

DETERMINING THE HIGGS SPIN AND PARITY USING GLUON POLARIZATION

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arXiv:1304.2654

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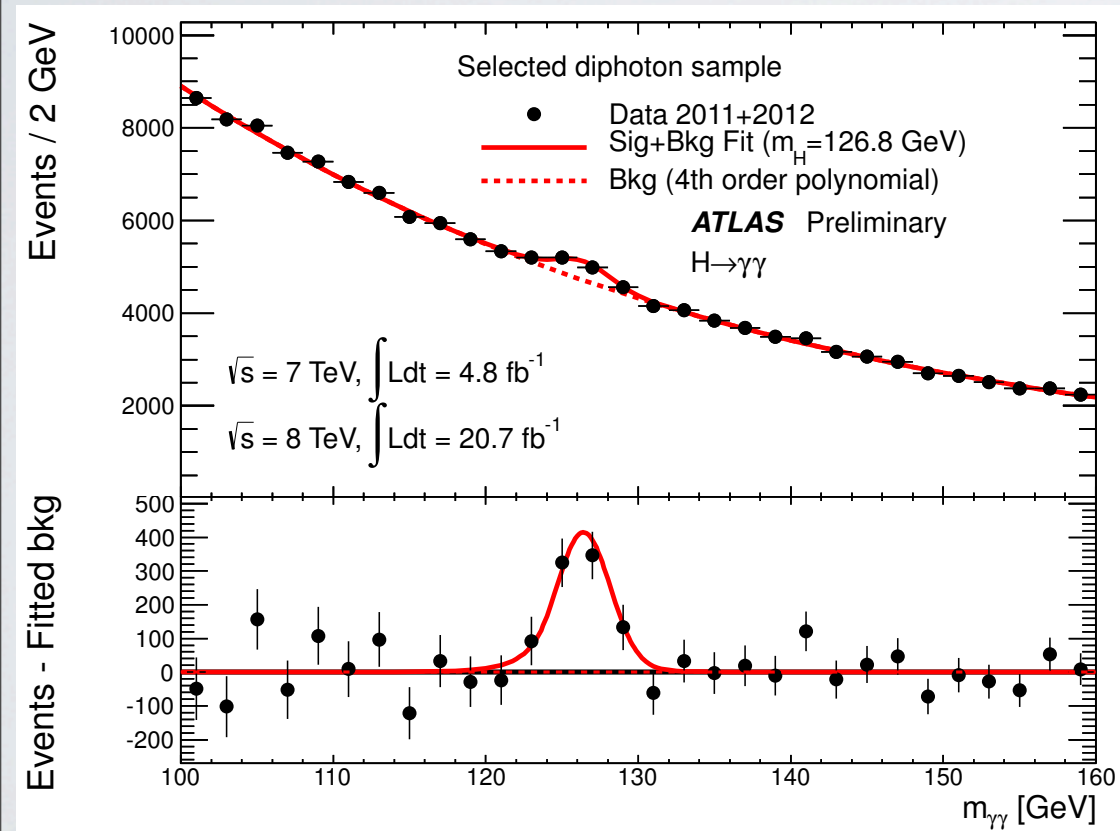
HIGGS J^P DETERMINATION

	postive parity	negative parity
spin-0	0^+	0^-
spin-1	\times	\times
spin-2	2_m^+ 2_h^+ $2_{h'}^+$ $2_{h''}^+$	2_h^-

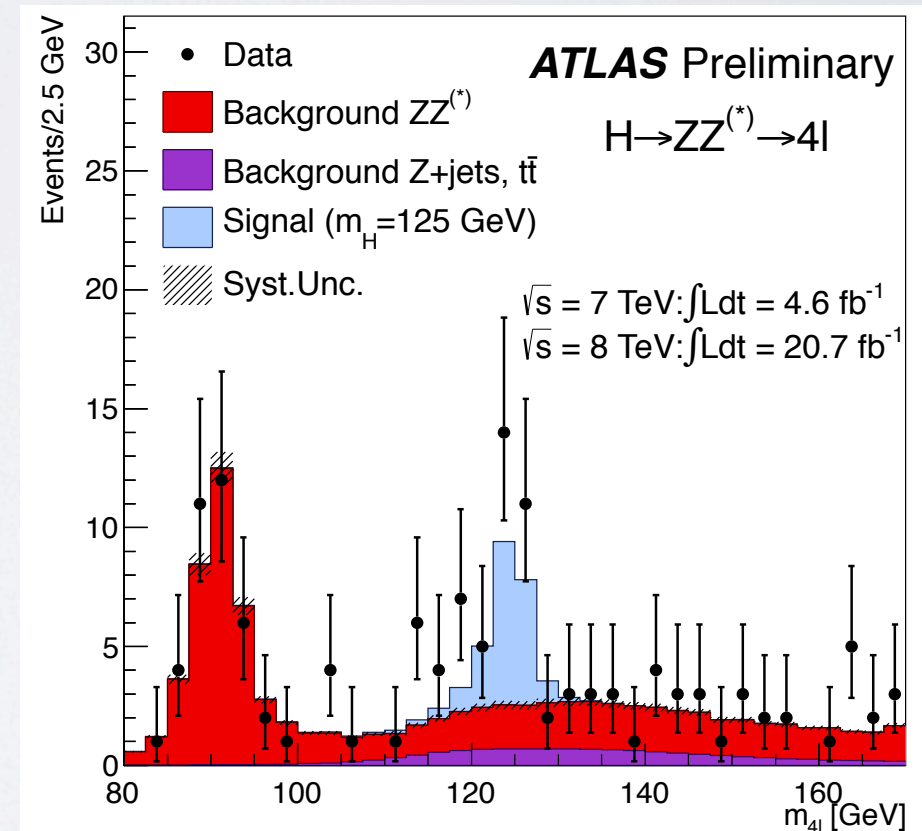
HIGGS J^P DETERMINATION

di-photon

$ZZ^* \rightarrow 4l$



ATLAS-CONF-2013-012

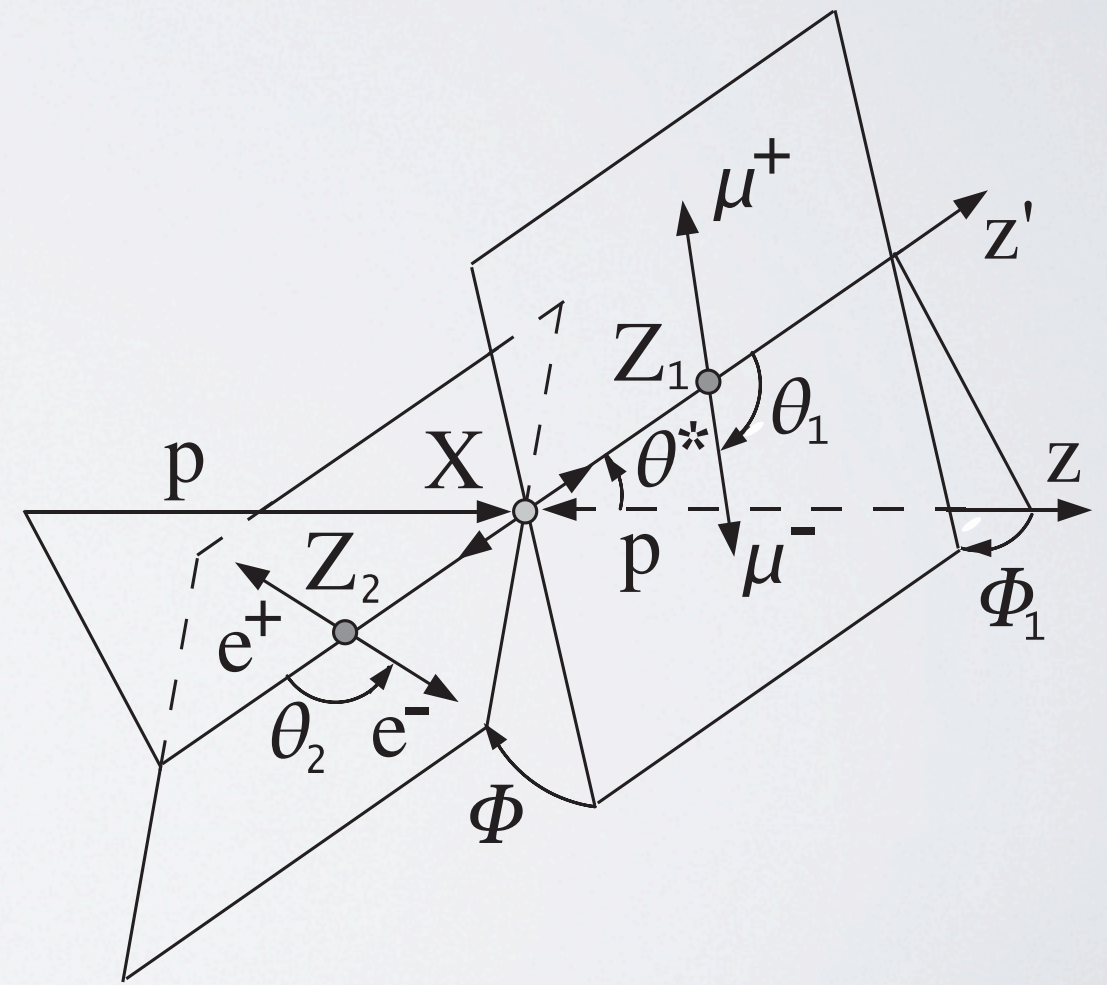
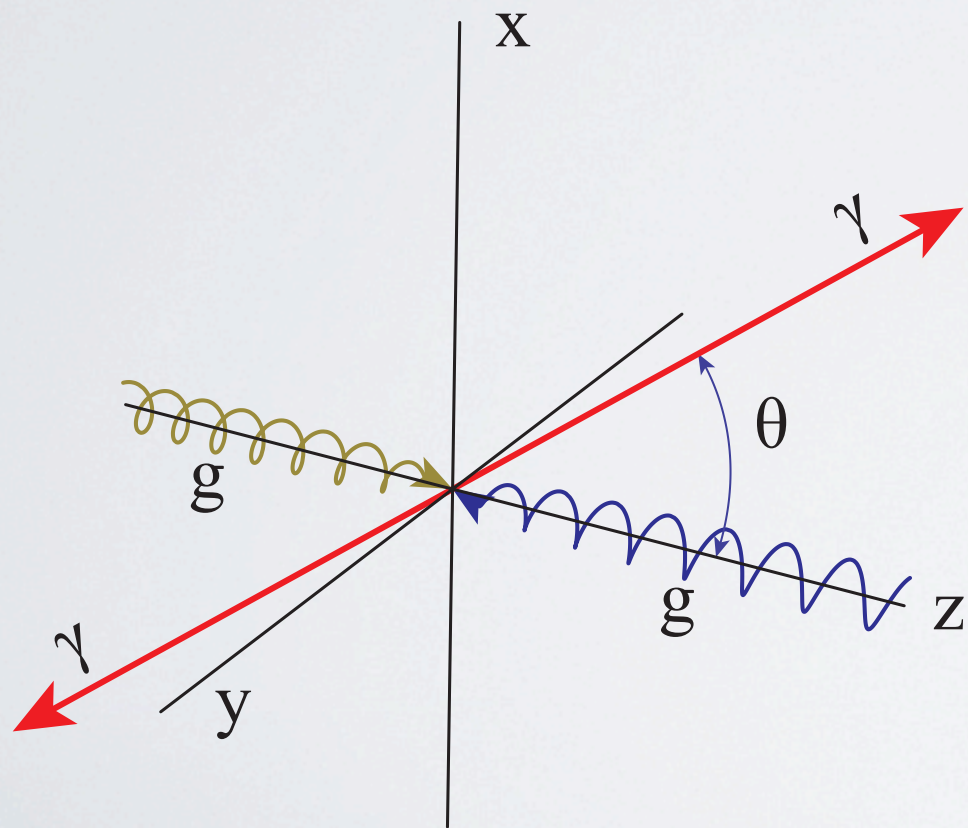


ATLAS-CONF-2013-013

HIGGS J^P DETERMINATION

di-photon

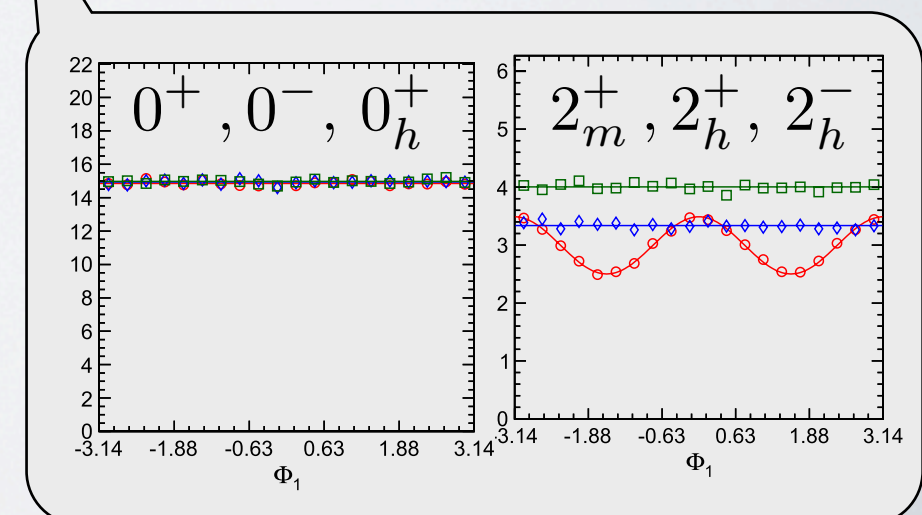
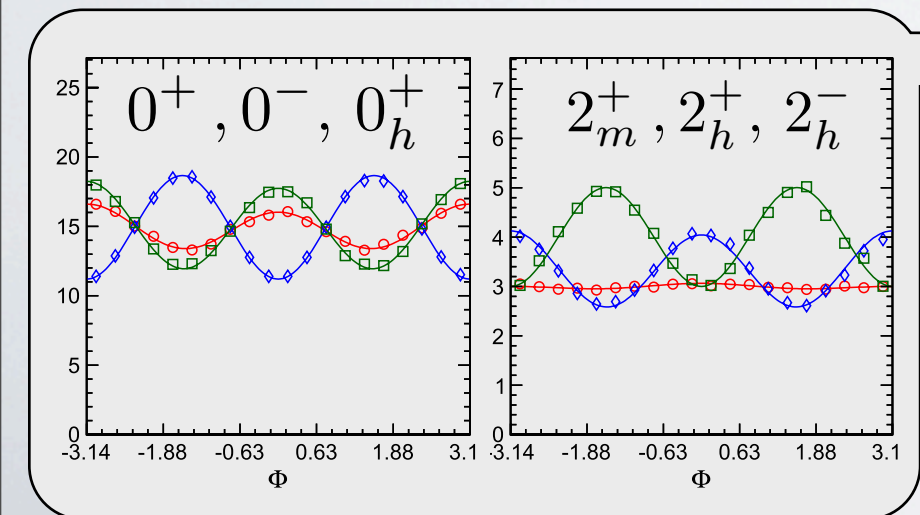
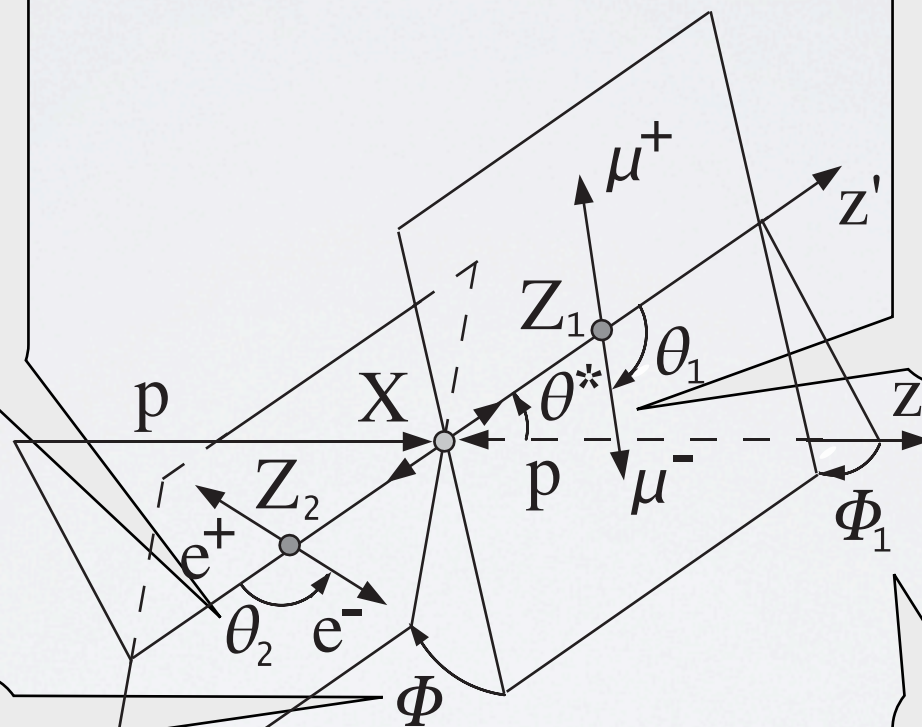
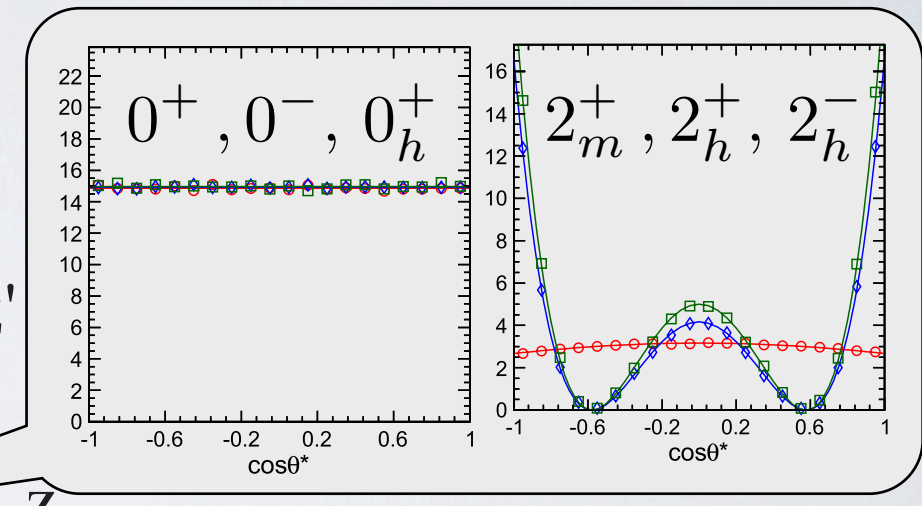
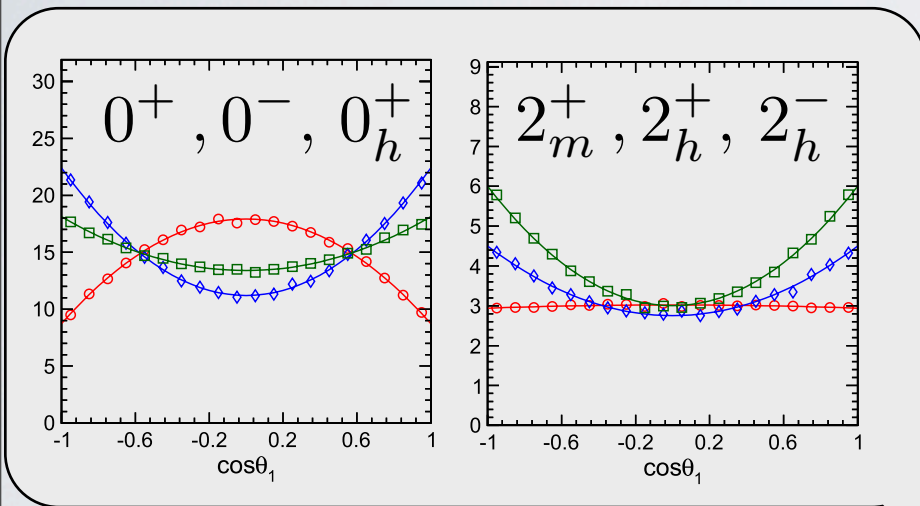
$$ZZ^* \rightarrow 4l$$



PR D81, 075022 (2010)

HIGGS J^P DETERMINATION

$$ZZ^* \rightarrow 4l$$

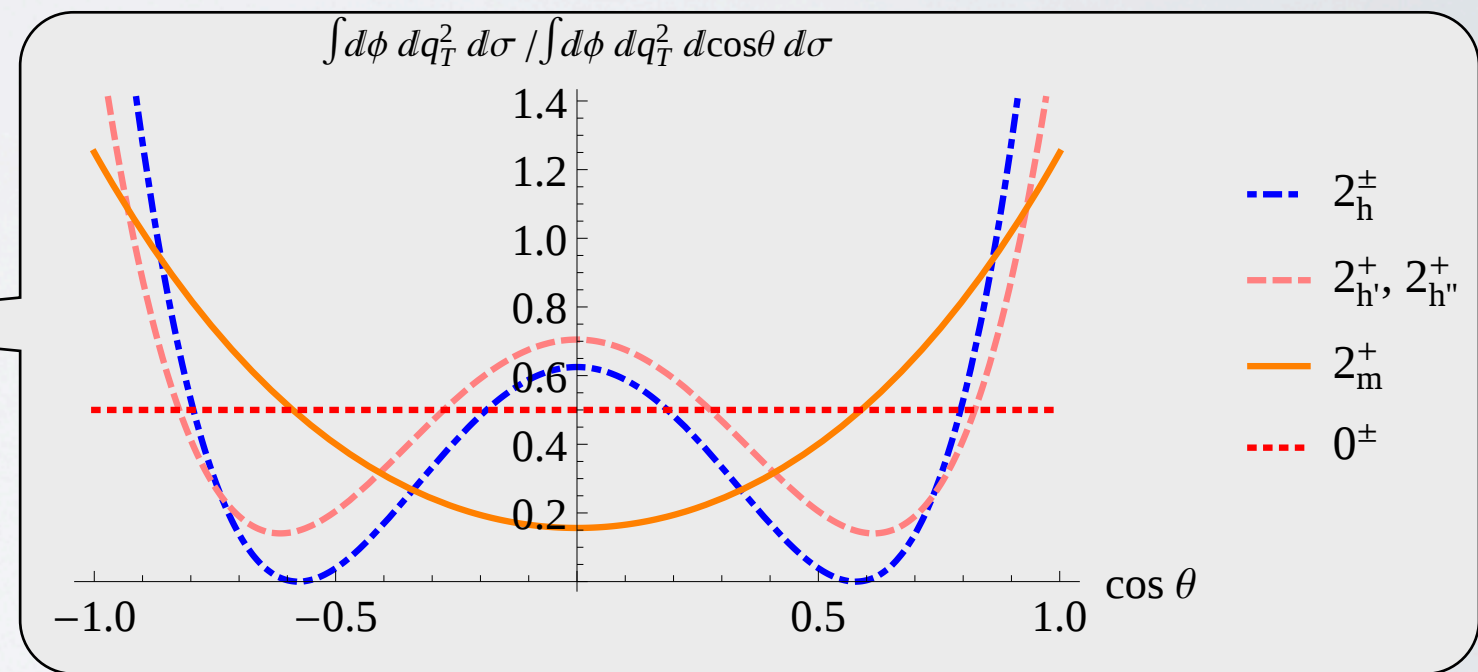
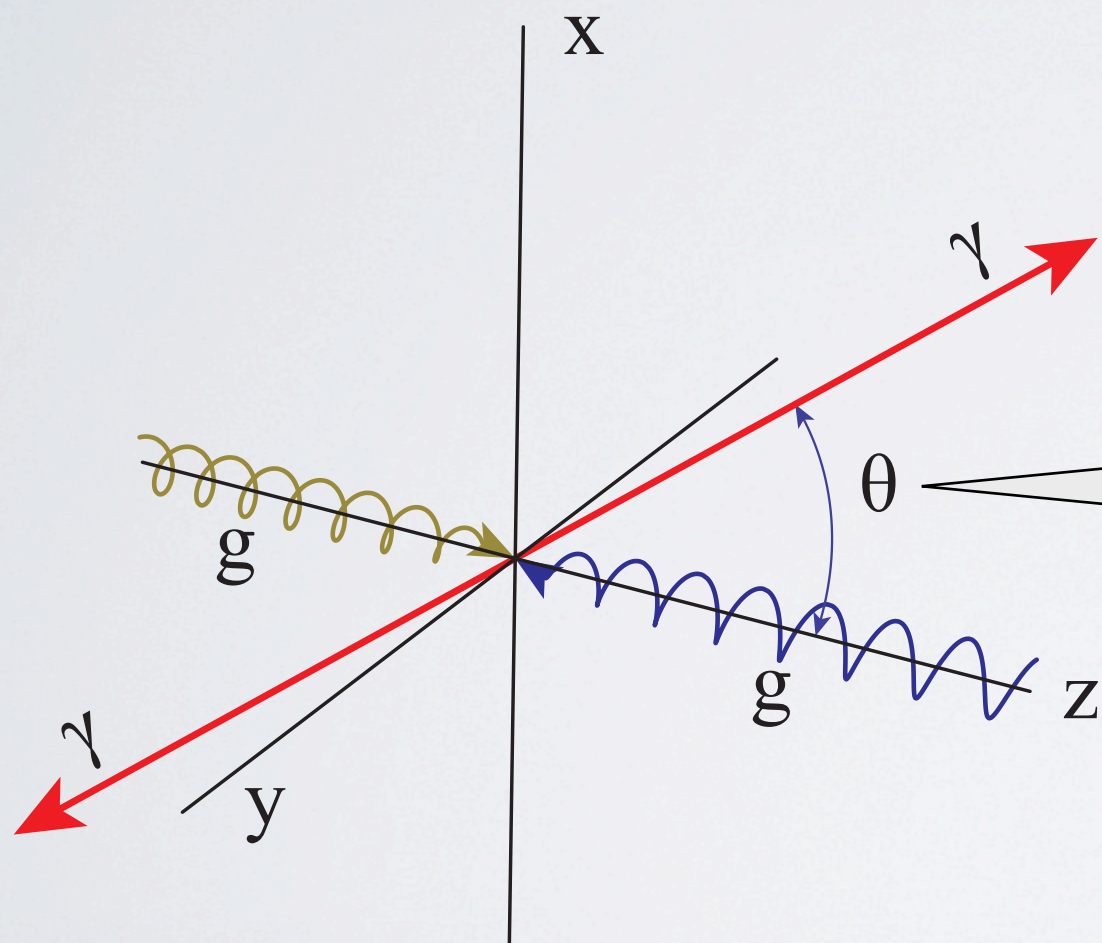


PR D81, 075022 (2010)

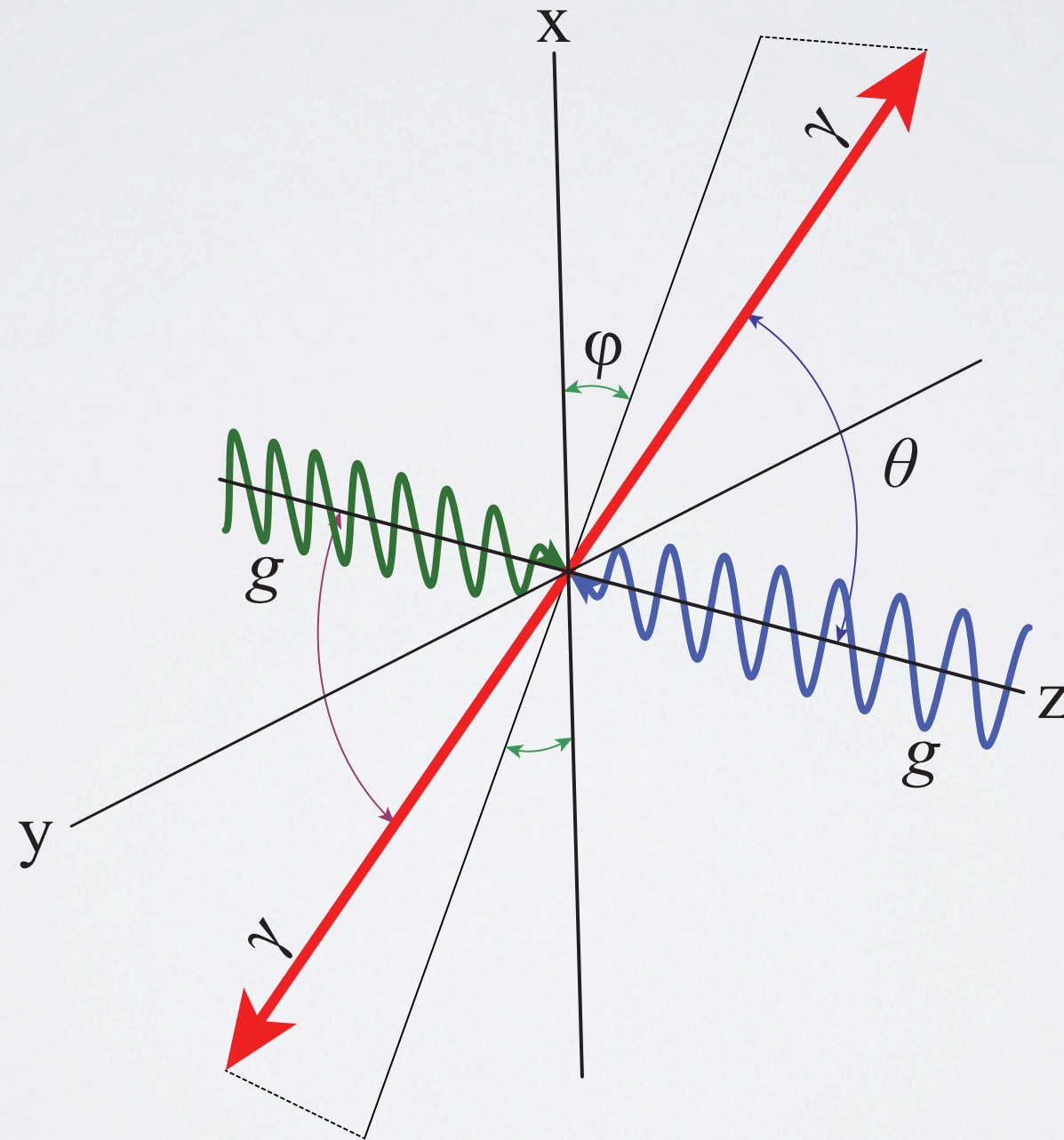
PR D86, 095031 (2012)

HIGGS J^P DETERMINATION

di-photon



WITH GLUON POLARIZATION



TMD FACTORIZATION

$$\frac{d\sigma}{d^4q d\Omega} \propto \int d^2\mathbf{p}_T d^2\mathbf{k}_T \delta^2(\mathbf{p}_T + \mathbf{k}_T - \mathbf{q}_T) \mathcal{M}_{\mu\rho\kappa\lambda} (\mathcal{M}_{\nu\sigma}{}^{\kappa\lambda})^* \Phi_g^{\mu\nu}(x_1, \mathbf{p}_T, \zeta_1, \mu) \Phi_g^{\rho\sigma}(x_2, \mathbf{k}_T, \zeta_2, \mu),$$

Hard scattering
matrix element

Transverse Momentum
Dependent (TMD)
correlator

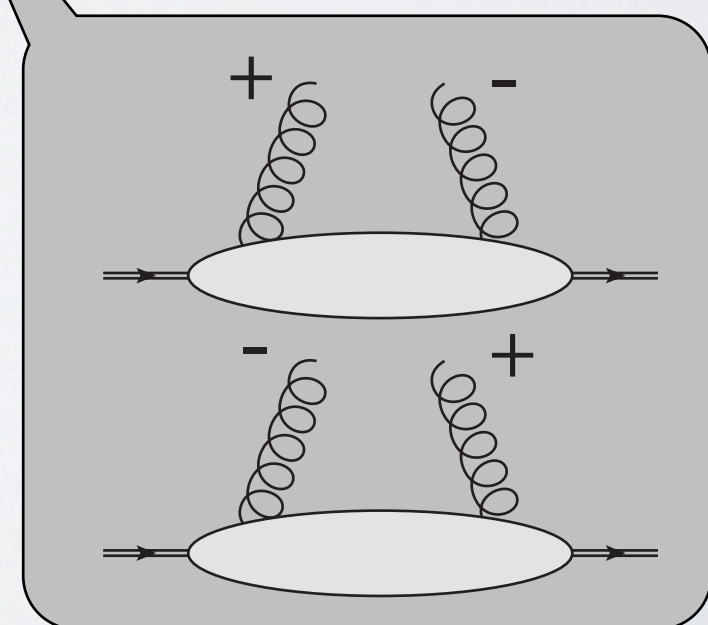
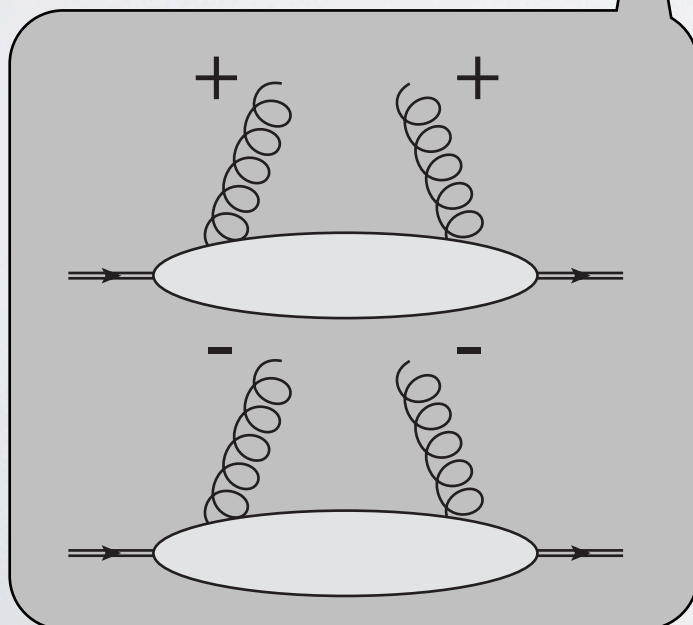
Ji, Ma, Yuan, JHEP07 (2005) 020

in principle also soft factor,
but vanishes (up to NLO) for $\zeta_{1,2} \rightarrow 3/2\sqrt{S}$

TMD FACTORIZATION

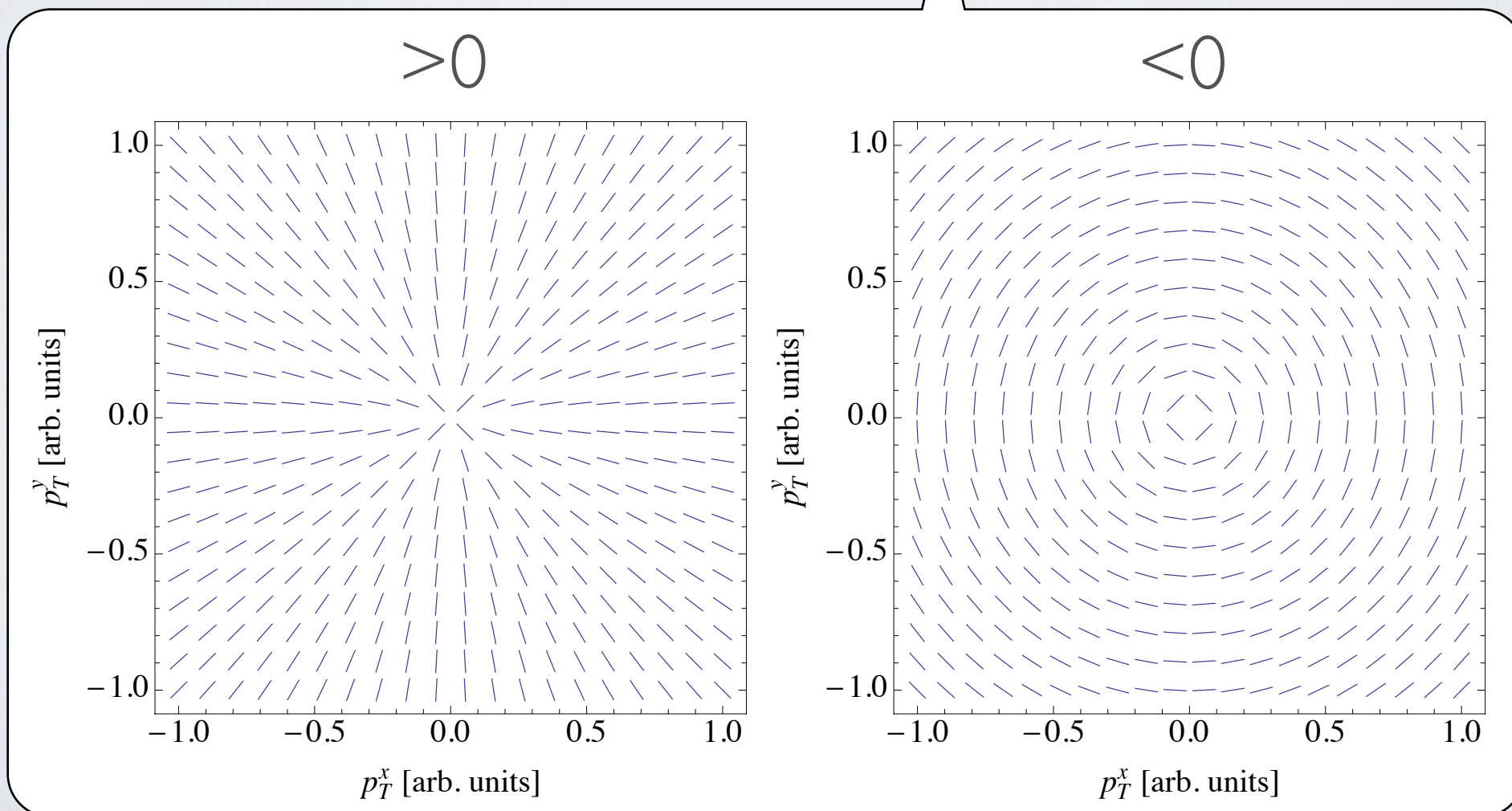
$$\frac{d\sigma}{d^4q d\Omega} \propto \int d^2\mathbf{p}_T d^2\mathbf{k}_T \delta^2(\mathbf{p}_T + \mathbf{k}_T - \mathbf{q}_T) \mathcal{M}_{\mu\rho\kappa\lambda} (\mathcal{M}_{\nu\sigma}{}^{\kappa\lambda})^* \Phi_g^{\mu\nu}(x_1, \mathbf{p}_T, \zeta_1, \mu) \Phi_g^{\rho\sigma}(x_2, \mathbf{k}_T, \zeta_2, \mu),$$

$$\begin{aligned} \Phi_g^{\mu\nu}(x, \mathbf{p}_T, \zeta, \mu) &\equiv 2 \int \frac{d(\xi \cdot P) d^2\xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + p_T) \cdot \xi} \text{Tr}_c \left[\langle P | F^{n\nu}(0) \mathcal{U}_{[0,\xi]}^{n[-]} F^{n\mu}(\xi) \mathcal{U}_{[\xi,0]}^{n[-]} | P \rangle \right]_{\xi \cdot P' = 0} \\ &= -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g - \left(\frac{p_T^\mu p_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{\mathbf{p}_T^2}{2M_p^2} \right) h_1^{\perp g} \right\} + \text{higher twist}, \end{aligned}$$

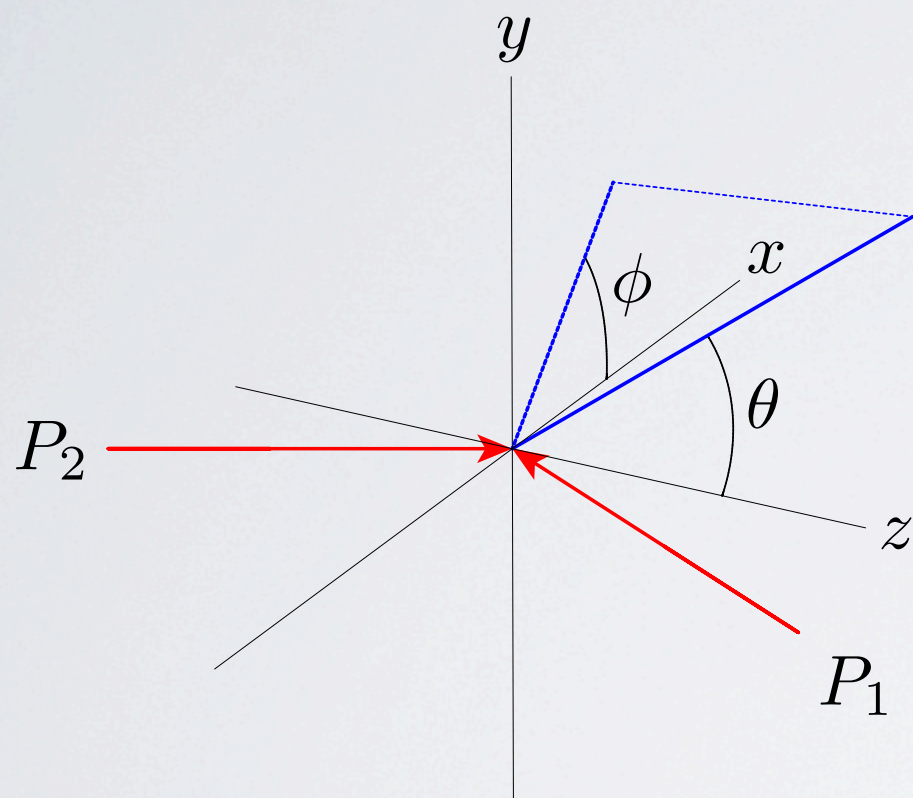


LINEARLY POLARIZED GLUON DISTRIBUTION

$$\begin{aligned} \Phi_g^{\mu\nu}(x, \mathbf{p}_T, \zeta, \mu) &\equiv 2 \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + p_T) \cdot \xi} \text{Tr}_c \left[\langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]}^{n[-]} F^{n\mu}(\xi) \mathcal{U}_{[\xi, 0]}^{n[-]} | P \rangle \right]_{\xi \cdot P' = 0} \\ &= -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g - \left(\frac{p_T^\mu p_T^\nu}{M_p^2} + g_T^{\mu\nu} \frac{\mathbf{p}_T^2}{2M_p^2} \right) h_1^{\perp g} \right\} + \text{higher twist,} \end{aligned}$$



GENERAL STRUCTURE

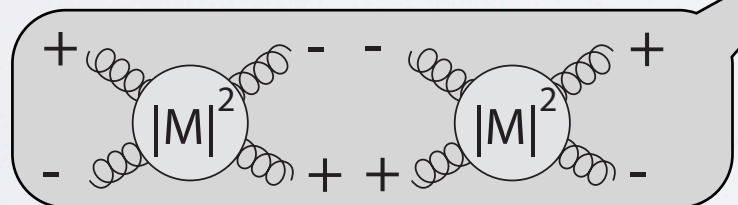
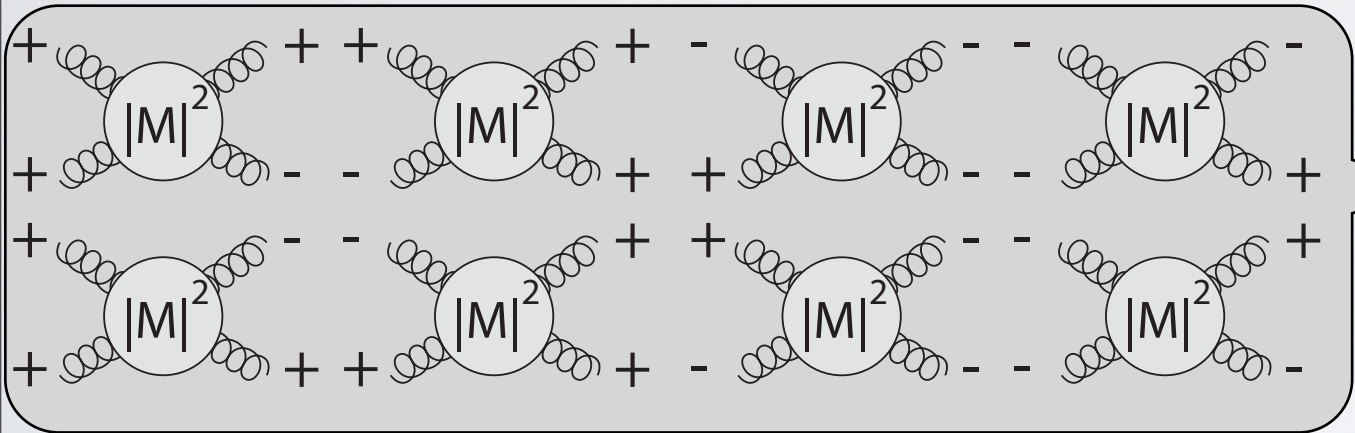
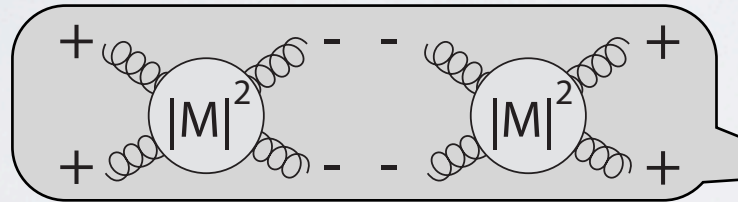
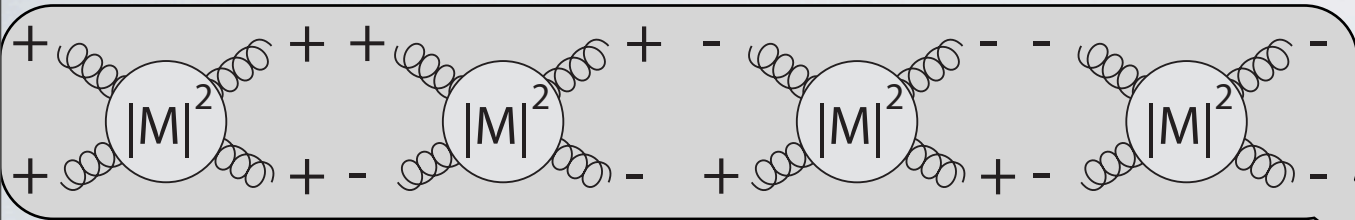


Collins-Soper frame

$$\begin{aligned}
 \frac{d\sigma}{d^4q d\Omega} \propto & \\
 & F_1(Q, \theta) \mathcal{C} [f_1^g f_1^g] + \\
 & F_2(Q, \theta) \mathcal{C} [w_2 h_1^{\perp g} h_1^{\perp g}] + \\
 & F_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} + h_1^{\perp g} f_1^g)] \cos(2\phi) + \\
 & F'_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} - h_1^{\perp g} f_1^g)] \sin(2\phi) + \\
 & F_4(Q, \theta) \mathcal{C} [w_4 h_1^{\perp g} h_1^{\perp g}] \cos(4\phi) + \\
 & \mathcal{O}(q_T/Q)
 \end{aligned}$$

ϕ azimuthal Collins-Soper angle

GENERAL STRUCTURE



$$\frac{d\sigma}{d^4q d\Omega} \propto$$

$$F_1(Q, \theta) \mathcal{C} [f_1^g f_1^g] +$$

$$F_2(Q, \theta) \mathcal{C} [w_2 h_1^{\perp g} h_1^{\perp g}] +$$

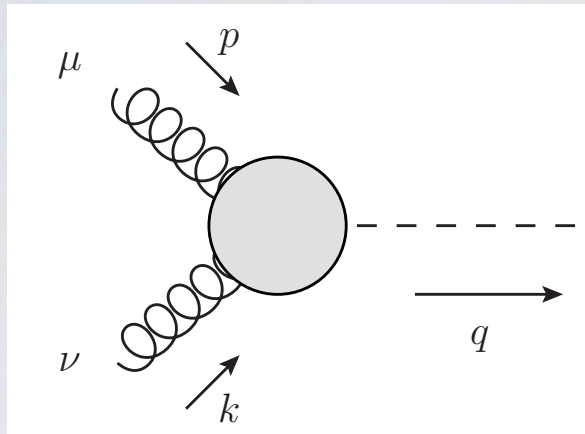
$$F_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} + h_1^{\perp g} f_1^g)] \cos(2\phi) +$$

$$F'_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} - h_1^{\perp g} f_1^g)] \sin(2\phi) +$$

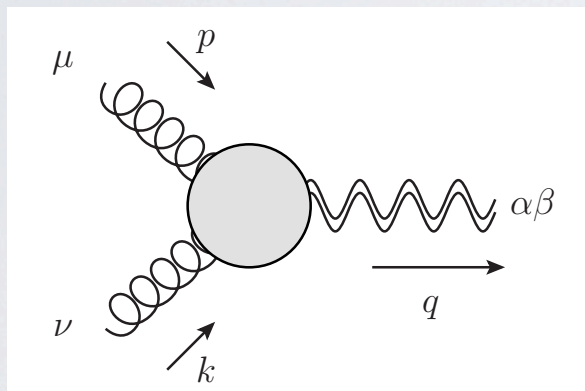
$$F_4(Q, \theta) \mathcal{C} [w_4 h_1^{\perp g} h_1^{\perp g}] \cos(4\phi) +$$

$$\mathcal{O}(q_T/Q)$$

PARTONIC AMPLITUDES



$$= a_1 q^2 g^{\mu\nu} + a_3 \epsilon^{pk\mu\nu}$$



$$= \frac{1}{2} c_1 q^2 g^{\mu\alpha} g^{\nu\beta} + [c_2 q^2 g^{\mu\nu} + c_5 \epsilon^{pk\mu\nu}] \frac{(p-k)^\alpha (p-k)^\beta}{q^2}$$

scenario	0^+	0^-	2_m^+	2_h^+	$2_{h'}^+$	$2_{h''}^+$	2_h^-
a_1	1	0	-	-	-	-	-
a_3	0	1	-	-	-	-	-
c_1	-	-	1	0	1	1	0
c_2	-	-	$-\frac{1}{4}$	1	1	$-\frac{3}{2}$	0
c_5	-	-	0	0	0	0	1

GENERAL STRUCTURE

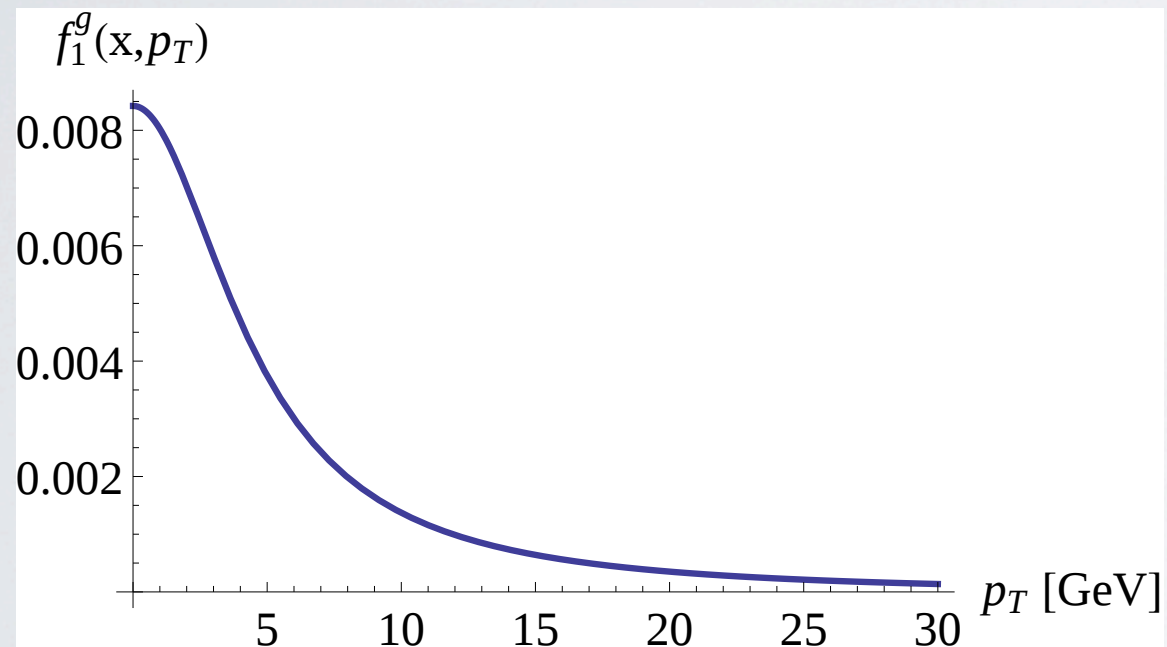
$$\begin{aligned} \frac{d\sigma}{d^4q d\Omega} \propto & \\ & F_1(Q, \theta) \mathcal{C} [f_1^g f_1^g] + \\ & F_2(Q, \theta) \mathcal{C} [w_2 h_1^{\perp g} h_1^{\perp g}] + \\ & F_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} + h_1^{\perp g} f_1^g)] \cos(2\phi) + \\ & F'_3(Q, \theta) \mathcal{C} [w_3 (f_1^g h_1^{\perp g} - h_1^{\perp g} f_1^g)] \sin(2\phi) + \\ & F_4(Q, \theta) \mathcal{C} [w_4 h_1^{\perp g} h_1^{\perp g}] \cos(4\phi) + \\ & \mathcal{O}(q_T/Q) \end{aligned}$$

- Unpolarized distribution
- gluon TMD
- f_1^g

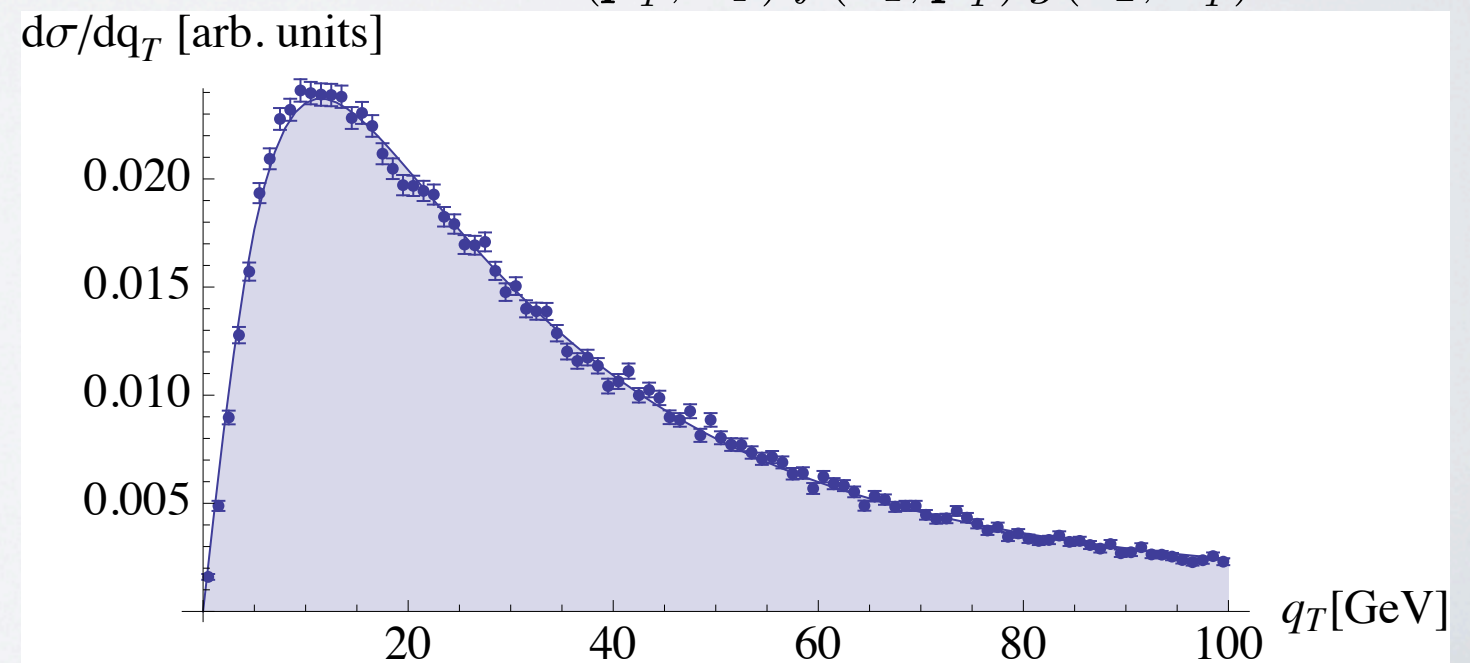
- Polarized distribution
- linearly polarized gluon distribution
- $h_1^{\perp g}$

UNPOLARIZED DISTRIBUTION

$$f_1^g(x, \mathbf{p}_T^2, \frac{3}{2}\sqrt{s}, M_h) = \frac{A_0 M_0^2}{M_0^2 + \mathbf{p}_T^2} \exp\left[-\frac{\mathbf{p}_T^2}{a\mathbf{p}_T^2 + 2\sigma^2}\right]$$



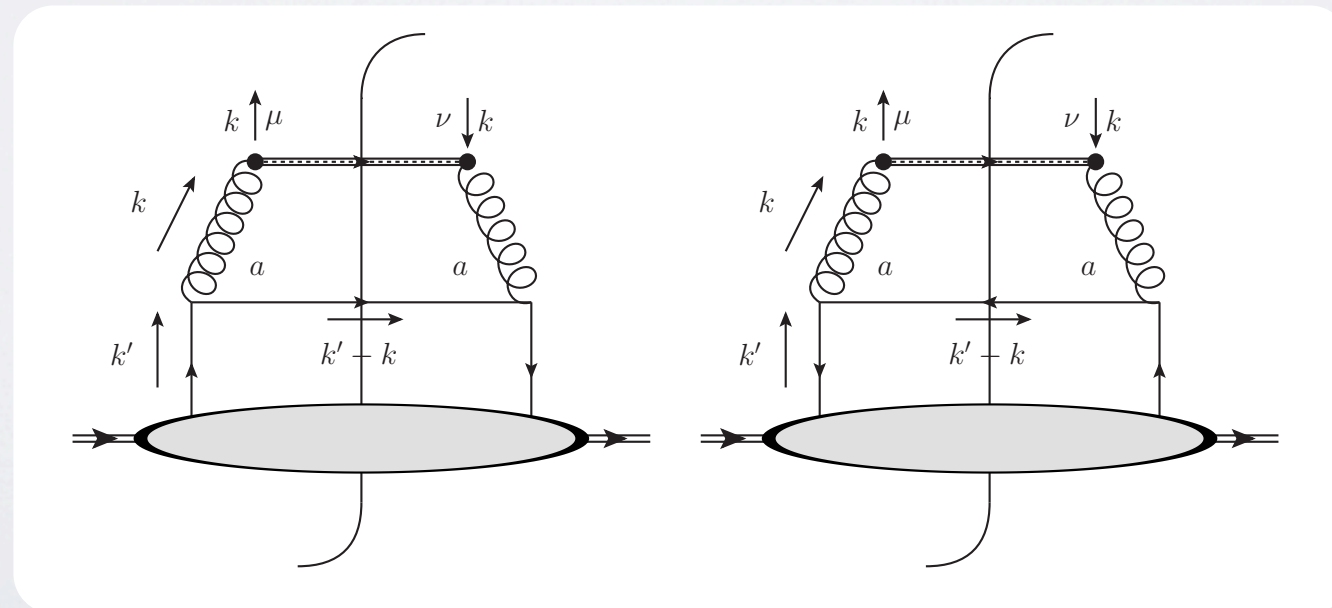
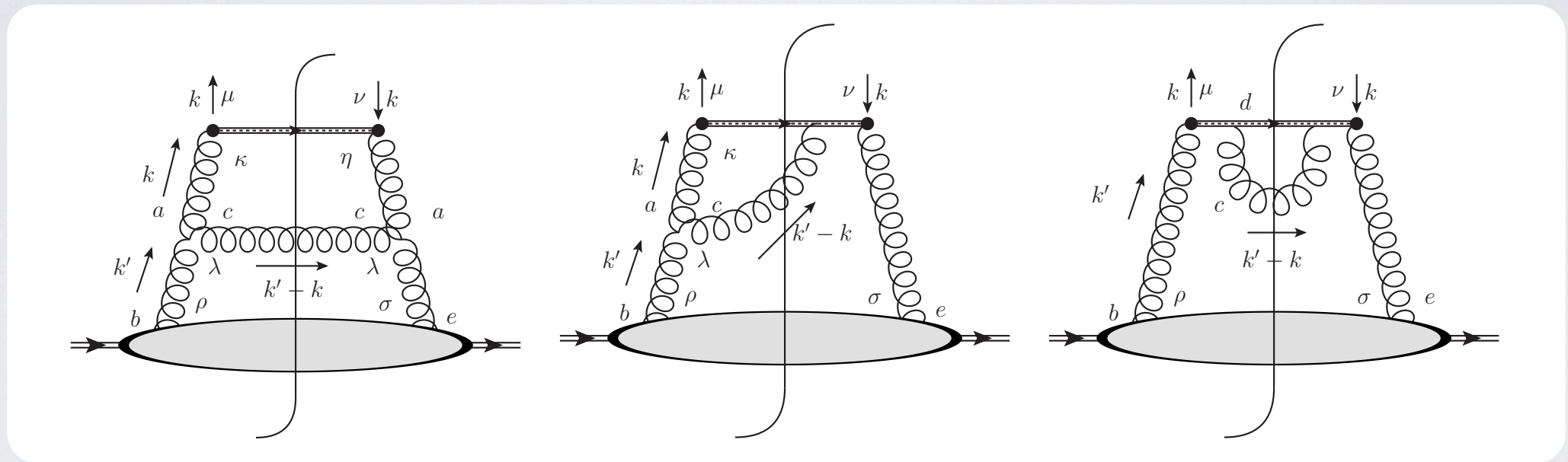
$$\mathcal{C}[w f g] \equiv \int d^2\mathbf{p}_T \int d^2\mathbf{k}_T \delta^2(\mathbf{p}_T + \mathbf{k}_T - \mathbf{q}_T) w(\mathbf{p}_T, \mathbf{k}_T) f(x_1, \mathbf{p}_T^2) g(x_2, \mathbf{k}_T^2)$$



POWHEG+Pythia 8 Higgs q_T distribution

POLARIZED DISTRIBUTION

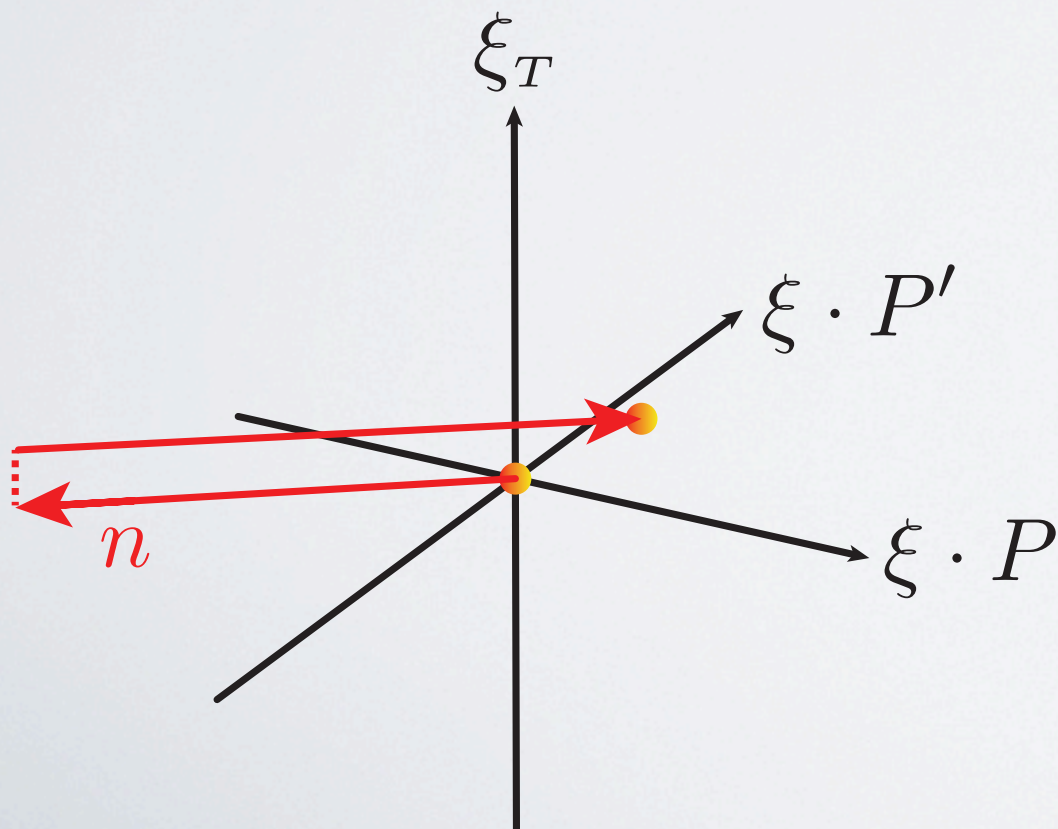
$$\Phi_g^{\mu\nu}(x, \mathbf{p}_T, \zeta, \mu) \equiv 2 \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + p_T) \cdot \xi} \text{Tr}_c \left[\langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]}^{n[-]} F^{n\mu}(\xi) \mathcal{U}_{[\xi, 0]}^{n[-]} | P \rangle \right]_{\xi \cdot P' = 0}$$



POLARIZED DISTRIBUTION

$$\Phi_g^{\mu\nu}(x, \mathbf{p}_T, \zeta, \mu) \equiv 2 \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + p_T) \cdot \xi} \text{Tr}_c \left[\langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]}^{n[-]} F^{n\mu}(\xi) \mathcal{U}_{[\xi, 0]}^{n[-]} | P \rangle \right]_{\xi \cdot P' = 0}$$

$$\begin{aligned} \mathcal{U}_{[0, \xi]}^{n[-]} &\equiv \mathcal{U}_{[0, -\infty]}^n \mathcal{U}_{[-\infty, \xi]}^n \\ &= \mathcal{P} e^{-ig \int_0^{-\infty} dy A^n(0 + ny)} \mathcal{P} e^{-ig \int_{-\infty}^0 dy A^n(\xi + ny)} \end{aligned}$$

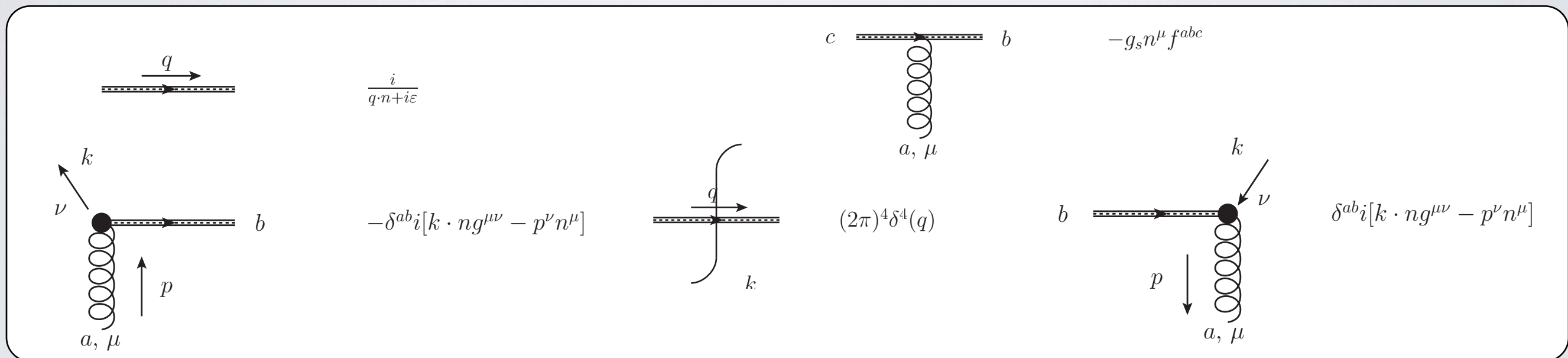


$$n \propto \frac{1}{\zeta} P + \frac{\zeta}{P \cdot P'} P'$$

$$\zeta \equiv \frac{2(n \cdot P)}{\sqrt{n^2}}$$

POLARIZED DISTRIBUTION

$$\Phi_g^{\mu\nu}(x, \mathbf{p}_T, \zeta, \mu) \equiv 2 \int \frac{d(\xi \cdot P) d^2 \xi_T}{(xP \cdot n)^2 (2\pi)^3} e^{i(xP + p_T) \cdot \xi} \text{Tr}_c \left[\langle P | F^{n\nu}(0) \mathcal{U}_{[0, \xi]}^{n[-]} F^{n\mu}(\xi) \mathcal{U}_{[\xi, 0]}^{n[-]} | P \rangle \right]_{\xi \cdot P' = 0}$$



POLARIZED DISTRIBUTION

in $\zeta \rightarrow \infty$ limit results compatible with the literature

$$f_{1\text{tail}}^g(x, \mathbf{k}_T) = -\frac{4g_s^2}{(2\pi)^3 k_T^2} \int_x^1 \frac{dz}{z} \left[C_A \left\{ \frac{1-z}{z} + z(1-z) + \frac{z}{(1-z)^+} - \frac{1}{2} \delta(z-1) \left[1 + \log \left(\frac{-k_T^2}{\zeta^2} \right) - \log x^2 (1-x)^2 \right] \right\} f_1^g \left(\frac{x}{z} \right) + C_F \frac{1+(1-z)^2}{2z} \sum_{q, \bar{q}} f_1^q \left(\frac{x}{z} \right) \right]$$

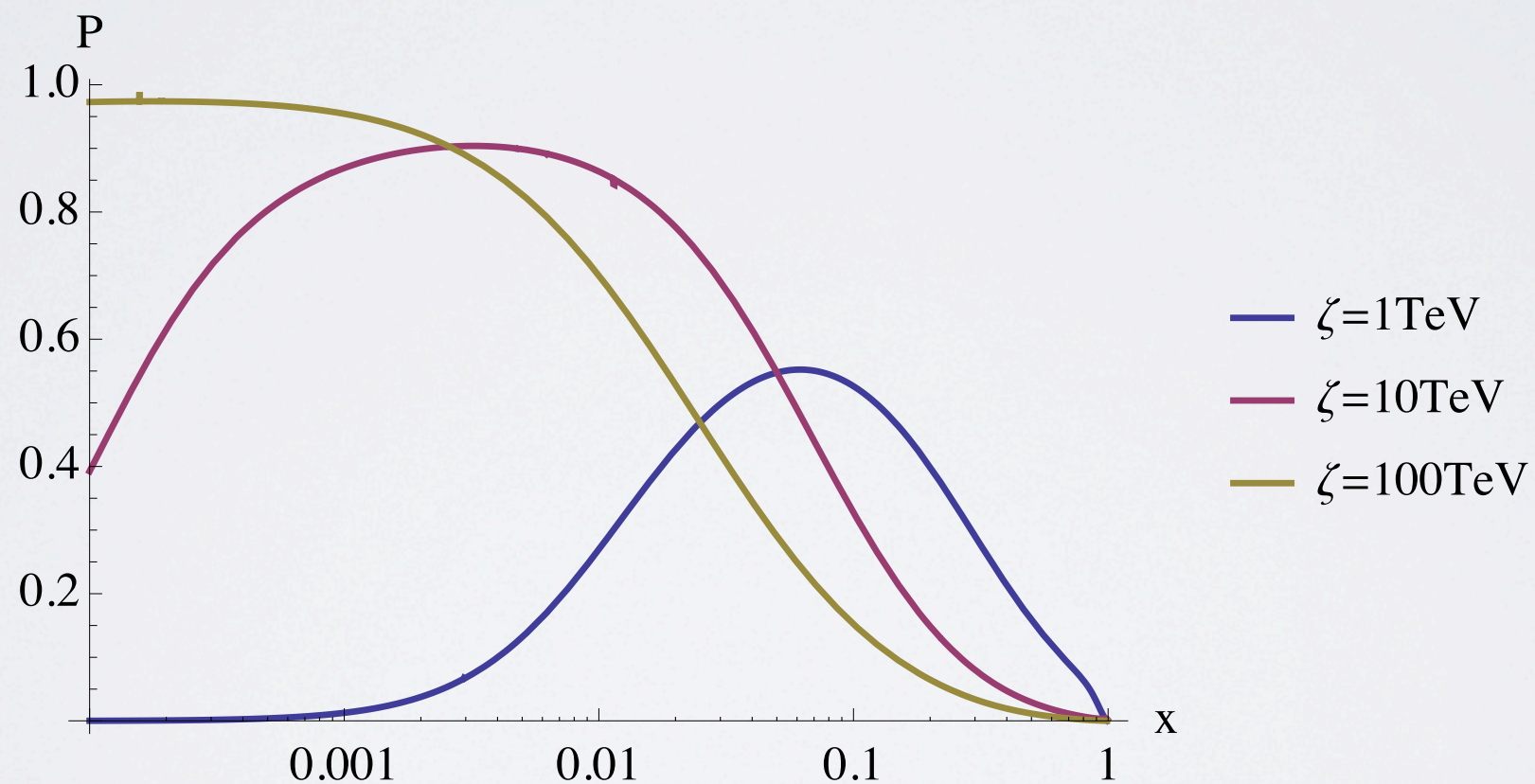
cf. Ji, Ma, Yuan
JHEP07 (2005) 020

$$h_{1\text{tail}}^{\perp g}(x, \mathbf{k}_T) = \frac{4g_s^2}{(2\pi)^3 k_T^2} \frac{2M^2}{k_T^2} \int_x^1 \frac{dz}{z} \frac{1-z}{z} \left[C_A f_1^g \left(\frac{x}{z} \right) + C_F \sum_{q, \bar{q}} f_1^q \left(\frac{x}{z} \right) \right]$$

cf. Sun, Xiao, Yuan
PR D84, 094005 (2011)

DEGREE OF POLARIZATION

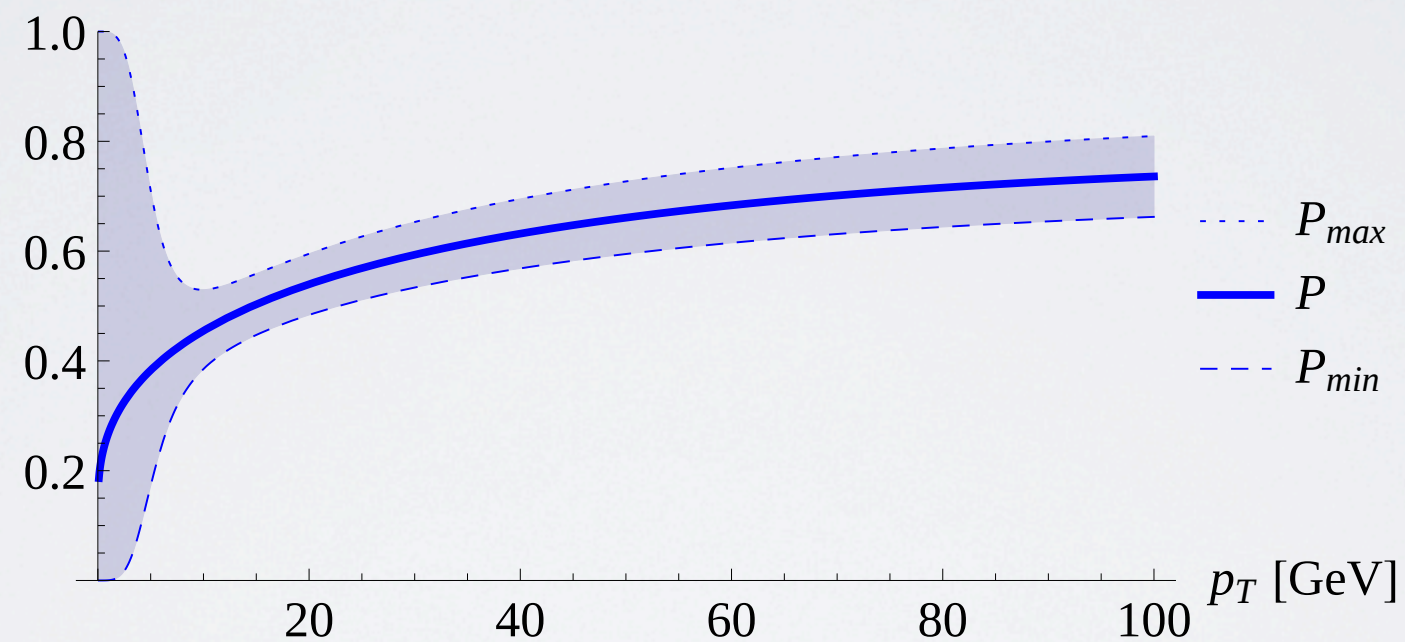
$$h_1^{\perp g}(x, \mathbf{p}_T, \zeta, \mu) = \mathcal{P}(x, \mathbf{p}_T^2, \zeta) \frac{2M_p^2}{\mathbf{p}_T^2} f_1^g(x, \mathbf{p}_T, \zeta, \mu),$$



CGC model predicts full polarization at small x:
A. Metz and J. Zhou, Phys. Rev. D 84, 051503 (2011)

DEGREE OF POLARIZATION

$$h_1^{\perp g}(x, \mathbf{p}_T, \zeta, \mu) = \mathcal{P}(x, \mathbf{p}_T^2, \zeta) \frac{2M_p^2}{\mathbf{p}_T^2} f_1^g(x, \mathbf{p}_T, \zeta, \mu),$$

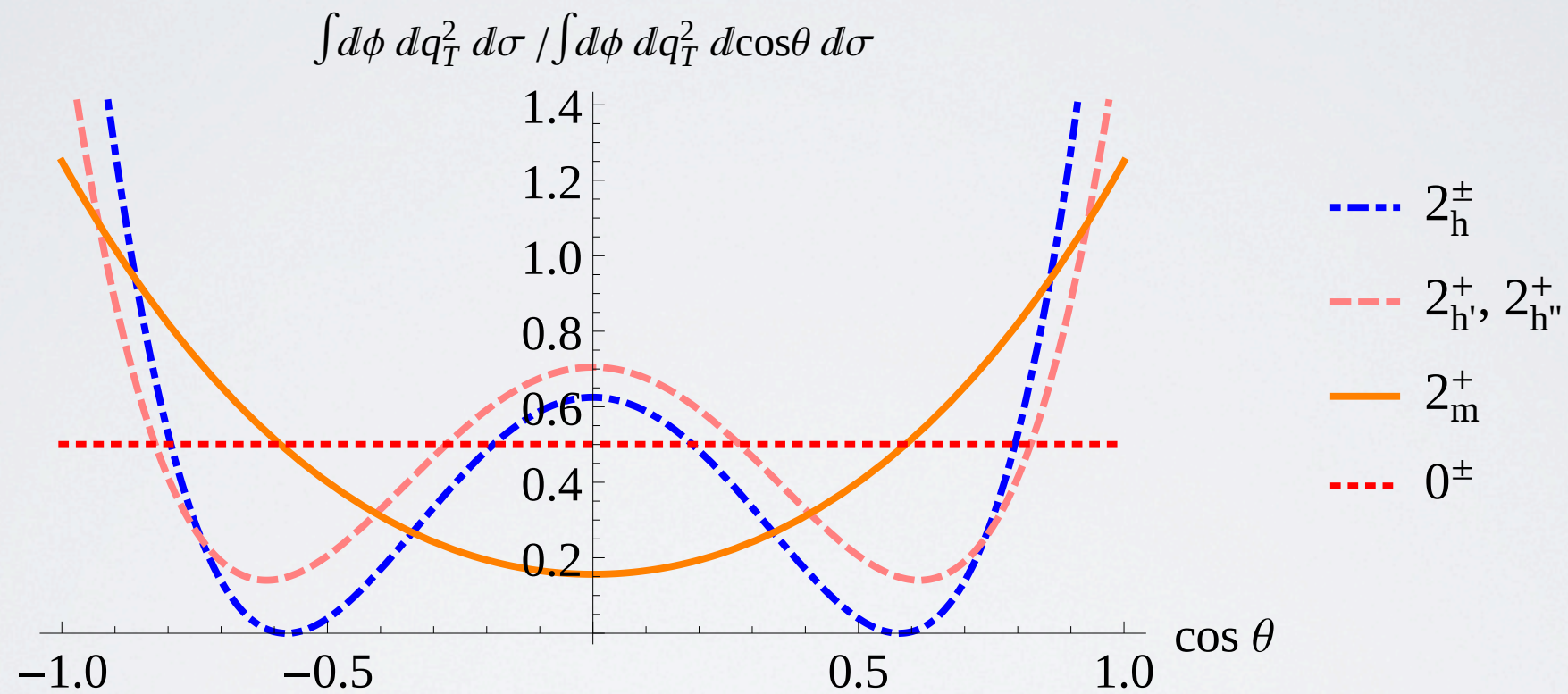


$$\mathcal{P}_{min} \equiv \frac{\mathbf{p}_T^4}{p_0^4 + \mathbf{p}_T^4} 0.9 \mathcal{P}_{p\text{QCD}}(x, \mathbf{p}_T^2),$$

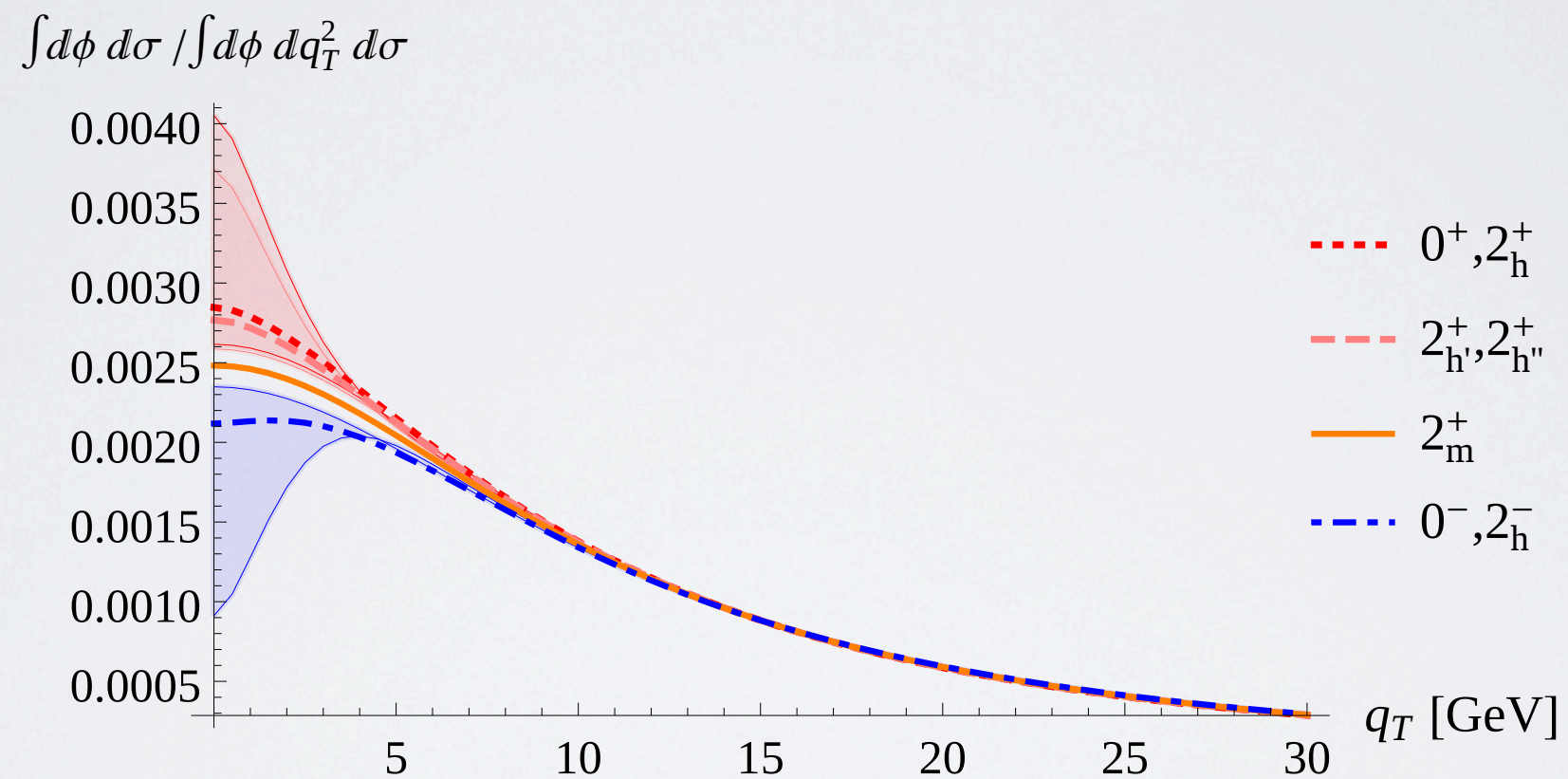
$$\mathcal{P} \equiv \mathcal{P}_{p\text{QCD}}(x, \mathbf{p}_T^2),$$

$$\mathcal{P}_{max} \equiv 1 - \frac{\mathbf{p}_T^4}{p_0^4 + \mathbf{p}_T^4} [1 - 1.1 \mathcal{P}_{p\text{QCD}}(x, \mathbf{p}_T^2)],$$

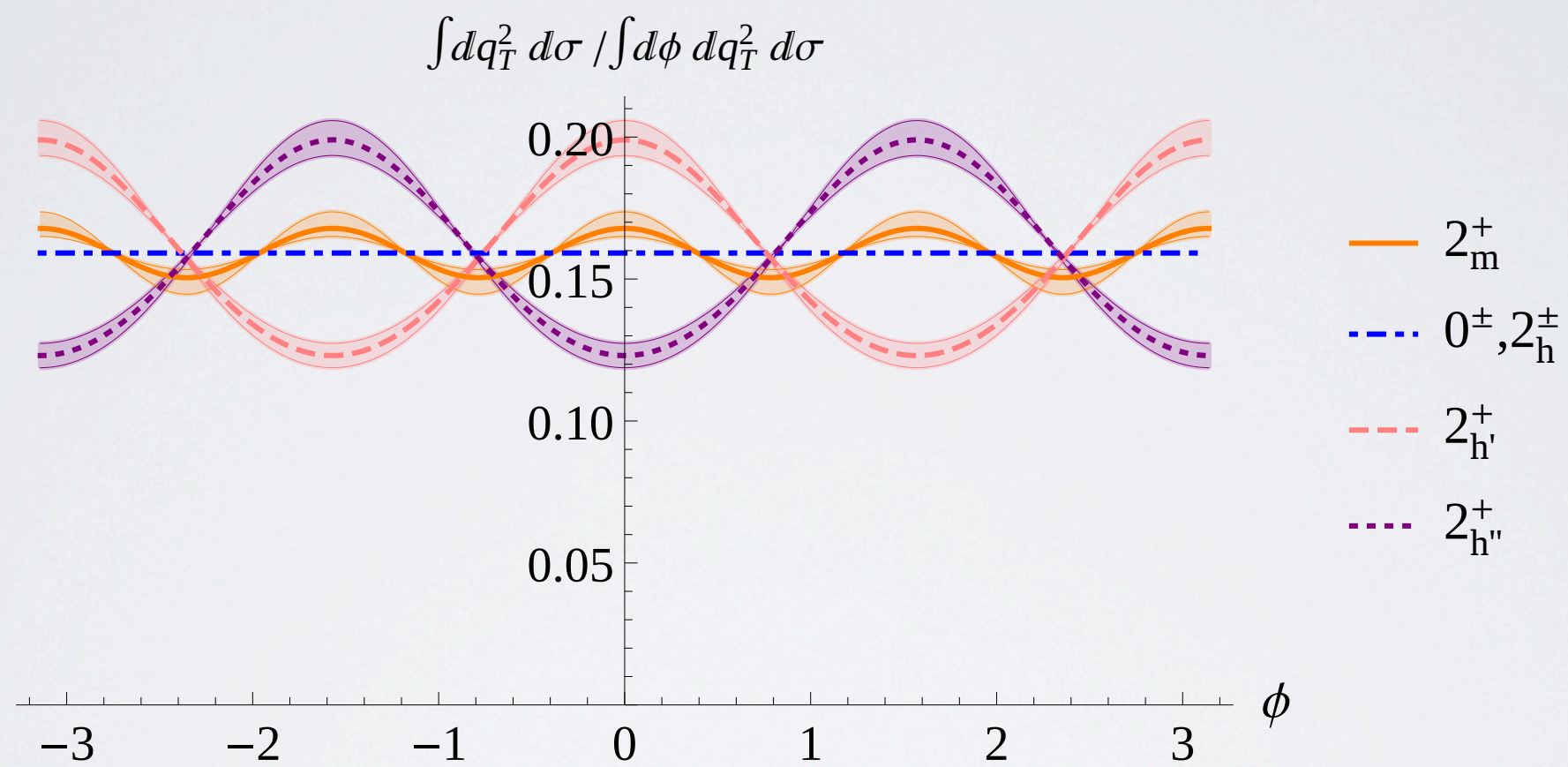
COS θ DISTRIBUTION



TRANSVERSE MOMENTUM DISTRIBUTION



Φ DISTRIBUTION



REMARKS

- spin-2 with CP violating coupling \leftrightarrow $\sin^2\phi$ dependence
- $gg \rightarrow \text{box} \rightarrow \gamma\gamma$ background also ϕ dependent
- same can be done in the $H \rightarrow ZZ^*$ channel

for $gg \rightarrow \text{box} \rightarrow \gamma\gamma$ see also
J. -W. Qiu, M. Schlegel and W. Vogelsang,
Phys. Rev. Lett. 107, 062001 (2011)
[arXiv:1103.3861 [hep-ph]]

CONCLUSIONS

- gluon polarization modifies both Higgs q_T and ϕ distribution
- q_T distribution modification different for positive/negative parity states
- ϕ distribution modification different for various spin-0 and spin-2 coupling scenarios

for more info see:
arXiv:1304.2654

SPIN STATUS

May 15, 2013

$0^+ \text{ vs } 2_m^+$	ATLAS	CMS
YY	99.3% CLs (2.7 σ)	-
WW*	94.7% CLs (1.9 σ)	86% CLs (1.5 σ)
ZZ*	83.4% CLs (1.4 σ)	98.5% CLs (2.4 σ)

PARITY STATUS

May 15, 2013

$0^+ \text{ vs } 0^-$	ATLAS	CMS
YY	-	-
WW*	-	-
ZZ*	99.6% CLs (2.9 σ)	99.84% CLs (3.2 σ)