

Lightfront QED and intense laser fields

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LightCone 2013-May-21



CHALMERS



- Chris Harvey, Tom Heinzl, Florian Hebenstreit, Pieter Maris, Mattias Marklund and Greger Torgrimsson, James Vary, Xingbo Zhao

Outline

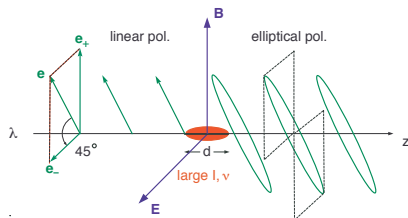


1. Lasers and prospects.
2. Time-dependent processes.
 - ▷ Front form vs. instant form.
 - ▷ The mass shift.
 - ▷ Pair production: the Wigner formalism.
3. Nonperturbative methods.

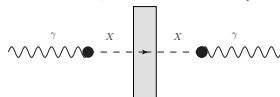
Experimental prospects

- Low energy, high intensity.
- Femtosecond duration, 10^{20} photons/ pulse.
- 10^1 - 10^2 J \rightarrow intensity 10^{22} - 10^{23} W/cm²

- ▷ Light-by-light scattering.
- ▷ Vacuum birefringence.
- ▷ New particle searches:
Light shining through walls
- ▷ Radiation reaction.
- ▷ Schwinger pair production.



T. Heinzl et al, *Opt. Commun.* **267** (2006) 318



Jaeckel & Ringwald, *Ann.Rev.Nucl.Part.Sci.* (2010)

Approaches to 'strong field QED'

- Laser \rightarrow background field.
- Dimensionless field strength
- **Cannot** be treated perturbatively.

$$a_0 \sim \frac{eE}{m\omega} \gg 1.$$

- Treat background **exactly**: use **Furry picture**.

Furry, 1951

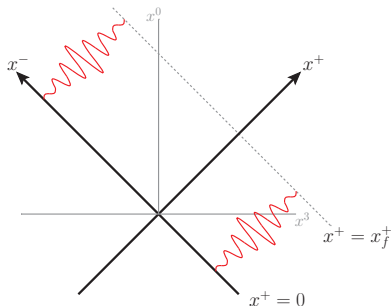


- Fermion propagator: $[i\not{\partial} - m - eA_{\text{ext}}]S = \delta^4(x - y)$

\rightarrow This talk: **Furry picture** and **simple backgrounds**.

Spacetime structure

- Simple field model. $F_{\text{ext}}^{\mu\nu} \equiv F_{\text{ext}}^{\mu\nu}(x^+)$.

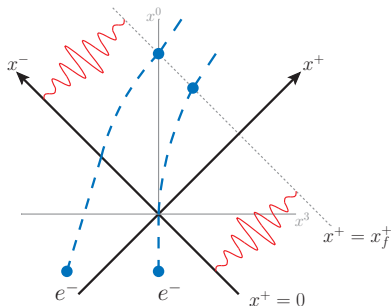


1. Plane wave (\perp to lightfront)
2. Longitudinal electric (pairs)
 - Compare x^0 and x^+ .

- All particles enter at same front times.
- Lorentz orbit: $x^+ = \frac{p^+}{m} \tau$

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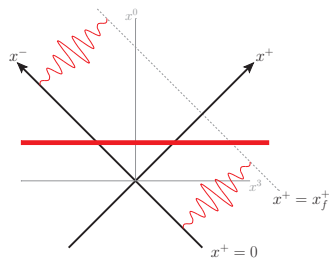
Physics in plane waves: quantum

- Scalar field in a **plane wave**.

$$\phi = \int dp \, b_p \varphi_p + d_p^\dagger \varphi_{-p}$$

$$\varphi_p = \exp \left[-ip \cdot x - i \int_{x^-}^{x^+} \frac{2p \cdot a - a^2}{p^+} \right]$$

Volkov *Z. Phys.* 94 (1953)



- Canonical quantisation, instant form:

$$[\phi, \partial_0 \phi] = i\delta \implies \dots?$$

- ✗ Orthogonality of φ_p on spacelike hyperplanes?
- Progress only in recent years.

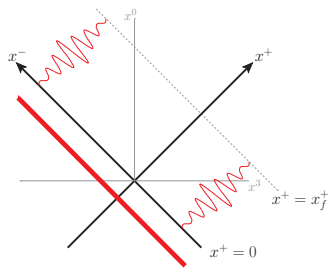
Physics in plane waves: quantum

- Scalar field in a **plane wave**.

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Volkov *Z. Phys.* 94 (1953)



- ✓ Front form: **as in free theory**.

$$[b_p, b_q^\dagger] = 2p^+ (2\pi)^3 \delta^{\perp,+}(q - p)$$

- ✓ Usual particle interpretation.
- ✓ **Time dependent processes in lightfront QED.**

Neville & Rohrlich *PRD* 8 (1971) 1692, Ilderton & Torgrimsson *PRD* 87 (2013) 085040

Poles in the propagator

- Monochromatic plane wave, frequency ω .
- Volkov propagator G : infinite series of poles ($n \in \mathbb{Z}$)

$$(p_\mu - nk_\mu)^2 = m_*^2$$
$$m_*^2 = m^2(1 + a_0^2)$$

$$k_\mu = \omega n_\mu$$
$$k \cdot x = \omega x^+$$
$$k \cdot p = \omega p^+$$

- 'Shifted mass' in a plane wave, intensity a_0 .
- Discrete spectrum?

Sengupta 1952

Zel'dovich 1967, Oleinik 1967

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Debate

Divergences? Oleinik 1967	Higher loops? Becker & Mitter 1976	No mass shift! Fried & Eberly 1964	Mass shift is there Kibble 1965
Finite mass reform. Reiss 1966	Non-pert. effect Reiss 1966	Pert. effect Lavelle 2012	What about pulses? Corson & Peatross PRA 85 (2012) Mackenroth & Di Piazza PRA 85

The shifted mass: observation

1. Compton Scattering.
2. 'Nonlinear Compton'.

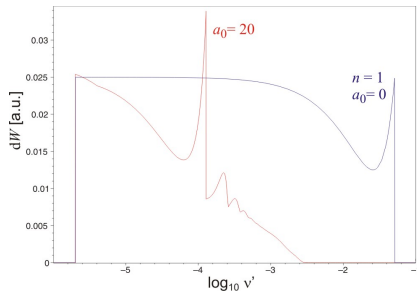
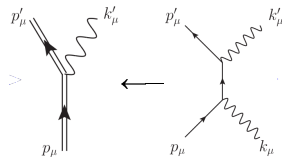
● m_* \implies frequency shift.

Kibble 1965

→ Spectrum ($\nu' = \omega'/m$)

☹ **Never** observed.

(N.B. undulators!)

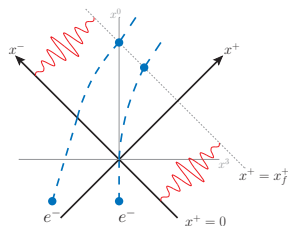


Answers from lightfront quantisation

- ▶ Lightcone quantisation:

$$P^-(x^+) |p_\mu\rangle = \pi^-(x^+) |p_\mu\rangle$$

- Particle content of [free theory](#).



Answers from lightfront quantisation

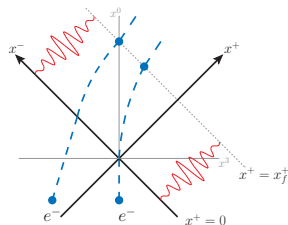
- ▶ Lightcone quantisation:

$$P^-(x^+) |p_\mu\rangle = \pi^-(x^+) |p_\mu\rangle$$

- Particle content of **free theory**.
- Time dependence \implies no explicit Lorentz invariance.
- All poles contribute. **Resum** contributions

$$G \sim \int dp \delta(p^2 - m^2) \varphi_p(x) \varphi_p^*(y)$$

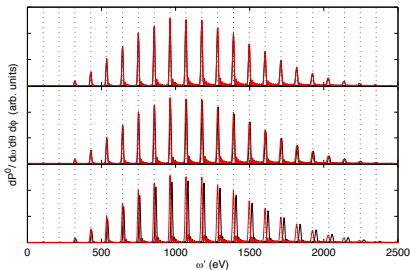
- Off shell poles = going onto **ordinary mass-shell**.
- Källén-Lehmann in a background field.



Living on the edge

- Poles/mass shift: fingerprint of beam shape.
- Requires **fine tuning**.

Harvey, Heinzl, Ilderton, Marklund PRL 109 (2012)



Laser

- $40\mu\text{m}$ spot radius.
- $a_0 \simeq 2$, 800nm .

Electron beam

- 5Mev , $8\mu\text{m}$ radius.
- e^- see a plane wave.

REGAE at DESY

- **Plane wave** vs. Gaussian beam.
- Peaks = mass-shift signals.

Radiation reaction from QED

- Classical radiation reaction: LAD \implies runaways.
→ Different classical equations.
- Measurable at 10^{23} W/cm²?
Di Piazza et al. Rev. Mod. Phys. 84 (2012), Heinzl Int. J. Mod. Phys. A27 (2012), Harvey, Heinzl, Marklund PRD 84 (2011), Di Piazza, Hatsagortsyan, Keitel, PRL 102 (2009), Bulanov et al. PRE 84 (2011)
- Radiation Reaction from QED?
- Progress using [lightfront](#) quantisation. Ilderton & Torgrimsson (2013)

See talk by Greger Torgrimsson

Pair production → zero modes

- Dirac-Heisenberg-Wigner function $W(x, p)$.

Wigner Phys.Rev.40 (1932), Heisenberg Z.Phys.90 (1934), Dirac Proc.Camb.Phil.Soc.30 (1934)

- Phase space (quasi) probability distribution.
- Instant and front forms:

$$W_I = \int d^3\mathbf{y} e^{ip \cdot y} \langle 0 | \psi(x + \frac{y}{2}) e^{ie \int dz \cdot A(z)} \psi^\dagger(x - \frac{y}{2}) | 0 \rangle \Big|_{y^0=0}$$

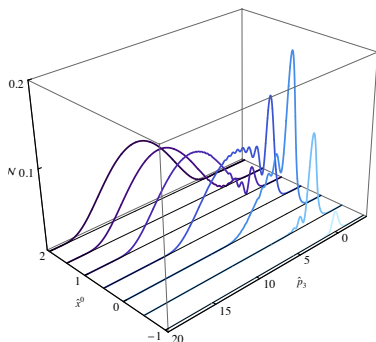
$$W_F = \int d^2y^+ dy^- e^{ip \cdot y} \langle 0 | \psi_+(x + \frac{y}{2}) e^{ie \int dz \cdot A(z)} \psi_+^\dagger(x - \frac{y}{2}) | 0 \rangle \Big|_{y^+=0}$$

- $W(x, p) \sim$ prob. momentum p at time/position x .

Compare: instant vs. front form

- In a **pair producing background**
- $W =$ momentum (p) distribution at time x .

■ Instant form.

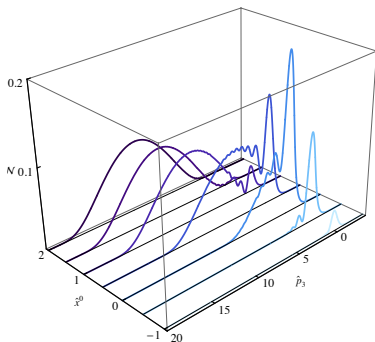


- Oscillations: transient effects.
- **Virtual** particles.
*Bialynicki-Birula, Gornicki, Rafelski, PRD (1991),
Bialynicki-Birula and Rudnicki (2011)*
- Bump moving out: **real** particles

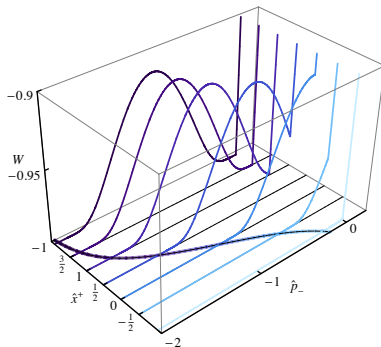
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■ Front form.



Compare: instant vs. front form

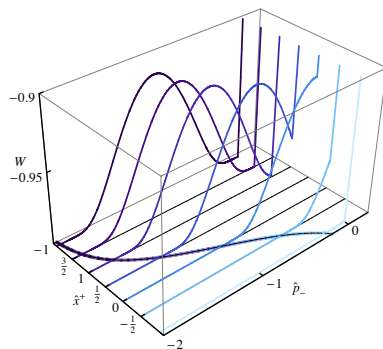
- In a pair producing background
- W = momentum (p) distribution at time x .

■ Front form.

- Only real particles.
- W supported on classical worldlines.
- Zero modes essential!

Tomaras et al. JHEP 0111 (2001),

Woodard, Nucl.Phys.Proc.Suppl 108 (2002)



Pair production?

→ Phenomenology.

☹ **Very far** from Sauter-Schwinger limit $E_S \sim 10^{18}$ V/m.

Heisenberg and Euler 1936; Sauter 1931; Schwinger 1951

- Next generation: $E < 10^{-2} E_S$.
- Many ways to 'lower' the threshold.

Schutzhold, Gies, Dunne PRL 101 (2008), PRD 80 (2009)

- **Geometry helps**. Simple illustration:

$$\text{Number of pairs} \simeq \frac{\text{Vol}}{\lambda_c^4} \frac{E^2}{E_S^2} \exp\left(-\pi \frac{E_S}{E}\right)$$

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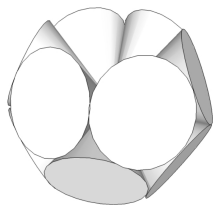
$$\text{Number of pairs} \simeq \frac{\text{Vol}}{\lambda_c^4} \frac{E^2}{E_S^2} \exp\left(-\pi \frac{E_S}{E}\right)$$

- **Focal Vol** $\sim 1\mu\text{m}^4$, 1 pair $\implies E \sim 0.06 E_S$.

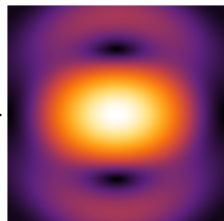
Focussed fields

- Multiple colliding pulses.

Bulanov et al, PRL 104 (2010)



→ near optimal focusing →
Gonoskov et al, 2013



- **Nonperturbative** calculations in real fields? / **in general?**
- Numerical approaches.
- PIC Codes + Monte-Carlo modules?
 - Would like to retain quantum and **lightfront** approach.

A non-perturbative approach

- Time dependent Basis Light-Front Quantisation.
- For explicitly time-dependent problems in QFT.

Xingbo Zhao, Anton Ilderton, Pieter Maris, James Vary (2013)

$$P^- = P_{\text{QED}}^- + V_{\text{ext}}(x^+)$$

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$$P^- = P_{\text{QED}}^- + V_{\text{ext}}(x^+)$$

- 1.) Solve QED. 😊

$$\hat{P}_{\text{QED}}^- |\beta\rangle = E_\beta |\beta\rangle$$

- 2.) Transitions due to V_{ext} :

$$|\beta\rangle \rightarrow |\beta'\rangle$$

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- 1.) Fock space truncation.

$$|e_{\text{phys}}\rangle = |e\rangle + |e\gamma\rangle + \dots$$

- 2.) Time step discretisation.

$$\mathcal{T}_+ e^{-\frac{i}{2} \int P^+} \rightarrow \left(1 - \frac{i}{2} P^+(x_n^+) \delta x^+\right) \dots$$

- Fully quantum, real time.

See talk by Xingbo Zhao.

Conclusions

- Intense laser fields offer prospects for
 - testing QED
 - new particle searches

- Old problems: [lightfront](#) provides answers.

- Effective mass
- Radiation reaction

Ilderton & Torgrimsson PRD (2012)

Ilderton & Torgrimsson (2013)

- Nonperturbative methods.

Talk by Xingbo Zhao