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Generalized parton distributions of spin-0 nuclei
([hep-ph/0509158](#))

1. Motivation
2. D-term and its A -dependence
3. Evaluation of nuclear GPDs
4. Results for asymmetries

I. Motivation

- Generalized parton distributions (GPDs) became a standard tool for the parameterization of the nonperturbative hadronic structure in hard processes. The standard definition for spin-0 target is

$$\frac{1}{2} \int \frac{dz^-}{2\pi} \langle P' | \bar{\psi}(0) \gamma_+ \psi(z) | P \rangle e^{ix\bar{P}^+ z^-} = H(x, \xi, t)$$

- The theoretical study of GPDs was initiated in 1996 (Ji 1996, Radyushkin 1996)
- Experimental study - through the Deeply Virtual Compton Scattering (DVCS) and meson electroproduction. Experiments are being held by HERMES, H1, CLAS collaborations.
- Nuclear DVCS - sensitivity both to the nuclear forces and distortion of the nucleon in the nuclei.
- A first experiment on nuclear DVCS-measurement of DVCS asymmetries with Deuterium and Neon nuclei at HERMES (DESY). Another experiment is planned at the future Electron Ion Collider (EIC) (Deshpande 2002).

- Study of the forward limit (DIS)-shadowing, antishadowing, EMC-effect etc.
- DVCS cross-section-possibly new nuclear effects ?
- Current approach to the study of the nuclear DVCS- *sum* of the free nucleon GPDs (Kirchner, Mueller 2003, Freund *et. al.* 2003, Guzey, Strikman 2003).
- The assumption is *good but not universal* - "pathological" A -dependence $d_A(0) \propto A^{7/3}$ (M. Polyakov 2002).

II. $d_A(0)$ and its A -dependence

- The framework for our analysis - field-theoretical Walecka model. (Walecka, Serot 1984)

$$\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{m_V^2}{2}V_\mu V^\mu + \frac{1}{2}(\partial_\mu\phi\partial^\mu\phi - m_s^2\phi^2) \\ + \bar{\psi}(i\hat{\partial} - M - g_v\hat{V} + g_s\phi)\psi$$

- D -term -introduced to supplement double distribution parametrization (Polyakov, Weiss, 1999). Formal definition-through its moments:

$$d_n(t) = \frac{1}{(n+1)!} \frac{\partial}{\partial \xi^{n+1}} \int dx x^n H(x, \xi, t) \\ D(z) = (1-z^2) \sum_{n \text{ odd}} d_n(t) C_n^{3/2}(z)$$

- (Ji 1996): Connection of the GPD first moments with energy-momentum tensor form factors $M_A(t)$ and $d_A(t)$:

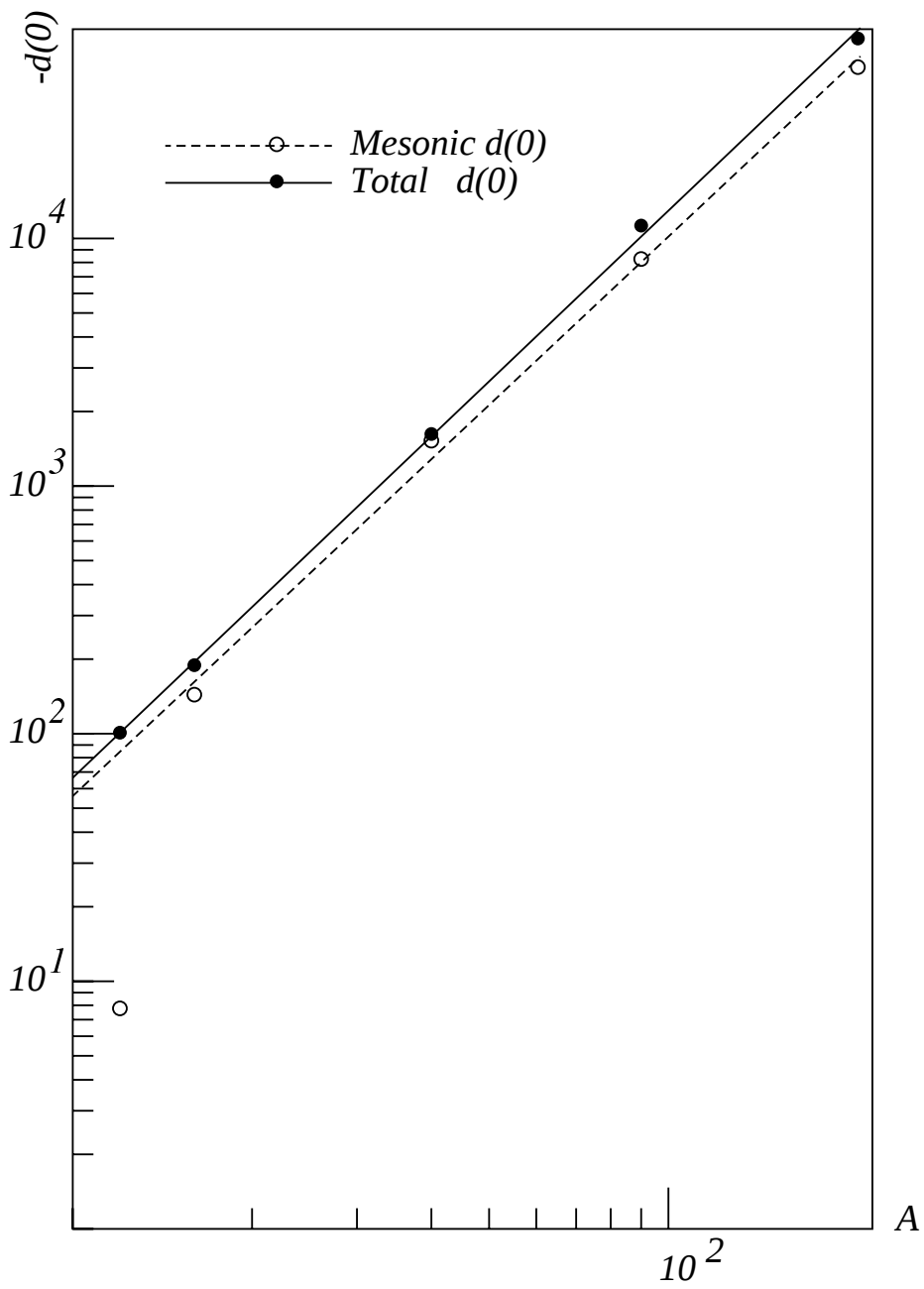
$$\langle P' | \hat{T}_{\mu\nu}(0) | P \rangle = M_A(t) \bar{P}_\mu \bar{P}_\nu + \frac{1}{5} d_A(t) (\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2)$$

$$d_A(0) \approx -0.3 A^{2.26}.$$

- Liquid drop model ([M. Polyakov 2002](#)):

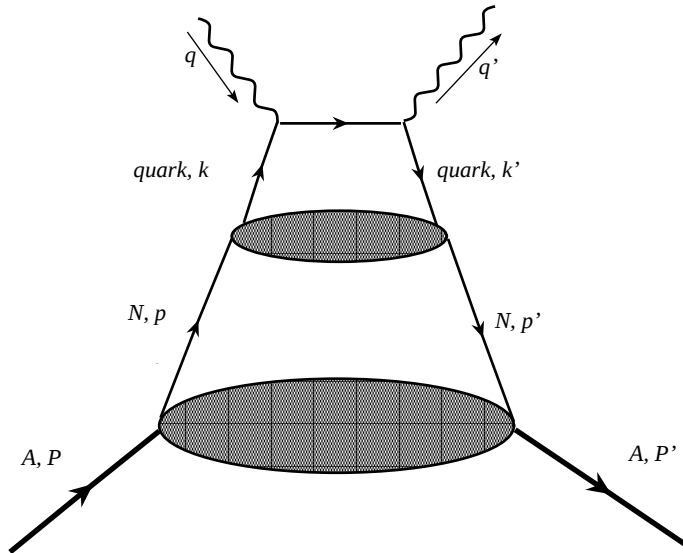
$$d_A(0) \approx -0.2 A^{7/3}.$$

- Dominant contribution from the mesons



III. Evaluation of nuclear GPDs

- The natural assumption in study of the nuclear hard processes-separation into the nucleonic and nuclear parts.

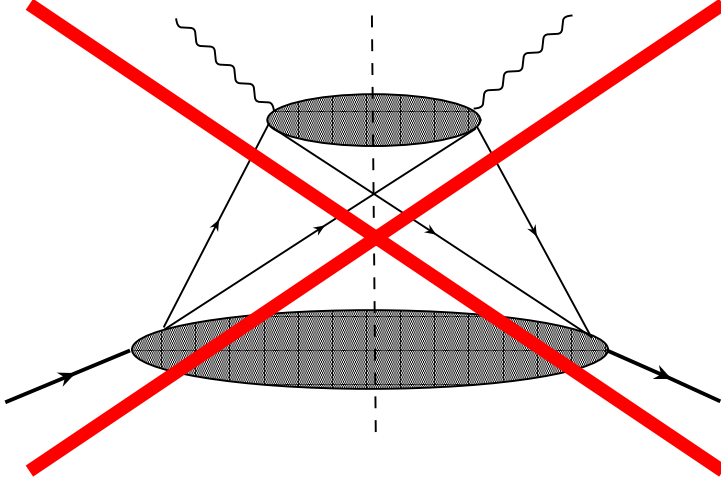


- Convolution formula

$$H_{q/A}(x, \xi, t) = \sum_i \int_x^1 \frac{dy}{y} H_{i/A}(y, \xi, t) H_{q/i} \left(\frac{x}{y}, \frac{\xi}{y}, t \right),$$

- Forward case-(Jaffe 1985, Berger 1983)

- The convolution approximation neglects the simultaneous coherent interaction of the virtual photon with several nuclear constituents. Inapplicable for $x < 0.1$.



- Definition of the nuclear parts $H_{i/A}$:

$$H_{N/A}(x, \xi, t) = \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P' | \bar{\psi} \left(\frac{z}{2} \right) e^{i \int_{-z/2}^{z/2} V(\lambda) \cdot d\lambda} \gamma_+ \psi \left(-\frac{z}{2} \right) | P \rangle,$$

$$H_{\phi/A}(x, \xi, t) = \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P' | \phi \left(\frac{z}{2} \right) i \overleftrightarrow{\partial}_+ \phi \left(-\frac{z}{2} \right) | P \rangle,$$

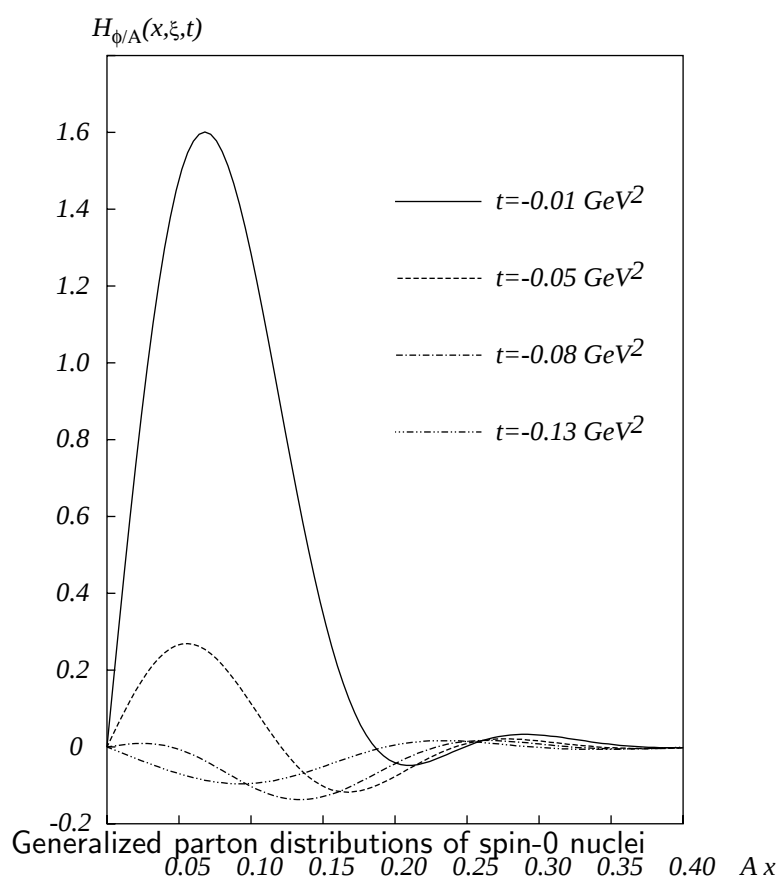
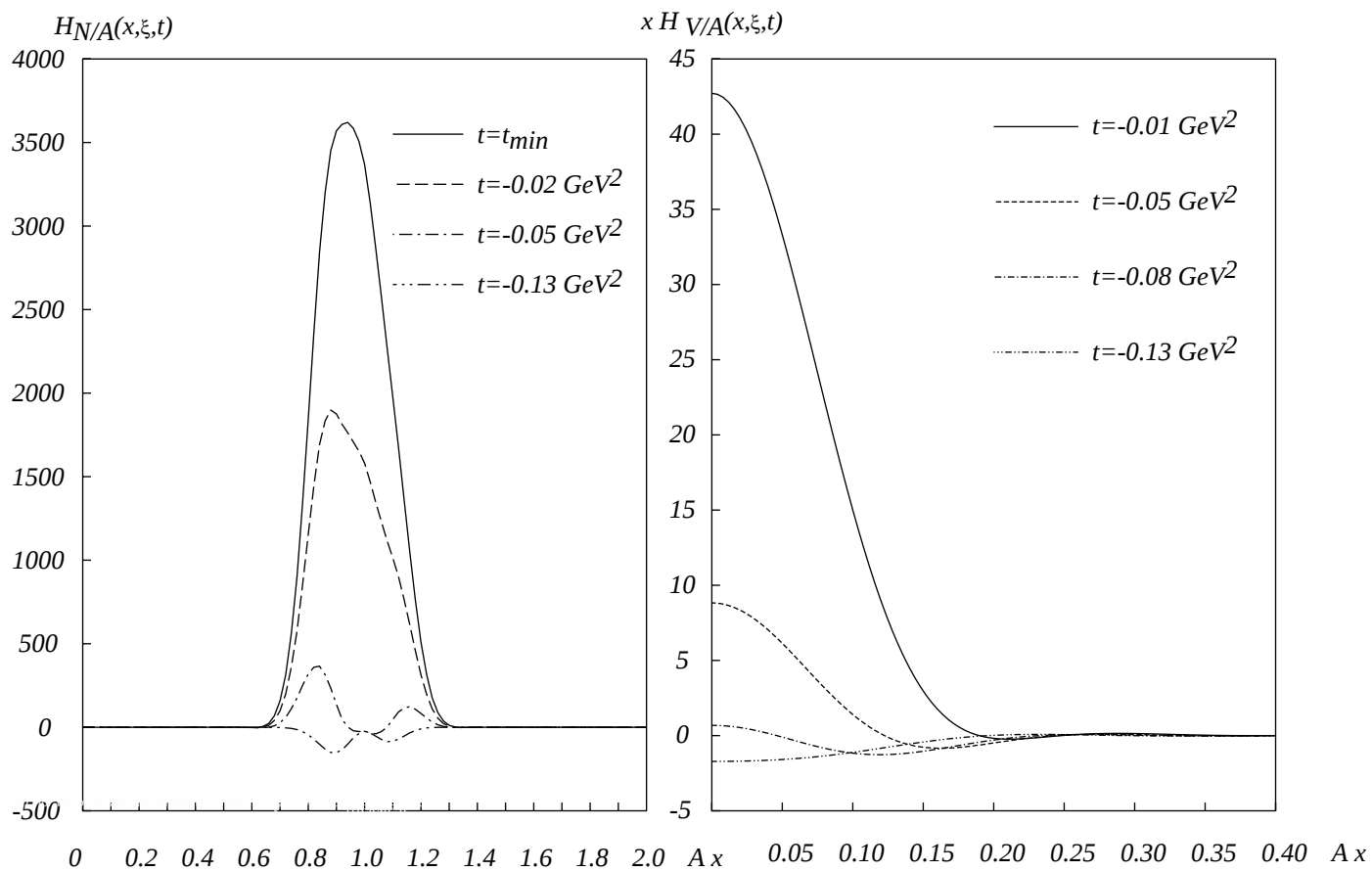
$$H_{V/A}(x, \xi, t) = \frac{1}{4x\bar{P}^+} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P' | V_{+\alpha} \left(\frac{z}{2} \right) V_+^\alpha \left(-\frac{z}{2} \right) | P \rangle$$

$$+ \frac{m_V^2}{4x\bar{P}^+} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P' | V_+ \left(\frac{z}{2} \right) V_+ \left(-\frac{z}{2} \right) | P \rangle.$$

- Final result:

$$\begin{aligned}
H_{N/A}(x, \xi, t) &= \frac{m_A}{2\pi} \int \frac{dz^-}{2\pi} e^{ix\bar{P}^+ z^-} \int d^3X \sum_n \bar{\Phi}_n \left(\frac{z}{2} - \vec{X} \right) \times \\
&\times P e^{i \int_{-z/2}^{z/2} V(\lambda) \cdot d\lambda} \gamma_+ \Phi_n \left(-\frac{z}{2} - \vec{X} \right), \\
H_{\phi/A}(x, \xi, t) &= \\
&\int \frac{d\bar{p}^+ d^2\bar{p}_\perp}{(2\pi)^3} \delta \left(x - \frac{\bar{p}^+}{\bar{P}^+} \right) \bar{p}^+ \phi \left((x - \xi), \bar{p}_\perp + \frac{\Delta_\perp}{2} \right) \phi \left((x + \xi), \bar{p}_\perp - \frac{\Delta_\perp}{2} \right), \\
H_{V/A}(x, \xi, t) &= \int \frac{d\bar{p}^+ d^2\bar{p}_\perp}{(2\pi)^3} \delta \left(x - \frac{\bar{p}^+}{\bar{P}^+} \right) \frac{\bar{p}_\perp^2 - \Delta_\perp^2/4 + m_V^2}{4x\bar{P}^+} \times \\
&\times V_+ \left((x - \xi), \bar{p}_\perp + \frac{\Delta_\perp}{2} \right) V_+ \left((x + \xi), \bar{p}_\perp - \frac{\Delta_\perp}{2} \right).
\end{aligned}$$

- We can see that similarly to the gluonic GPD, the vector off-forward distribution is singular at $x = 0$.



IV. Predictions for physical observables

- Model for the nucleon GPDs $H_{q/N}(x, \xi, t)$ (Radyushkin 2000; N. Kivel, M. V. Polyakov and M. Vanderhaeghen 2000)

$$\begin{aligned}
 H_N(x, \xi, t) &\equiv \sum_q e_q^2 H_{q/N} = \\
 &= F_N(t) \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(x - \beta - \alpha\xi) h(\beta, \alpha) q_N(\beta) + \theta\left(1 - \frac{x^2}{\xi^2}\right) D_N\left(\frac{x}{\xi}, t\right), \\
 h(\beta, \alpha) &= \frac{3}{4} \frac{(1 - |\beta|)^2 - \alpha^2}{(1 - |\beta|)^3}, \quad D_N(z, t) = -\sum_q e_q^2 / N_f d_1(t) (1 - z^2) C_1^{3/2}(z)
 \end{aligned}$$

CTEQ5L parameterization for nucleon PDFs.

- Models of meson GPDs $H_{q/mes}(x, \xi, t)$

$$\begin{aligned}
 H_V(x, \xi, t) &= H_\phi(x, \xi, t) = H_{mes}(x, \xi, t) \equiv \sum_q e_q^2 H_{q/mes}(x, \xi, t) \approx q_{mes}(x) \\
 q_{mes}(x) &= \frac{x^\alpha (1-x)^\beta}{B(\alpha+1, \beta)} \\
 \int_{-1}^1 \sum_q x dx H_{q/mes}(x, 0, 0) &= 1
 \end{aligned}$$

We have neglected possible ξ -dependence for the *meson* GPDs $H_{mes}(x, \xi, t)$ since in the kinematics of nuclear DVCS $\xi \ll 1$, $t \langle r_{mes}^2 \rangle \ll 1$, and give only small corrections compared to the forward case.

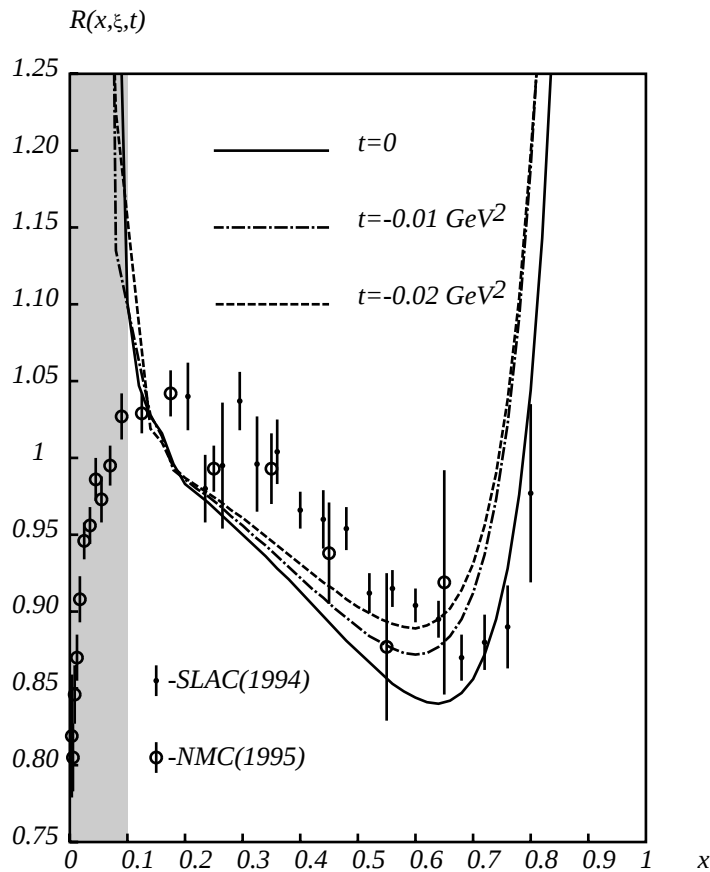
- Similar parametrization was used for description of the π -mesons (Owens 1984).

- Consider now the ratio

$$R(x, \xi, t) = \frac{\sum_q e_q^2 H_{q/A}(x_A, \xi, t)}{F_{N/A}(t) H_N(x, \xi, t)},$$

$$R(x, 0, 0) \approx R(x) \equiv \frac{F_2^A(x_A)}{A F_2^N(x)},$$

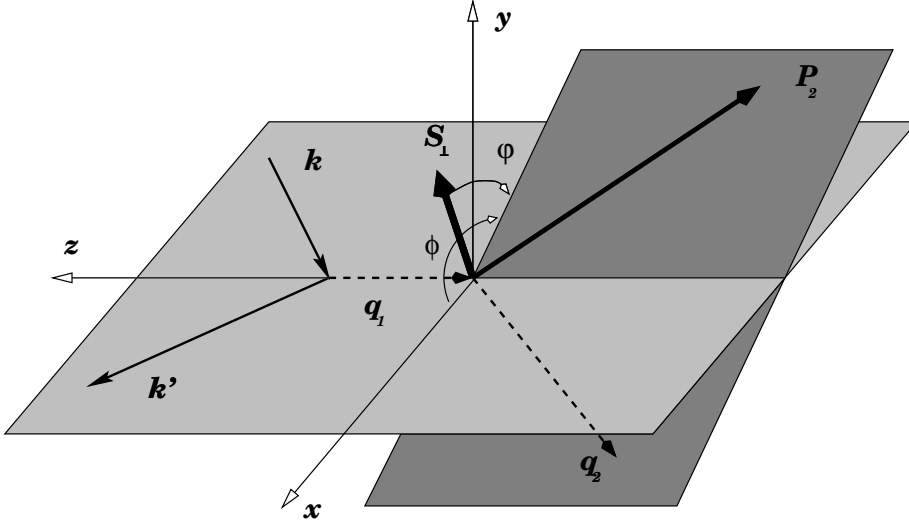
(the last equality is valid to the leading order in α_S)



Data for the ratio $R(x)$ are from the SLAC ([Gomez et.al., 1993](#)) and NMC ([Amaudruz et. al., 1995](#)).

- Beam-charge and beam-spin asymmetries:

$$A_C(\phi) = \frac{\sigma^+(\phi) - \sigma^-(\phi)}{\sigma^+(\phi) + \sigma^-(\phi)}, \quad A_{LU}(\phi) = \frac{\overrightarrow{\sigma}(\phi) - \overleftarrow{\sigma}(\phi)}{\overrightarrow{\sigma}(\phi) + \overleftarrow{\sigma}(\phi)},$$



$\sigma^\pm$ and $\overrightarrow{\sigma}, \overleftarrow{\sigma}$ -cross-sections of unpolarized electron/positron and longitudinally polarized leptons, respectively ([Belitsky 2001](#)).

- Choice of the kinematics-HERMES on Neon ([Ellinghaus 2002](#)): $\langle x_{Bj} \rangle_{per\ nucleon} = 0.09, \langle Q^2 \rangle = 2.2\ GeV^2, \langle t \rangle = -0.01\ GeV^2$.

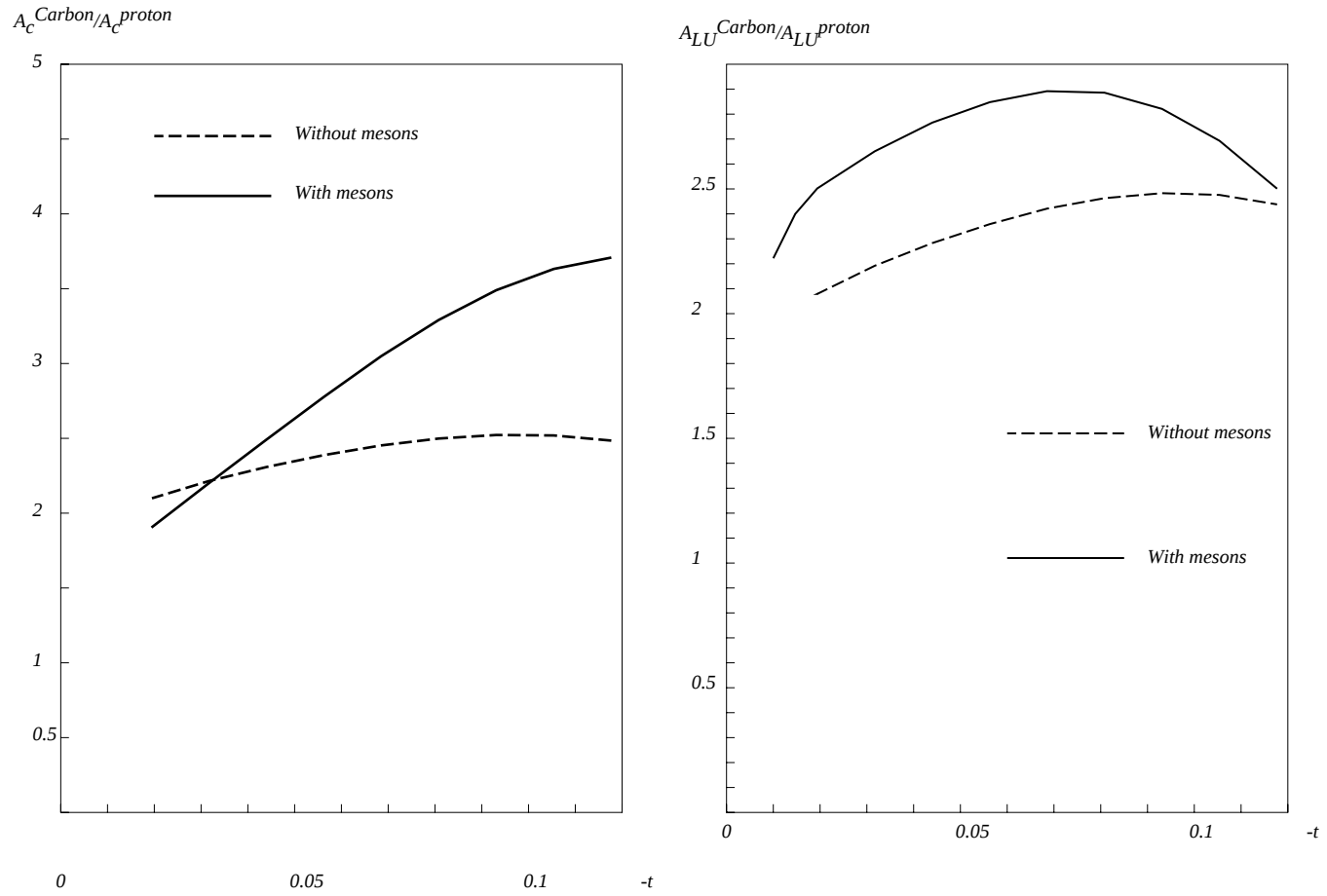
$$A_C^{cos} = \frac{1}{\pi} \int_0^{2\pi} d\phi \cos \phi A_C(\phi); \quad A_{LU}^{sin} = \frac{1}{\pi} \int_0^{2\pi} d\phi \sin \phi A_{LU}(\phi).$$

- Sensitivity to mesons of the values A_C^{cos}, A_{LU}^{sin} .

Nucleus	$A_C^{cos} A / A_C^{cos} N$	$A_{LU}^{sin} A / A_{LU}^{sin} N$	$A_C^{cos} A / A_C^{cos} N$	$A_{LU}^{sin} A / A_{LU}^{sin} N$
^{12}C	2.45	1.85	1.573	2.222
^{16}O	2.43	1.83	1.905	2.270
^{40}Ca	2.38	1.89	3.276	2.180
^{90}Zr	2.59	1.93	4.879	2.104

Table 1: The ratios of the nuclear to the free proton asymmetries for different nuclei. The second and third columns correspond to the calculation without the nuclear mesons; the fourth and fifth columns correspond to the full calculation including the meson contribution.

- A least-square fit gives the following approximate A -dependence: $A_C^{cos} A / A_C^{cos} N \propto A^{0.5}$; $A_{LU}^{sin} A / A_{LU}^{sin} N \propto A^{-0.03}$ for all A ; the ratio of the DVCS amplitudes squared $|A_{DVCS} A / A_{DVCS} N|^2 \propto A^{4.29}$.



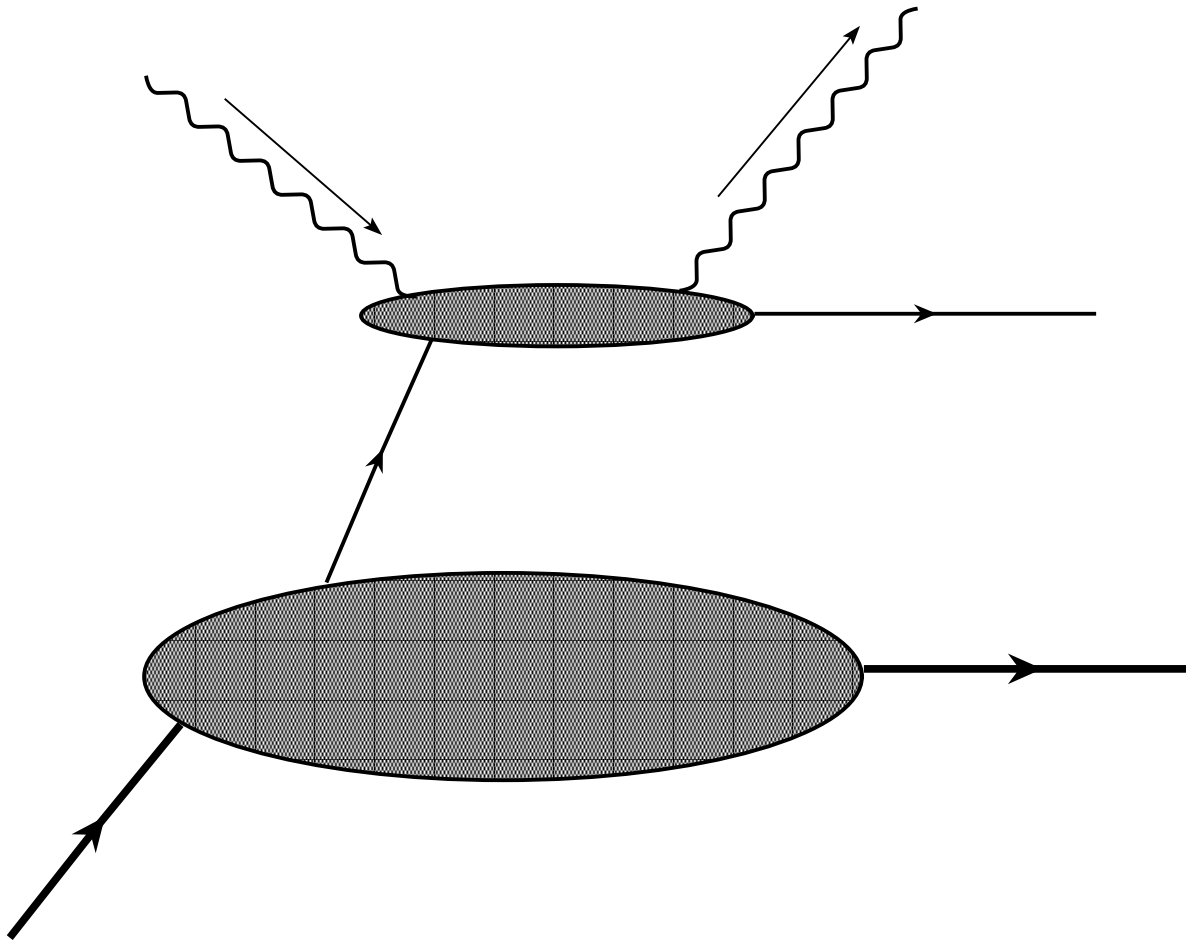
- Comparison with experimental data for Neon ($A = 20$)

$$\left(\frac{A_{LU}^{sin} A}{A_{LU}^{sin} N} \right)_{exp} = 1.22 \pm 0.26 ,$$

Interpolation of our results gives

$$\left(\frac{A_{LU}^{sin} A}{A_{LU}^{sin} N} \right)_{th} \approx 2.1 \pm 0.2 .$$

- One of the possible explanations of the discrepancy-contribution of incoherent nuclear scattering (with nucleus break-up) (V. Guzey and M. Strikman, 2003) (Ratio = 1 for both asymmetries).



V. Summary

- A microscopic evaluation of nuclear GPDs (for spin-0 nuclei).
- Meson (non-nucleonic) degrees of freedom might be not negligible.
- We studied the A and t -dependence of the beam-charge and beam-spin DVCS asymmetries.