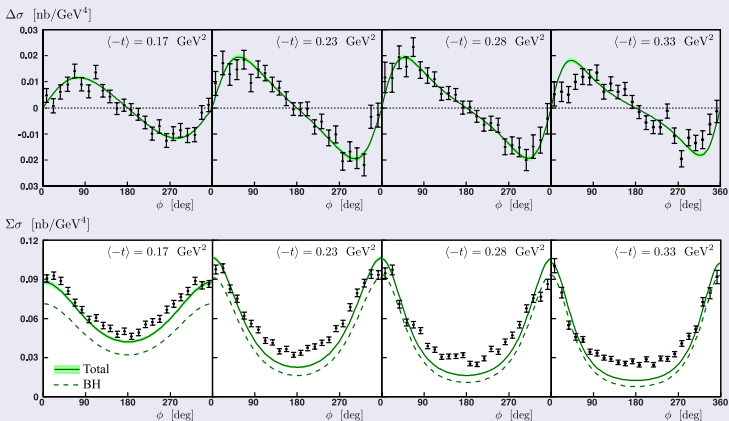
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Helicity-dependent and independent cross sections, JLab Hall A



Kroll *et al.*, Eur. Phys. J C **73** (2013) 2278

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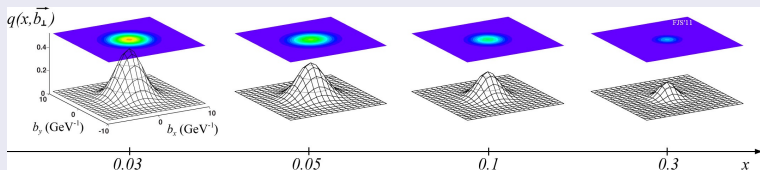
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Conclusions

Spin structure with GK model (quoted at 4 GeV²)

- $J^u \simeq 0.250$, $J^d \simeq 0.020$, $J^s \simeq 0.015$, $J^g \simeq 0.214$
- $\sum_{q,g} J^{q,g} \simeq 1/2$

3d nucleon structure with GK model



Spacelike Compton Form Factors.

Large NLO corrections, mostly due to gluons, maximum in the kinematic region of HERMES and COMPASS.

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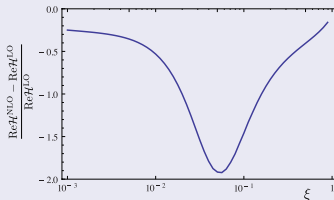
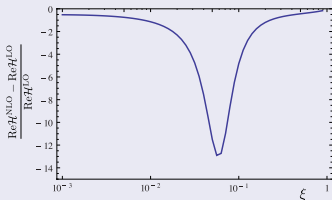
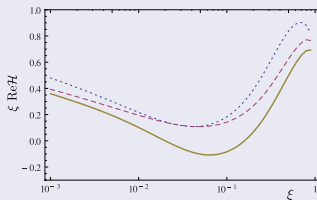
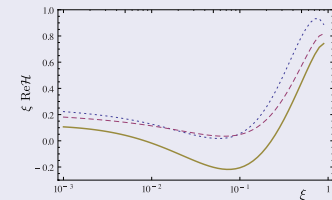
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$\text{Re}\mathcal{H}$ at LO and NLO



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

Left: KG model

Right: MSTW08-based model

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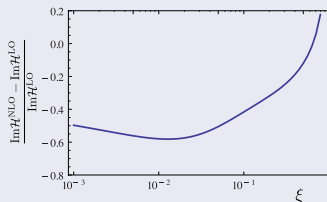
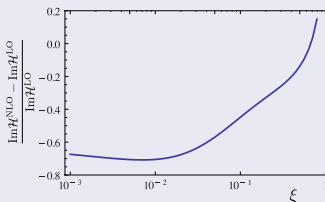
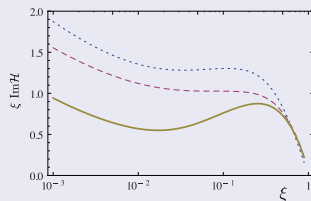
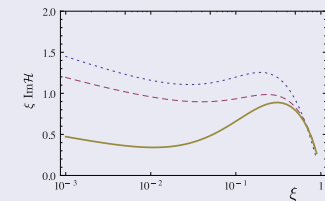
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$\text{Im}\mathcal{H}$ at LO and NLO



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

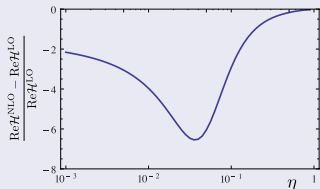
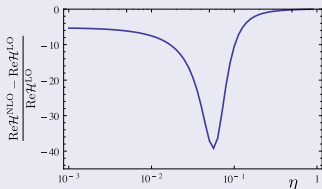
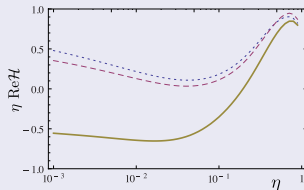
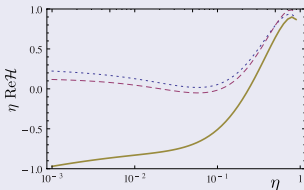
Left: KG model

Right: MSTW08-based model

Timelike Compton Form Factors.

Large NLO corrections, mostly due to gluons, maximum in the kinematic region of HERMES and COMPASS.

$Re\mathcal{H}$ at LO and NLO



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

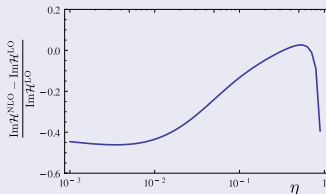
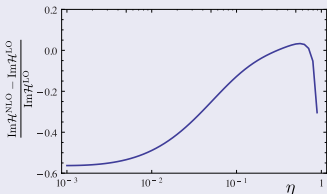
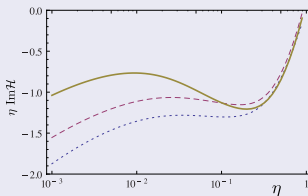
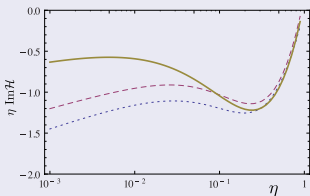
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$Im\mathcal{H}$ at LO and NLO



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

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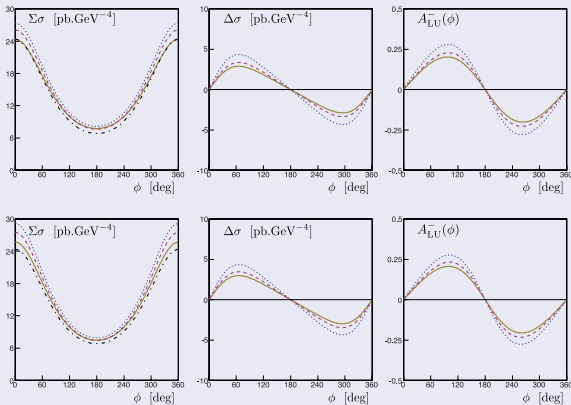
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Projections: CLAS12 kinematics, DVCS channel.

Sizeable NLO corrections and gluon contributions.

$$E_e = 11 \text{ GeV}, x_B = 0.36, Q^2 = 4 \text{ GeV}^2, t = -0.2 \text{ GeV}^2$$



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

Upper line: KG model

Lower line: □ MSTW08-based model

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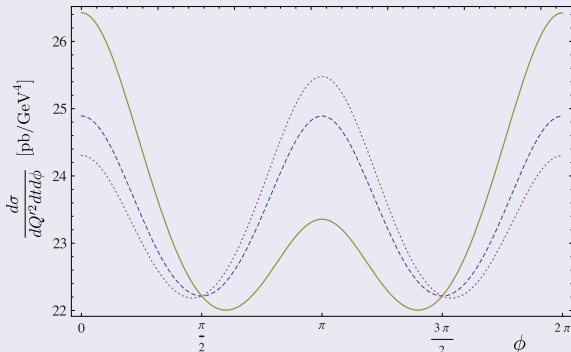
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$$E_\gamma = 10 \text{ GeV } (\eta \simeq 0.11), Q^2 = 4 \text{ GeV}^2, t = -0.1 \text{ GeV}^2$$



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dashed: pure BH

dotted: BH

solid: BH

+ LO Interference

+ NLO Interference

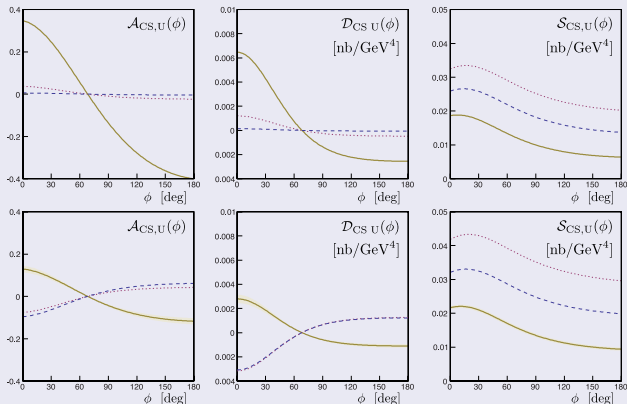
KG model

Cross section integrated over $\theta \in (\frac{\pi}{4}, \frac{3\pi}{4})$

Projections: COMPASS kinematics, DVCS channel.

Sizeable NLO corrections and gluon contributions.

$$E_\mu = 160 \text{ GeV}, x_B = 0.1, Q^2 = 4 \text{ GeV}^2, t = -0.2 \text{ GeV}^2$$



Moutarde *et al.*, Phys. Rev. **D87**, 054029 (2013)

dotted: LO dashed: NLO quark corrections solid: full NLO

Upper line: KG model

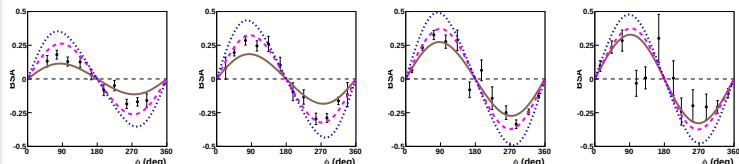
Lower line: MSTW08-based model

CLAS beam spin asymmetries, DVCS channel.

Distinction between LO and NLO already relevant for 6 GeV data.

From left to right: $x_B = 0.13, 0.18, 0.25$ and 0.34
 $Q^2 = 1.17, 1.37, 1.69$ and 1.99 GeV^2
 $t \simeq -0.3 \text{ GeV}^2$

Preliminary result



dotted: LO dashed: NLO quark corrections solid: full NLO

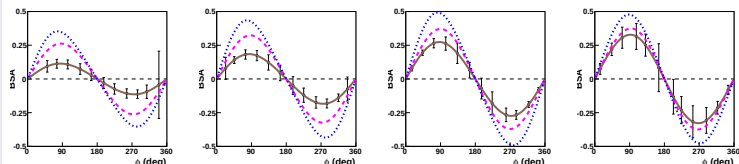
- Comparison with KG model.

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 $t \simeq -0.3 \text{ GeV}^2$

Preliminary result



dotted: LO dashed: NLO quark corrections solid: full NLO

- Comparison with KG model.
- Compare differences between LO and NLO computations to **experimental statistical uncertainty** considering full NLO computation as nominal result.

Conclusions.

Constraining gluon GPDs even from data in the valence region?

- **Large NLO "corrections"** to DVCS amplitude.
- Need resummed expressions!
Altinoluk et al., JHEP 1210, 049 (2012)
Altinoluk et al., arXiv:1206.3115 [hep-ph]
- Sensitivity to **gluon GPDs** even in the **valence region**.
- Direct impact on **extraction** of CFFs from experimental data and their **interpretation**.
- Need global GPD fits to **separate quarks and gluon** contributions and allow an **accurate** interpretation of extracted data.
- **COMPASS and JLab12 DVCS experiments may provide a way to constrain gluon GPDs!**