

# Structure Functions

From HERA to LHC

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Workshop on Hard Processes  
Graduiertenkolleg

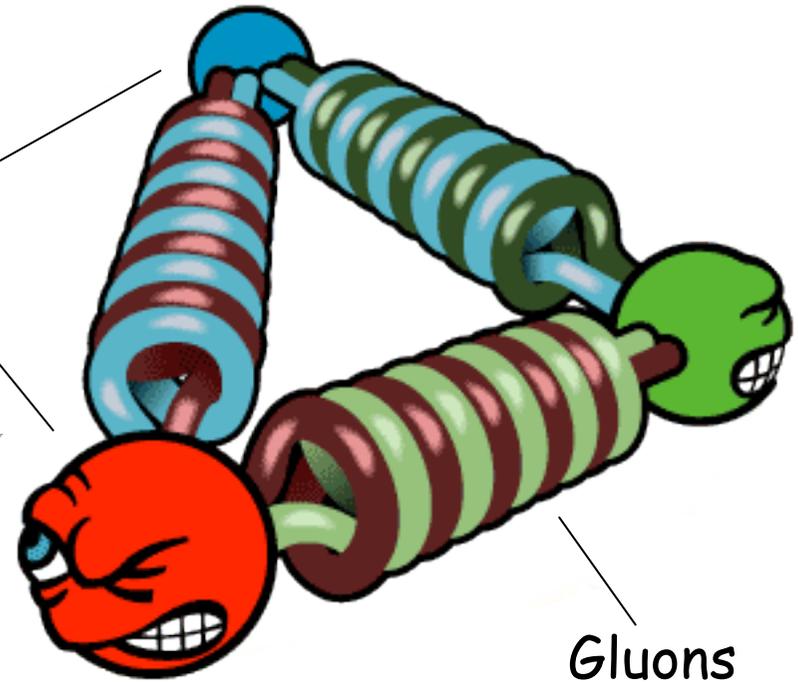
Dortmund, October 13<sup>th</sup>, 2005

# Nobelprize 2004



D.J. Gross, H.D. Politzer & F. Wilczek

Coloured Quarks

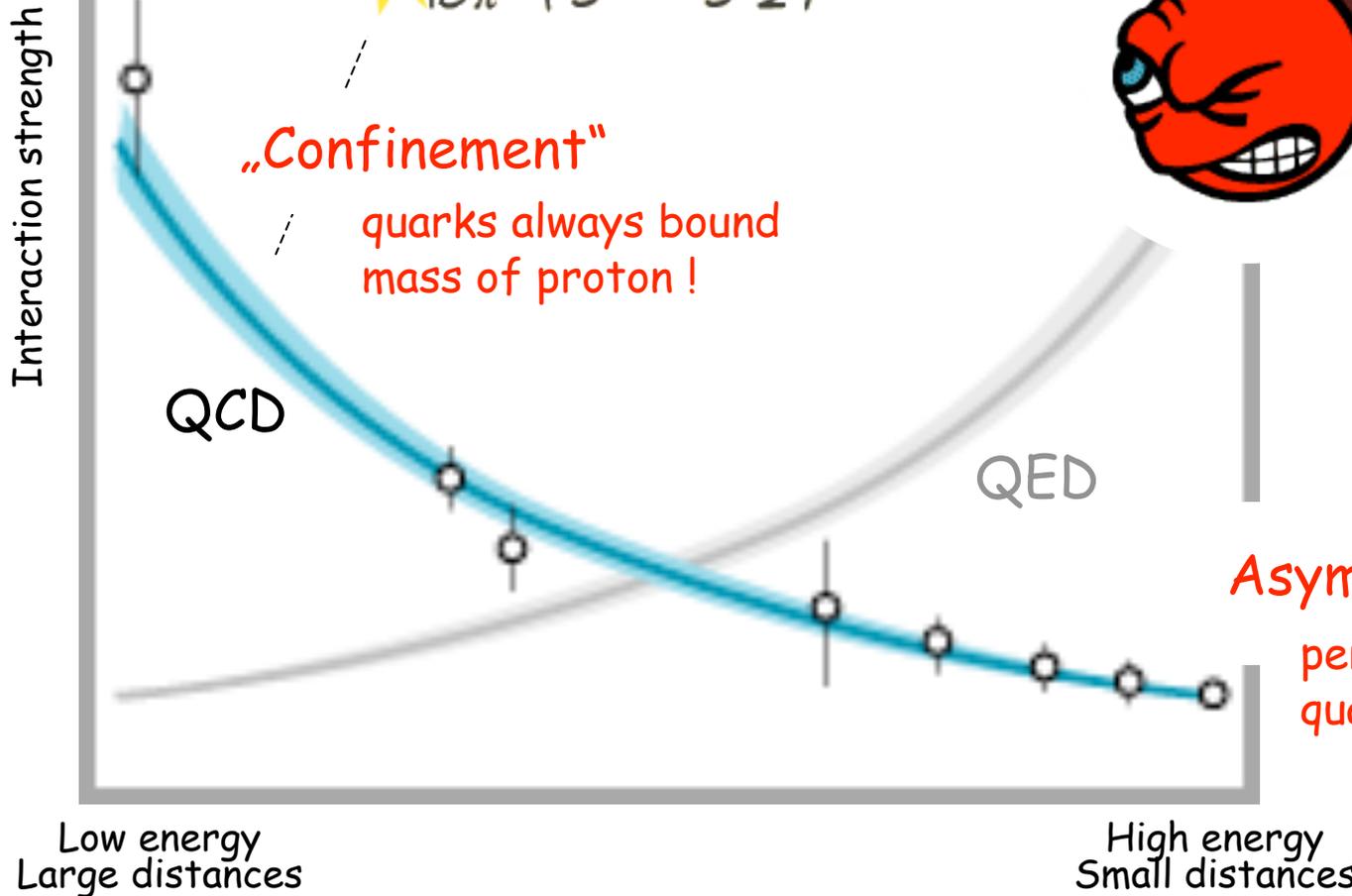


Gluons

$$\beta(g) = -\frac{g^3}{16\pi^2} \left( \frac{11}{3} N_C - \frac{4}{3} \frac{N_F}{2} \right)$$

„Confinement“

quarks always bound  
mass of proton !



Asymptotic freedom

perturbative QCD  
quasi-free partons

We know: QCD is the theory of the strong interactions !

# Why then QCD at HERA ?

and elsewhere ... ?

Because:

- ... the strong coupling  $\alpha_s$  is the least well known of the coupling constants
- ... we do not understand how partons are put together to make hadrons
- ... we need to understand future high energy experiments at the LHC
- ...

# QCD @ HERA ...

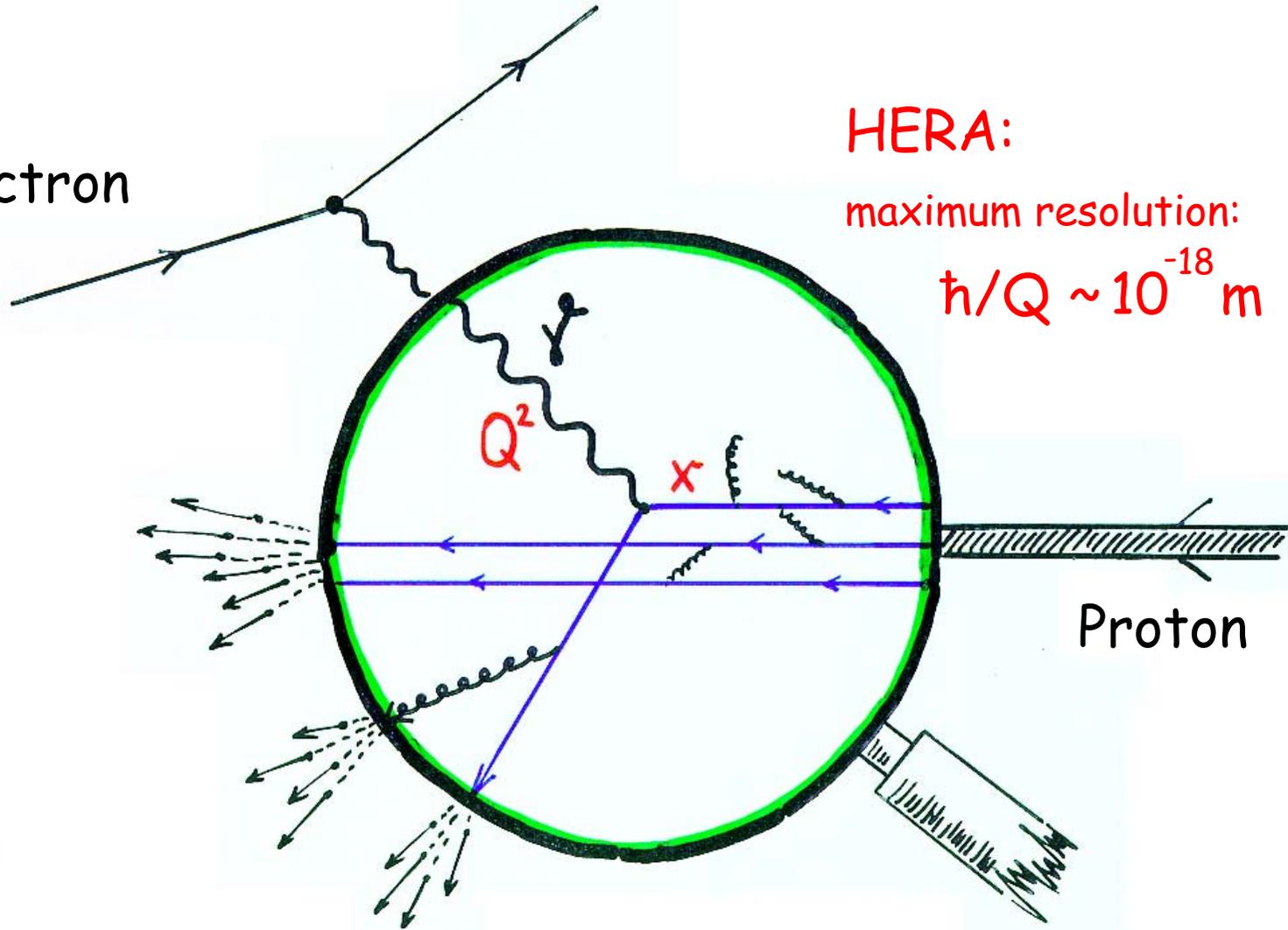
Today!

- **proton structure  $F_2$**   
quark- & gluon-PDFs ( $\rightarrow$  LHC),  $\Delta\alpha_s/\alpha_s \sim 1\%$  (NNLO)  
 $F_2$  at small  $Q^2$ ,  $x \rightarrow$  non-perturbative QCD  
 $xF_3$ , PDFs at large  $x$  (HERA II !) ...
- **heavy quarks**  
universality of proton structure (gluon-PDF!)  
fragmentation, production mechanisms,  $c/b$ -PDFs ...
- **diffraction and low- $x$  physics**  
QCD dynamics at high parton densities ...  
structure of diffractive interactions, factorization  
DVCS  $\rightarrow$  parton-parton correlations (GPDs)
- **jet physics**  
universality of proton structure (gluon-PDF!)  
parton dynamics, measurement of  $\alpha_s$
- **spectroscopy**  
pentaquarks ...

# Structure Functions

## Basics

Electron



HERA:

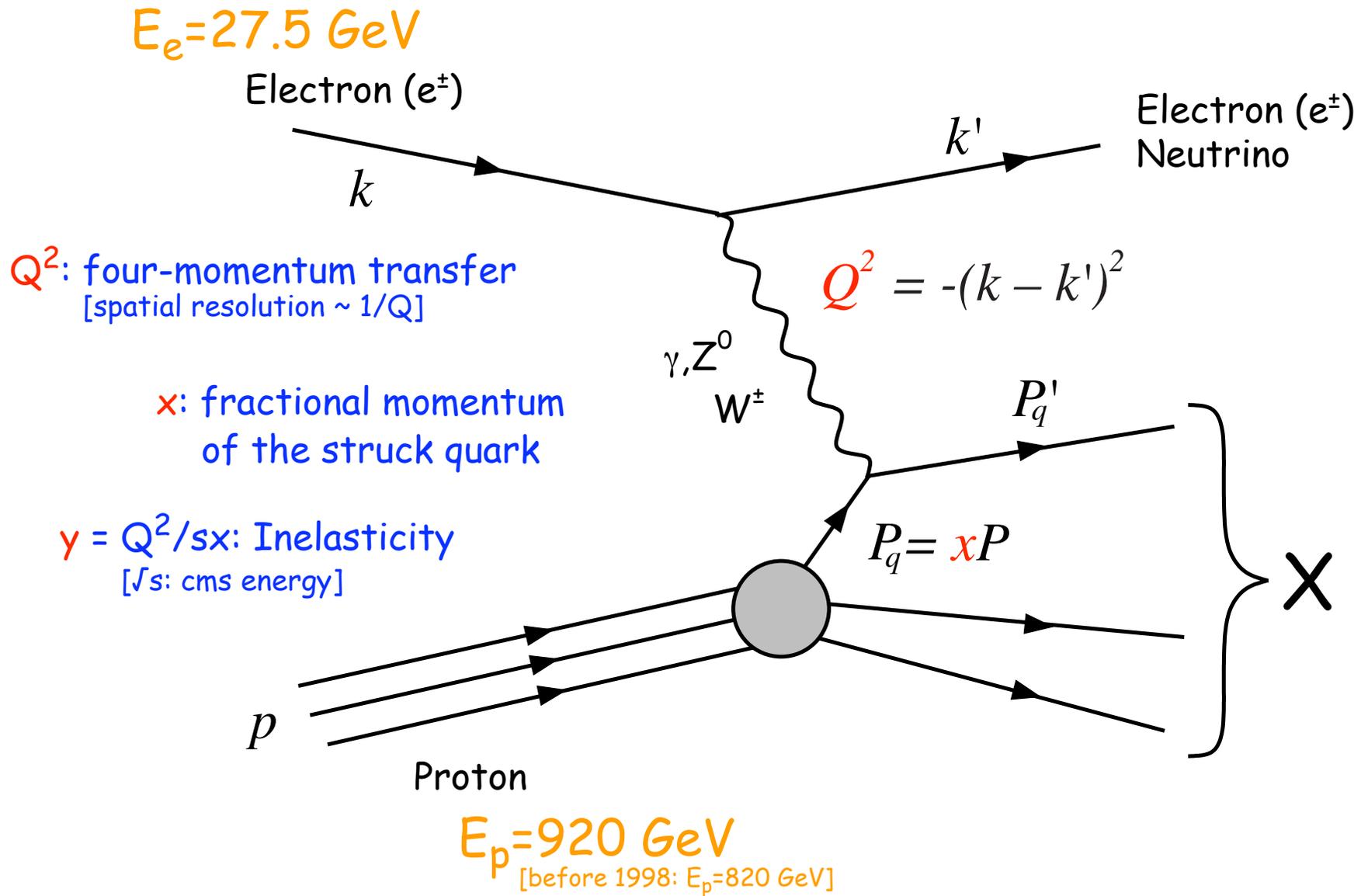
maximum resolution:

$$\hbar/Q \sim 10^{-18} \text{ m}$$

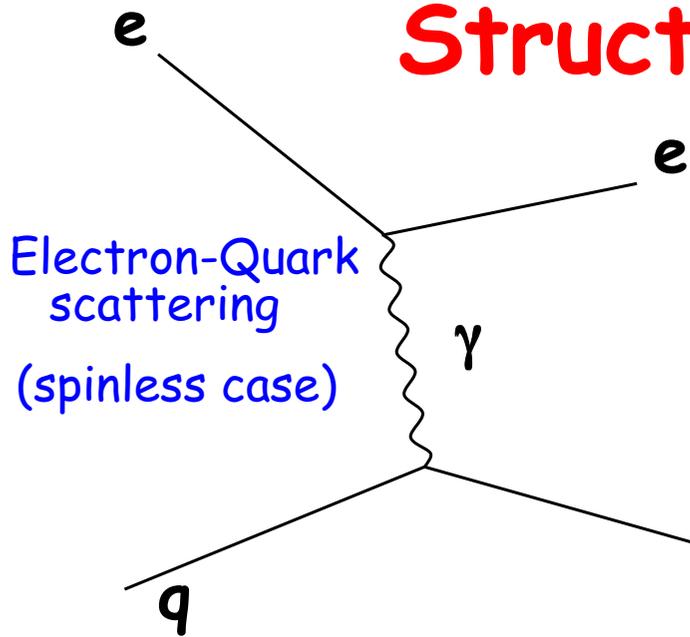
Proton

Ideal QCD laboratory

# HERA Kinematics

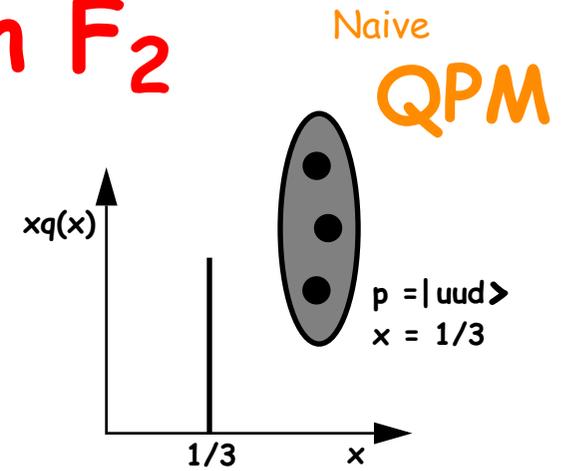


# Structure Function $F_2$



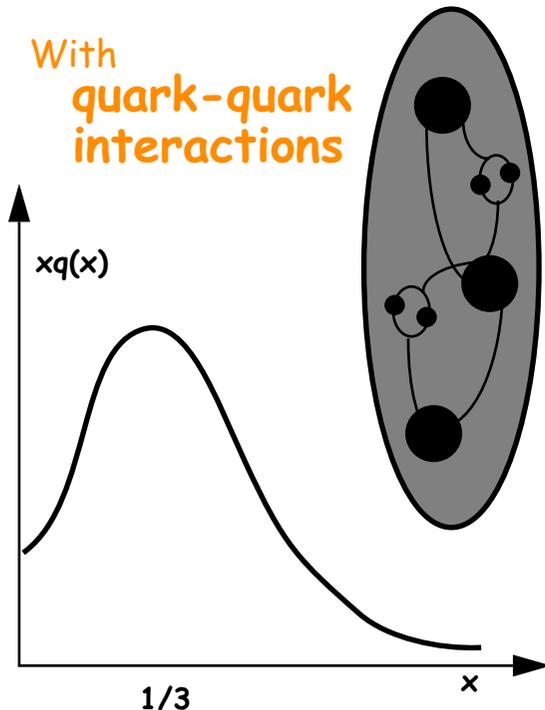
$$\frac{d\sigma(eq)}{dq^2} = \frac{4\pi\alpha^2}{q^4} e_q^2$$

Rutherford scattering  
on pointlike target



$$\frac{d\sigma(ep)}{dq^2} = \frac{4\pi\alpha^2}{q^4} [2e_u^2 + e_d^2] = \frac{4\pi\alpha^2}{q^4}$$

With quark-quark interactions



$$\frac{d\sigma(ep)}{dx dq^2} = \frac{4\pi\alpha^2}{q^4} [e_u^2 u(x) + e_d^2 d(x) + \dots]$$

$$= \frac{4\pi\alpha^2}{q^4} \frac{F_2(x)}{x}$$

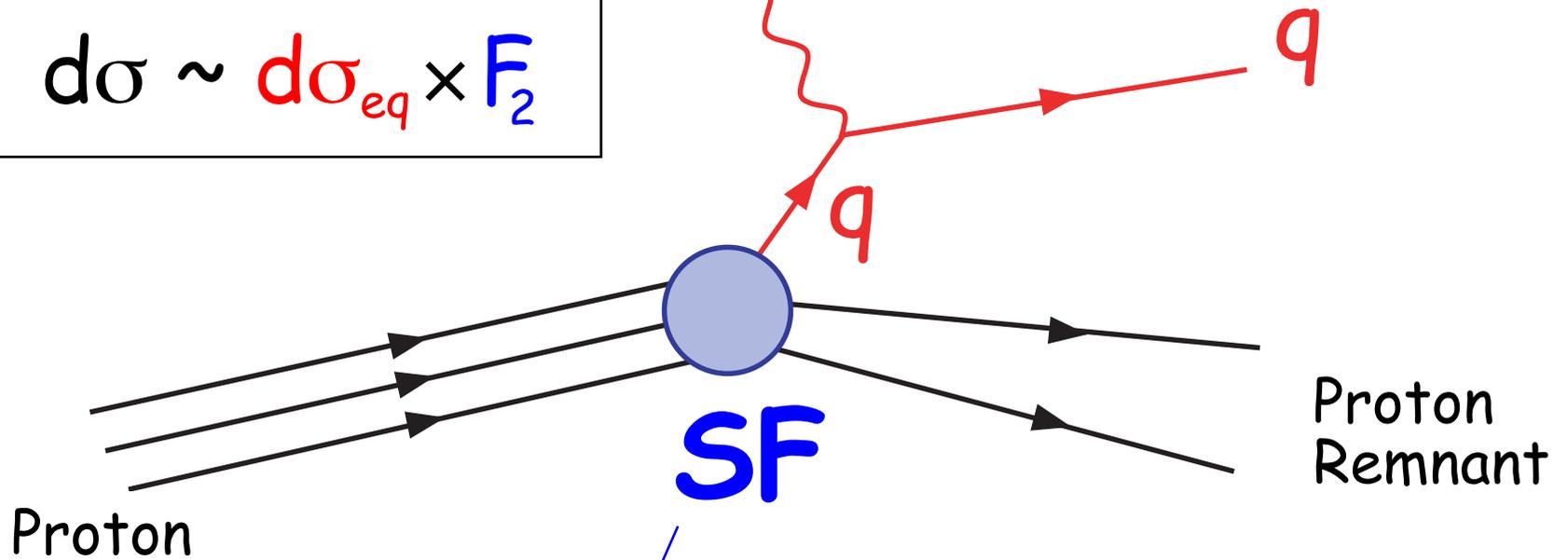
QPM: Structure Function  $F_2$  independent of  $Q^2$

Electron ( $e^\pm$ )

Electron ( $e^\pm$ )

Cross Section:

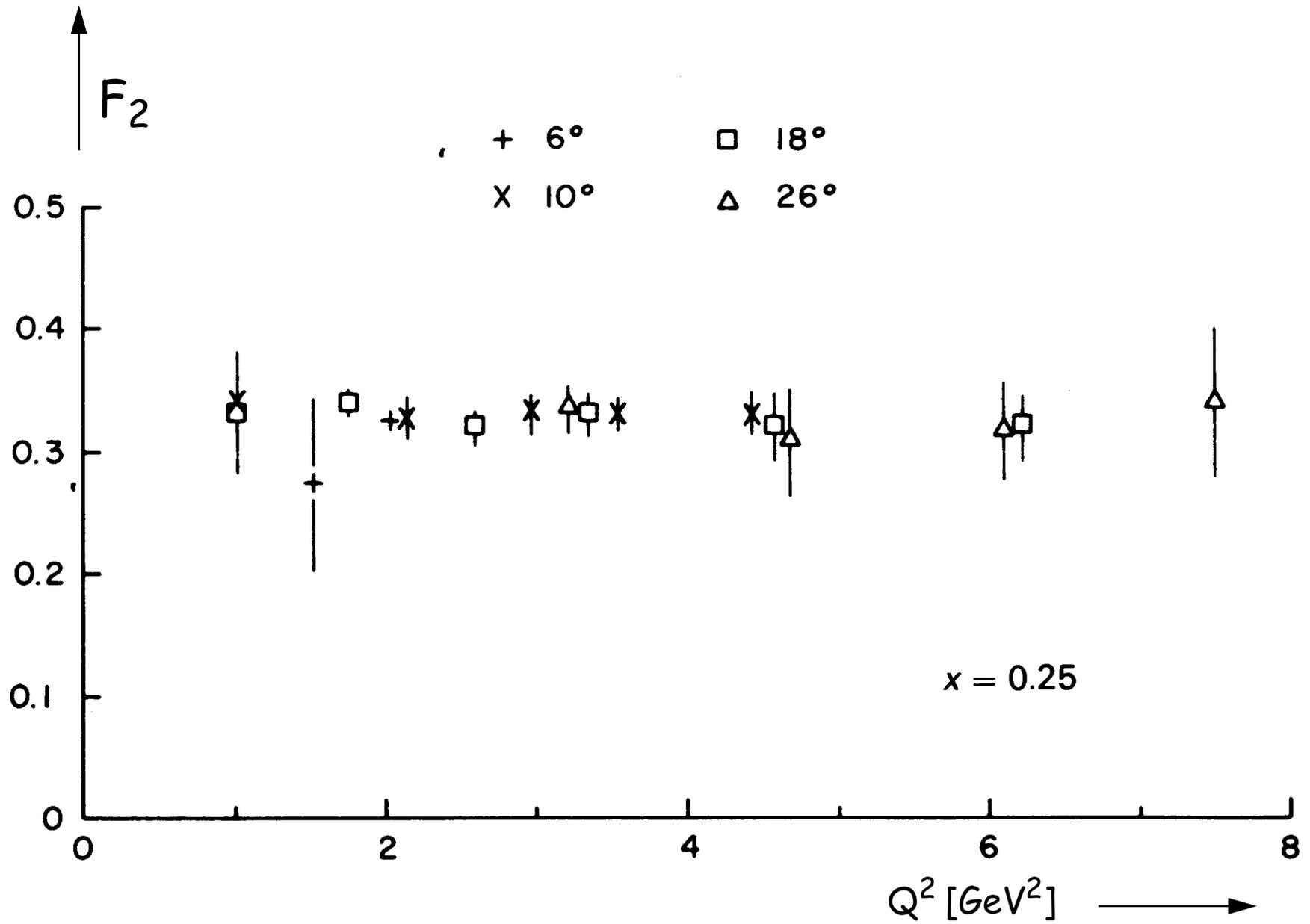
$$d\sigma \sim d\sigma_{eq} \times F_2$$



$$F_2 = \sum e_q^2 xq(x)$$

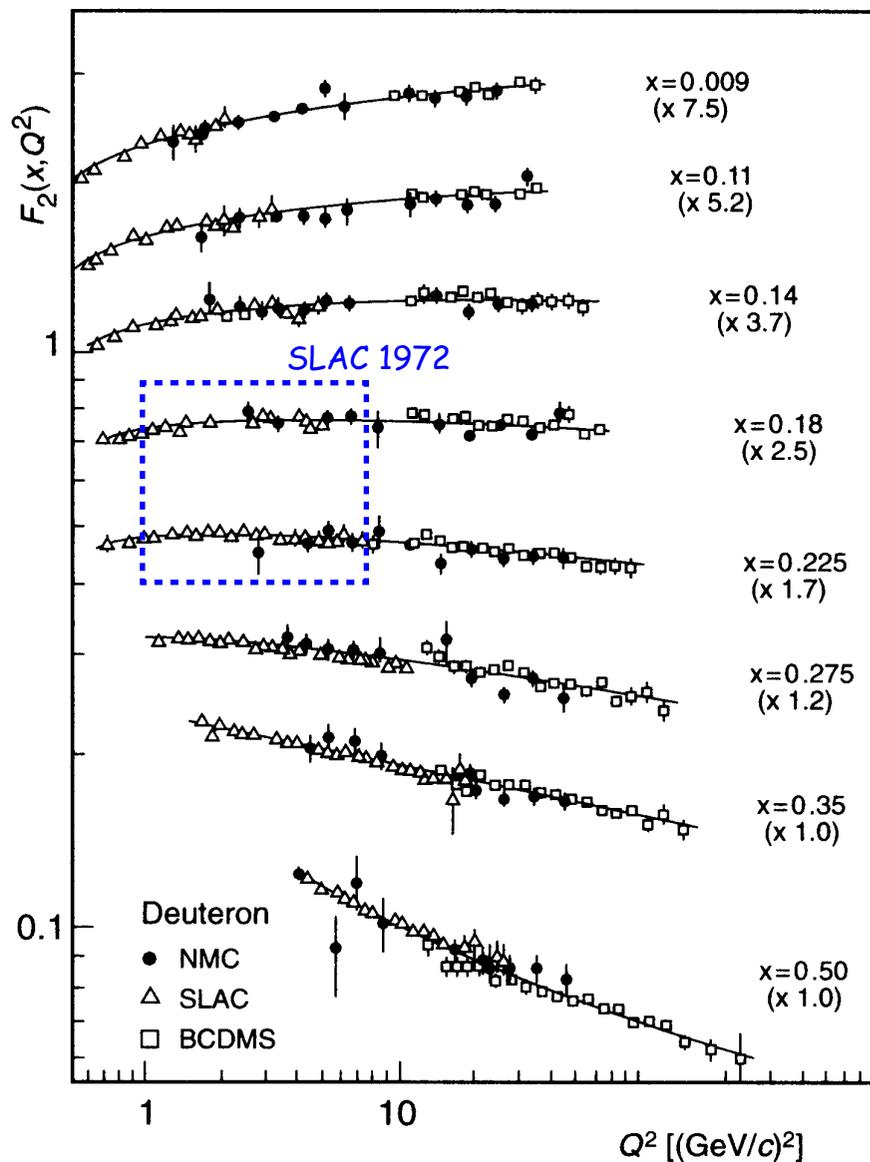
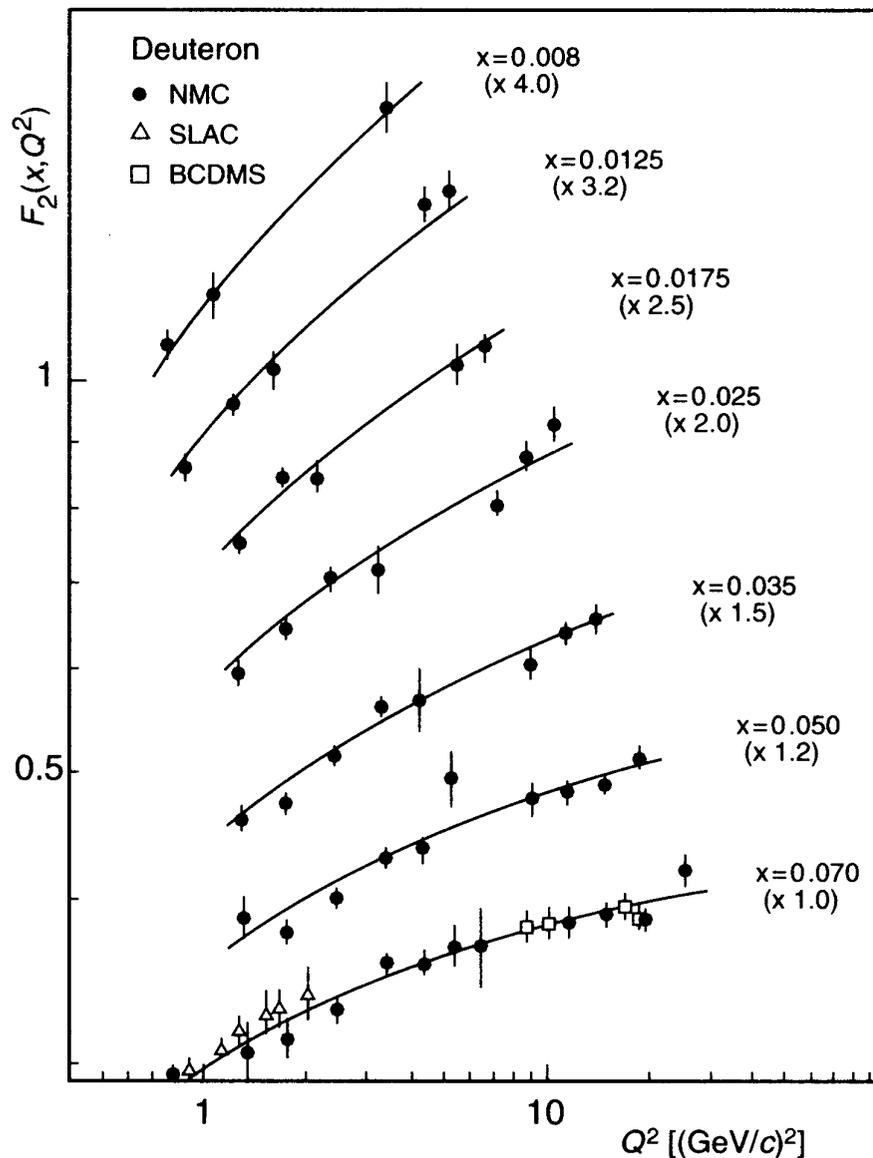
- describes structure of proton
- probability to find quark with momentum fraction  $x$
- QPM: independent of  $Q^2$ . Correct?

# Scaling [SLAC 1972]



# Scaling Violations [1990++]

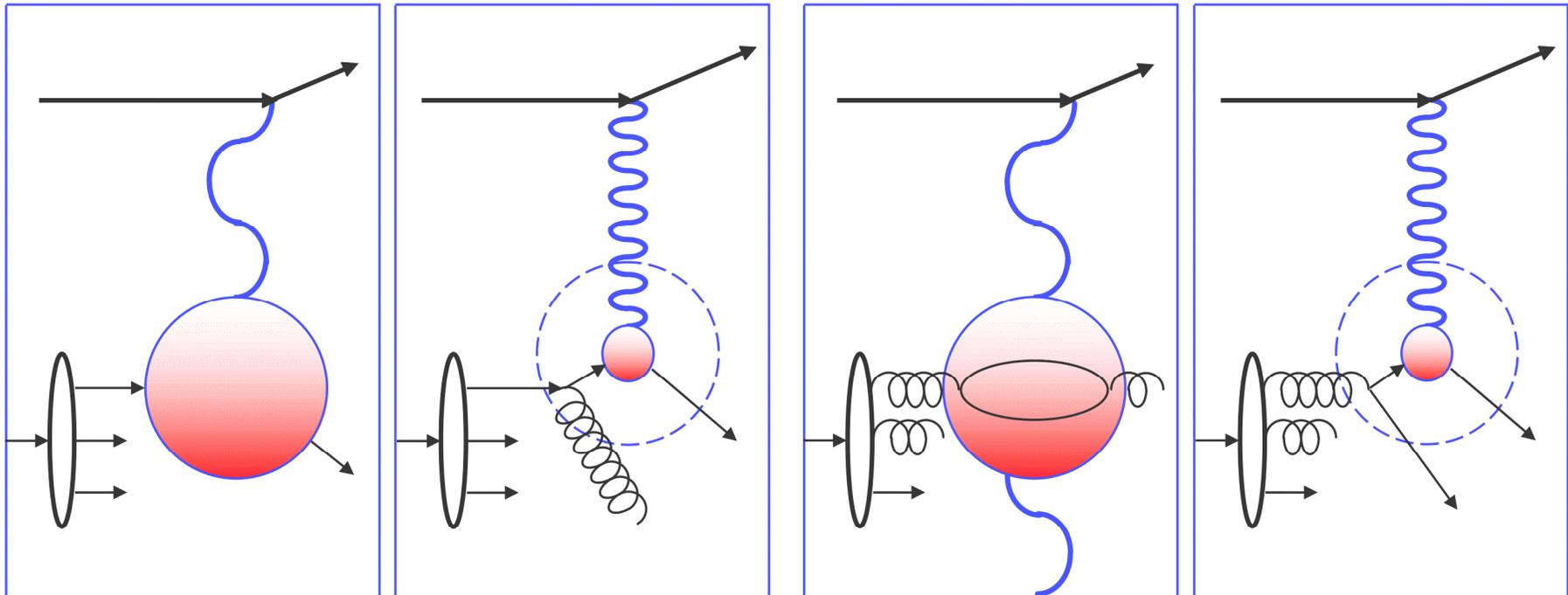
$$F_2(x, Q^2) = \sum e_q^2 x q(x, Q^2)$$



# The QCD Picture of Scaling Violation

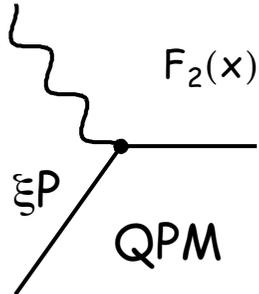
- Proton quark dominated:  
 $Q^2 \uparrow \Rightarrow F_2 \downarrow$  for fixed  $x$

- Proton gluon dominated:  
 $Q^2 \uparrow \Rightarrow F_2 \uparrow$  for fixed  $x$

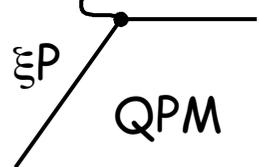


$Q^2$ -evolution described by DGLAP equations

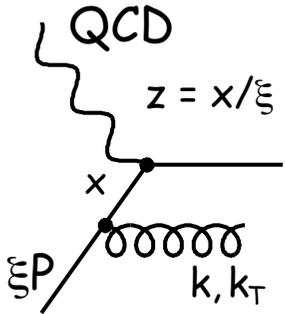
# QCD Improved Parton Model



$$F_2(x) = x \sum_q \int_0^1 e_q^2 d\xi q(\xi) \delta(x - \xi) = x \sum_q e_q^2 q(x)$$



$$F_2(x) = x \sum_q e_q^2 \int_x^1 \frac{d\xi}{\xi} q(\xi) \left[ \delta\left(1 - \frac{x}{\xi}\right) + \frac{\alpha_s}{2\pi} P_{qq}\left(\frac{x}{\xi}\right) \log \frac{Q^2}{\mu_0^2} \right]$$



$\mu_0$ : cutoff parameter

$$\sigma_{\gamma^* q \rightarrow qg} \sim \frac{\alpha_s}{2\pi} P_{qq}(z) \int_{\mu_0^2}^{Q^2} \frac{dk_T^2}{k_T^2}$$

$$\sim \frac{\alpha_s}{2\pi} P_{qq}(z) \log \frac{Q^2}{\mu_0^2}$$

Splitting function:

Probability to find quark with momentum fraction  $z$  of a parent quark having emitted a gluon with momentum  $(1-z)$



$$q(x, Q^2) = q(x) + \frac{\alpha_s}{2\pi} \log \frac{Q^2}{\mu_0^2} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z) \quad (A)$$

$$q(x, \mu^2) = q(x) + \frac{\alpha_s}{2\pi} \log \frac{\mu^2}{\mu_0^2} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z) \quad (B)$$

(A)-(B)

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$$q(x, Q^2) = q(x, \mu^2) + \frac{\alpha_s}{2\pi} \log \frac{Q^2}{\mu^2} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z)$$

# DGLAP Equations

DGLAP: Dokshitzer, Gribov, Lipatov, Altarelli, Parisi

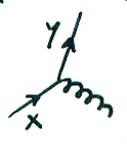
DGLAP evolution equations arise from requirement that  $q(x, Q^2)$  should not depend on the choice of scale  $\mu$ :

$$\left. \begin{aligned} q(x, Q^2) &= q(x, \mu^2) + \frac{\alpha_s}{2\pi} \log \frac{Q^2}{\mu^2} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z) \\ \& \frac{dq(x, Q^2)}{d \log \mu^2} &= \frac{dq(x, \mu^2)}{d \log \mu^2} - \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z) \stackrel{!}{=} 0 \end{aligned} \right\} \frac{dq(x, \mu^2)}{d \log \mu^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} P_{qq}(z) q(x/z, \mu^2)$$

From iteration

$$\frac{\partial}{\partial \log Q^2} \begin{bmatrix} q(x, Q^2) \\ g(x, Q^2) \end{bmatrix} = \frac{\alpha_s}{2\pi} \begin{bmatrix} P_{q/q} & P_{q/g} \\ P_{g/q} & P_{g/g} \end{bmatrix} \otimes \begin{bmatrix} q(x, Q^2) \\ g(x, Q^2) \end{bmatrix}$$

PDFs

$\frac{4}{3} \left[ \frac{1+z^2}{1-z} \right]$ 

 $P_{q/q}$

$\frac{1}{2} [z^2 + (1-z)^2]$ 

 $P_{q/g}$

$\frac{4}{3} \left[ \frac{1+(1-z)^2}{z} \right]$ 

 $P_{g/q}$

$6 \left[ \frac{z}{1-z} + \frac{1-z}{z} + z(1-z) \right]$ 

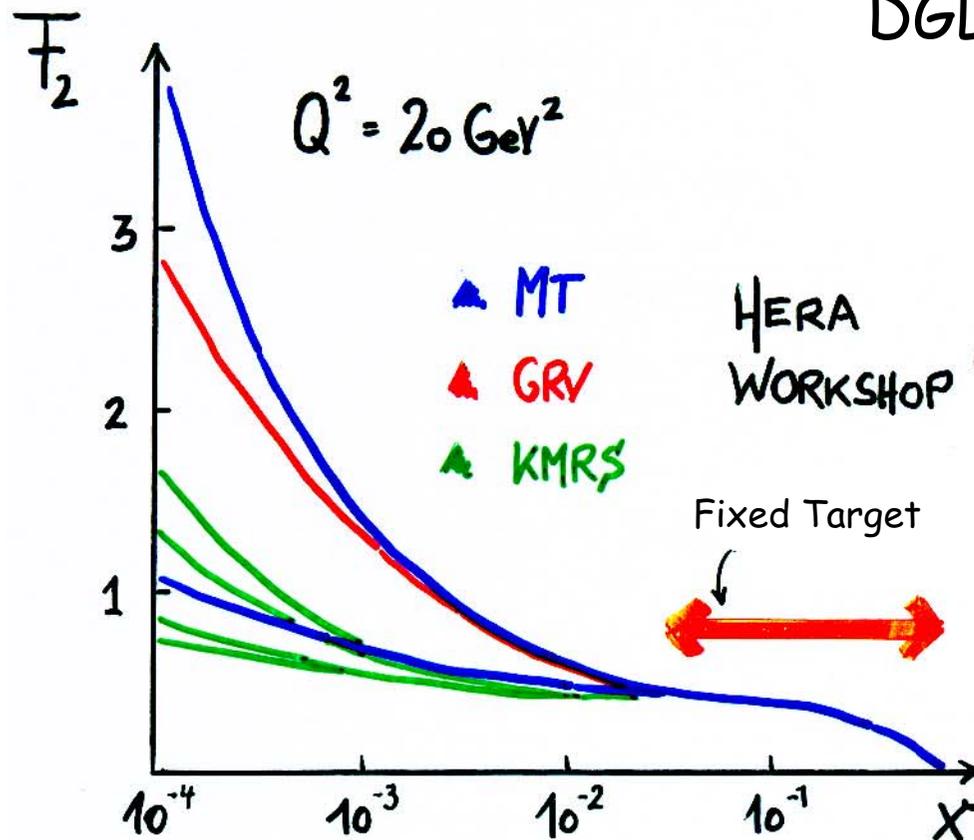
 $P_{g/g}$

$P \otimes f(x, Q^2) = \int_x^1 \frac{dy}{y} P(x/y) f(y, Q^2)$

# F<sub>2</sub> at Low Bjorken-x

[Pre-HERA Knowledge]

$$\frac{\partial}{\partial \log Q^2} \begin{pmatrix} q \\ g \end{pmatrix} = \frac{\alpha_s}{2\pi} \begin{bmatrix} P_{qq} & P_{qg} \\ P_{gq} & P_{gg} \end{bmatrix} \otimes \begin{pmatrix} q \\ g \end{pmatrix}$$



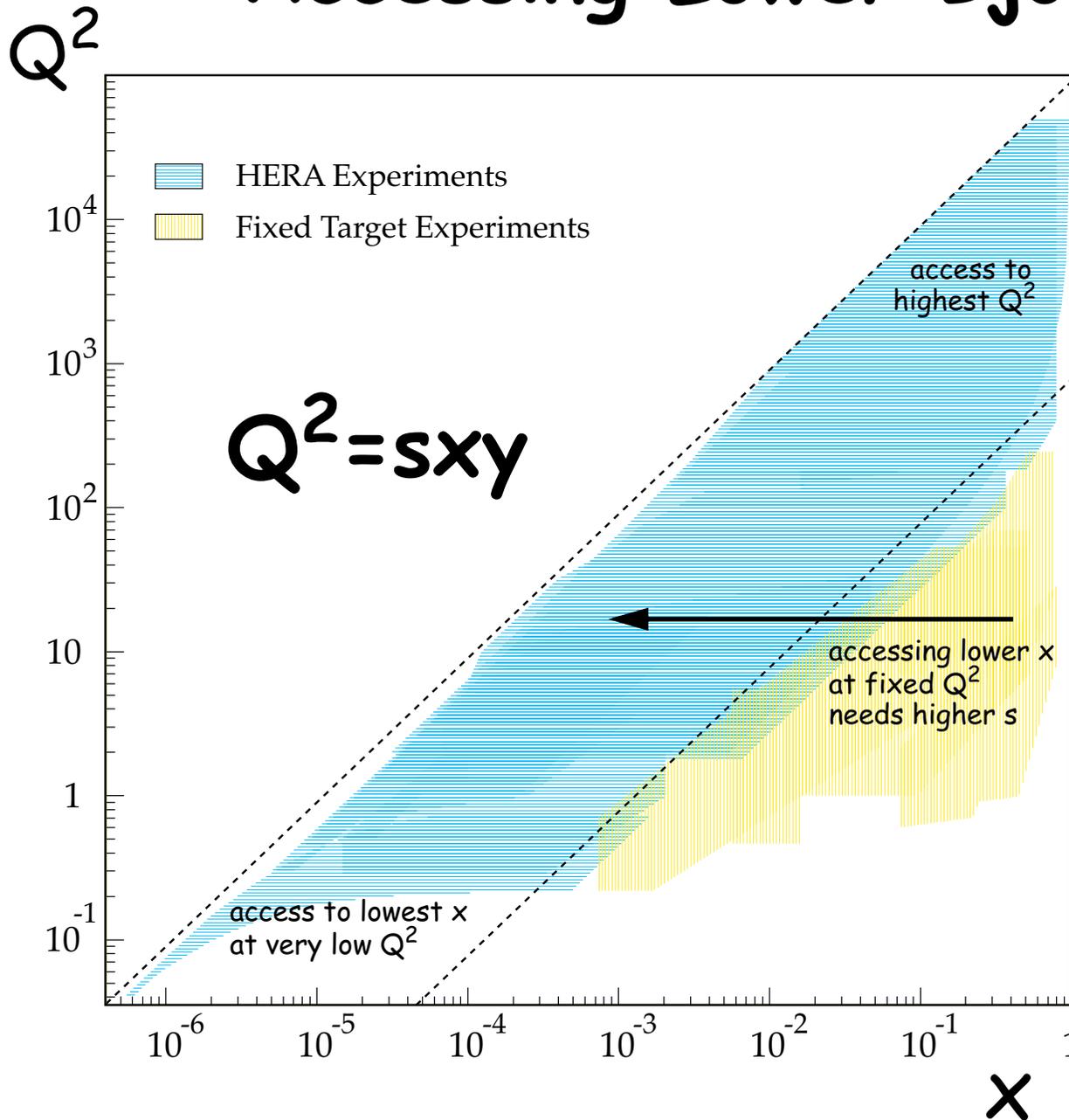
DGLAP: No prediction for the x-dependence of F<sub>2</sub>

[except asymptotic behaviour]

A. De Rujula et.al. 1974

**Measure !!**

# Accessing Lower Bjorken-x



$y = 1$   
[HERA:  $s \sim 10^5 \text{ GeV}^2$ ]

$y = 1$   
[Fixed Target:  $s < 10^3 \text{ GeV}^2$ ]

Fixed Target:

→ ●

$$s = 2M_p E_e$$

$$s = 10^5 \text{ GeV}$$

$$\Rightarrow E_e = 50 \text{ TeV}$$

ep-Collider:

→ ←

$$s = 4E_p E_e$$

$$E_e = 30 \text{ GeV}$$

$$E_p = 900 \text{ GeV}$$

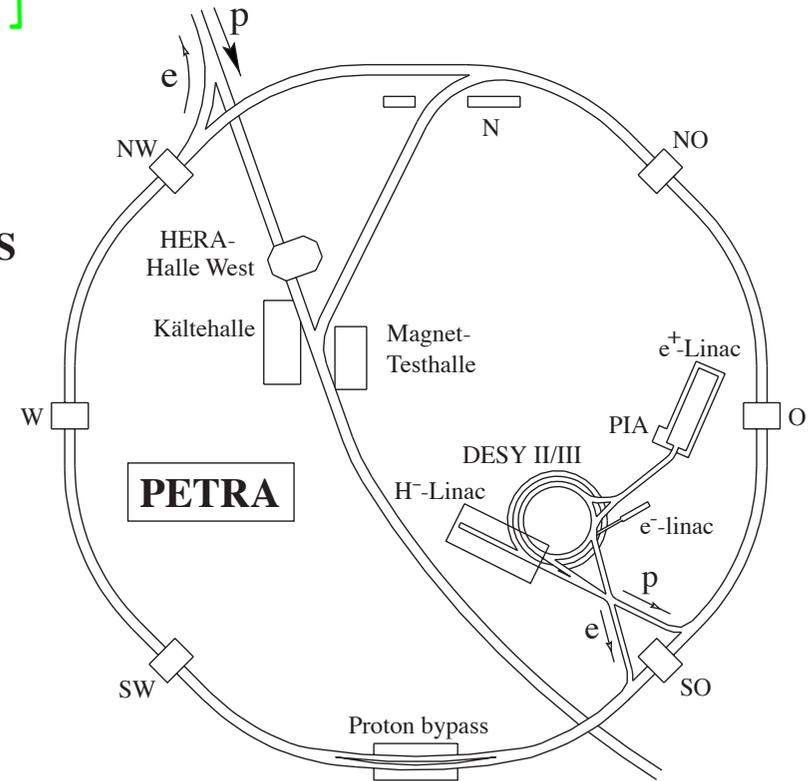
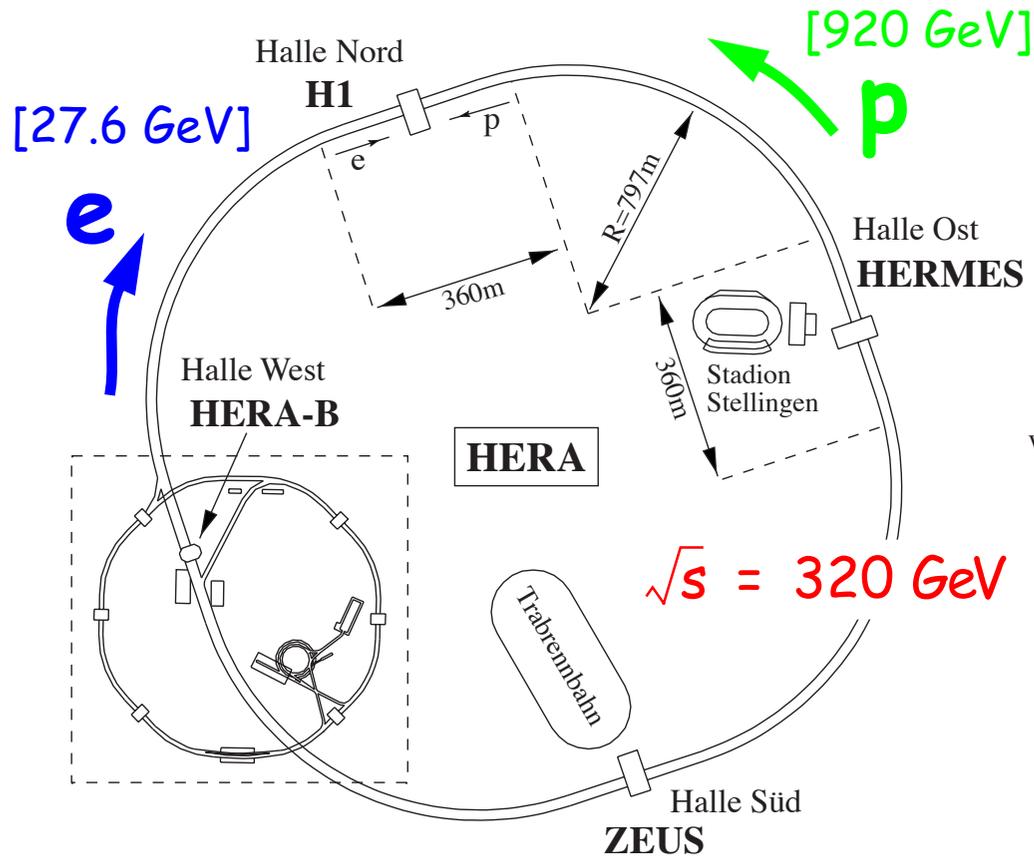
$$\Rightarrow s = 10^5 \text{ GeV}$$



HERA

PETRA

# The HERA Accelerator Complex



Proton ring:

Energy\*: 920 GeV  
Mag. Field: 4.682 T  
Current: ~ 100 mA

\* before 1998: 820 GeV

Electron ring:

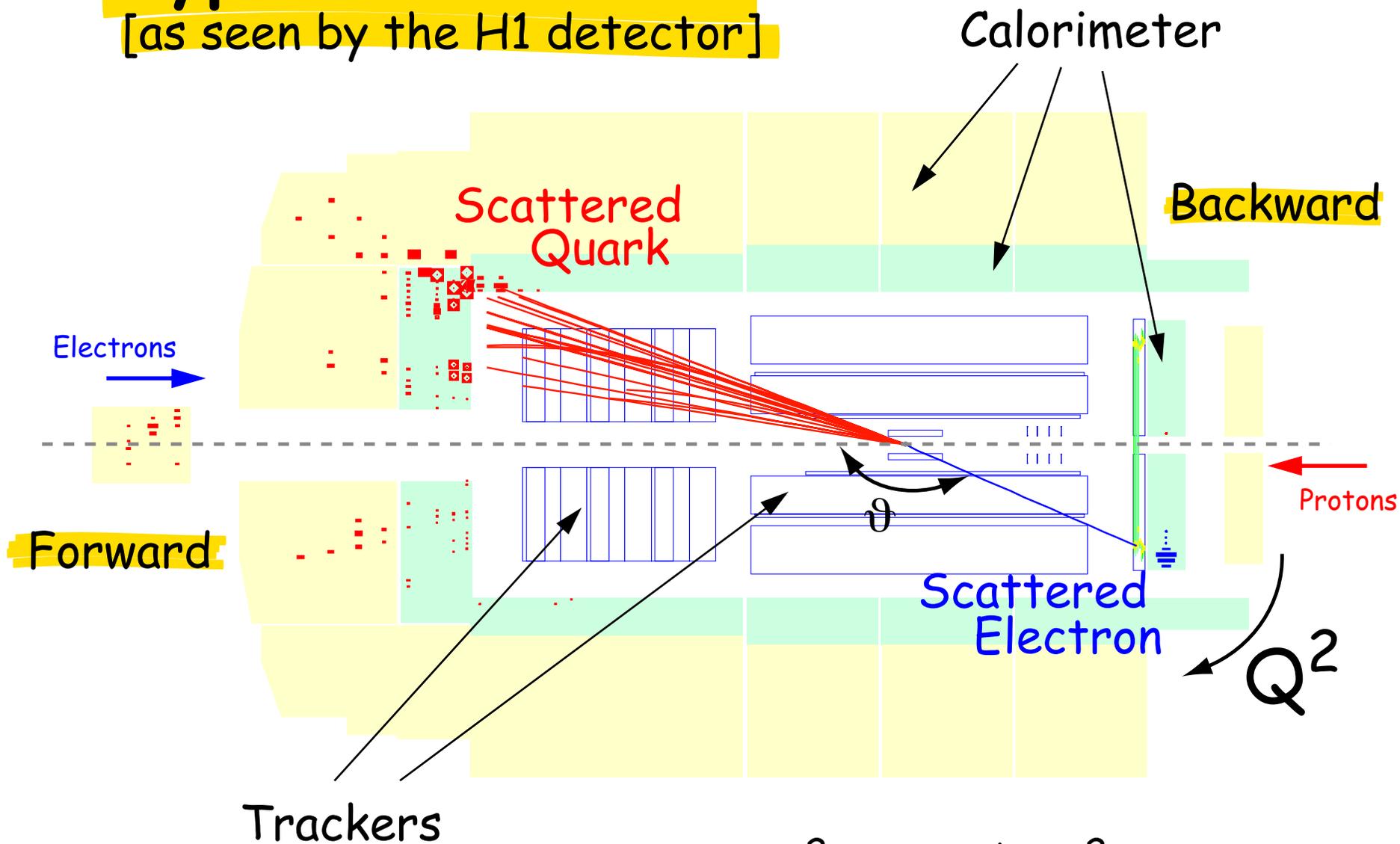
Energy: 27.5 GeV  
Mag. Field: 0.164 T  
Current: ~ 40 mA

General:

Energy in cms: 318 GeV  
Circumference: 6.3 km  
BX rate: 10.4 MHz  
Lumi:  $1.5 \cdot 10^{31} \text{ cm}^{-2}\text{s}^{-1}$

# Typical DIS-Event

[as seen by the H1 detector]



$$Q^2 = 4E_e E_e' \cos^2(\theta/2)$$

# ep Cross Section [low $Q^2$ approximation]

Proton Structure

$$F_2(x, Q^2) = x \sum_q e_q^2 [q(x, Q^2) + \bar{q}(x, Q^2)]$$

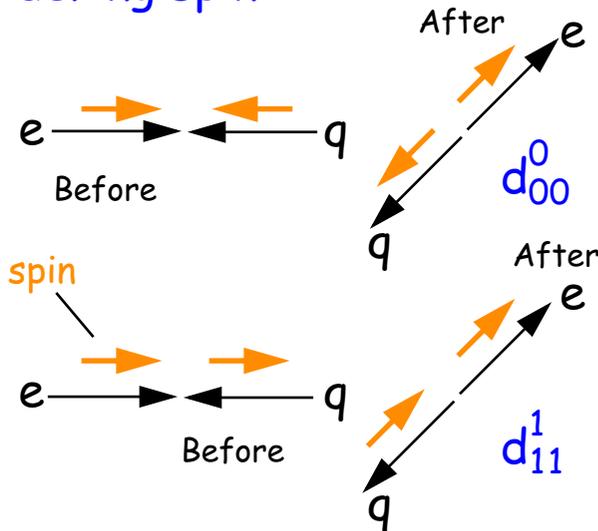
Rutherford

Evolution according to DGLAP

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} F_2(x, Q^2) \cdot \frac{1}{2} [1 + (1-y)^2] - \underbrace{y^2 F_L}_{\sim 0}$$

influence small  
related to gluon density  
[contribution only @ high  $y$ ]  
[LO:  $F_L=0$ ]

Considering spin



$$M^2 \propto |d_{\lambda, \lambda'}^J|^2 \quad d_{0,0}^0 = 1$$

$$d_{1,1}^1 = \frac{1 + \cos\theta^*}{2}$$

$$y = \frac{pq}{pk} = \frac{E_p E_e (1 - \cos\theta^*)}{2E_p E_e} = \frac{(1 - \cos\theta^*)}{2}$$

$$\rightarrow M^2 \propto 1 + (1-y)^2$$

$y$ -dependence describes helicity structure of interaction

# Structure Function $F_2$

[Principle of Measurement]

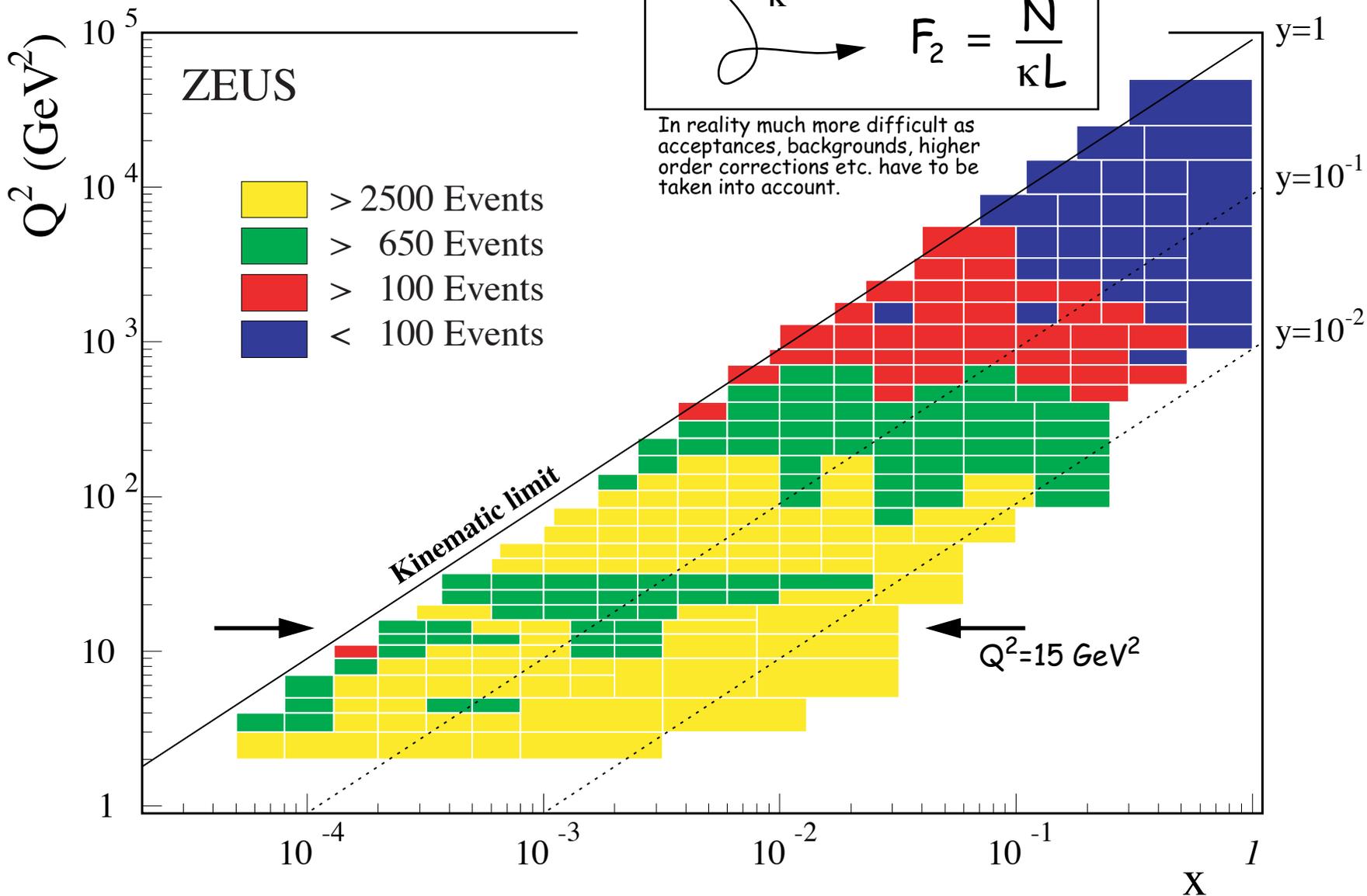
Basic (simplified) Procedure:

$$\sigma \sim \underbrace{\frac{4\pi\alpha^2}{xQ^4}}_{\kappa} F_2 \quad \text{and} \quad \sigma = N/L$$

$$F_2 = \frac{N}{\kappa L}$$

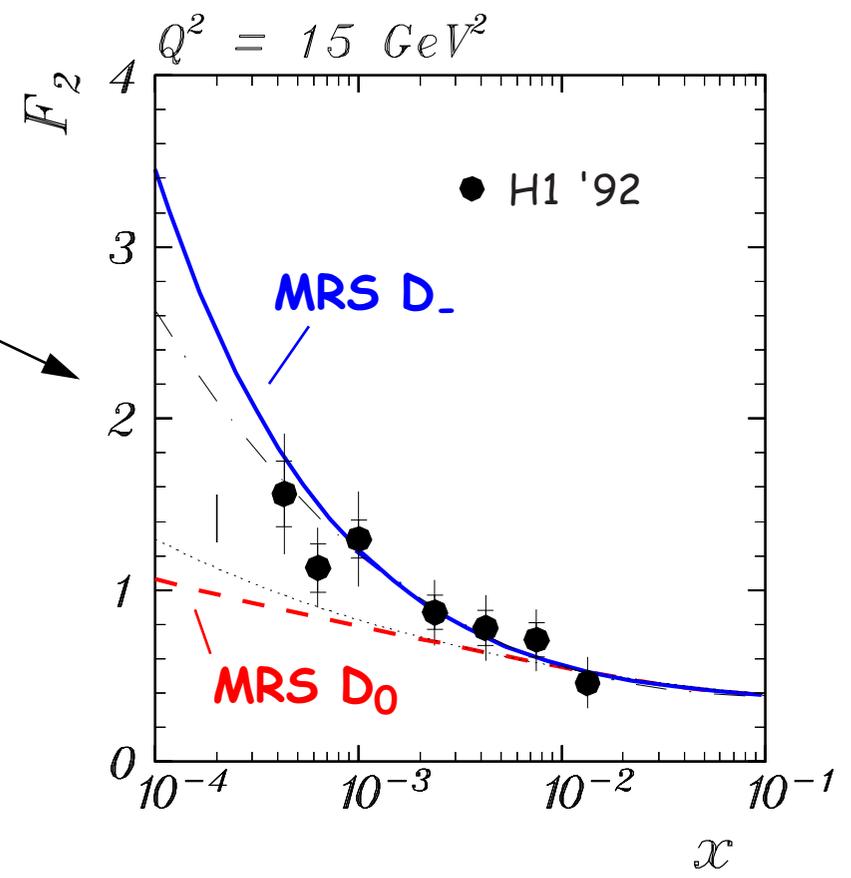
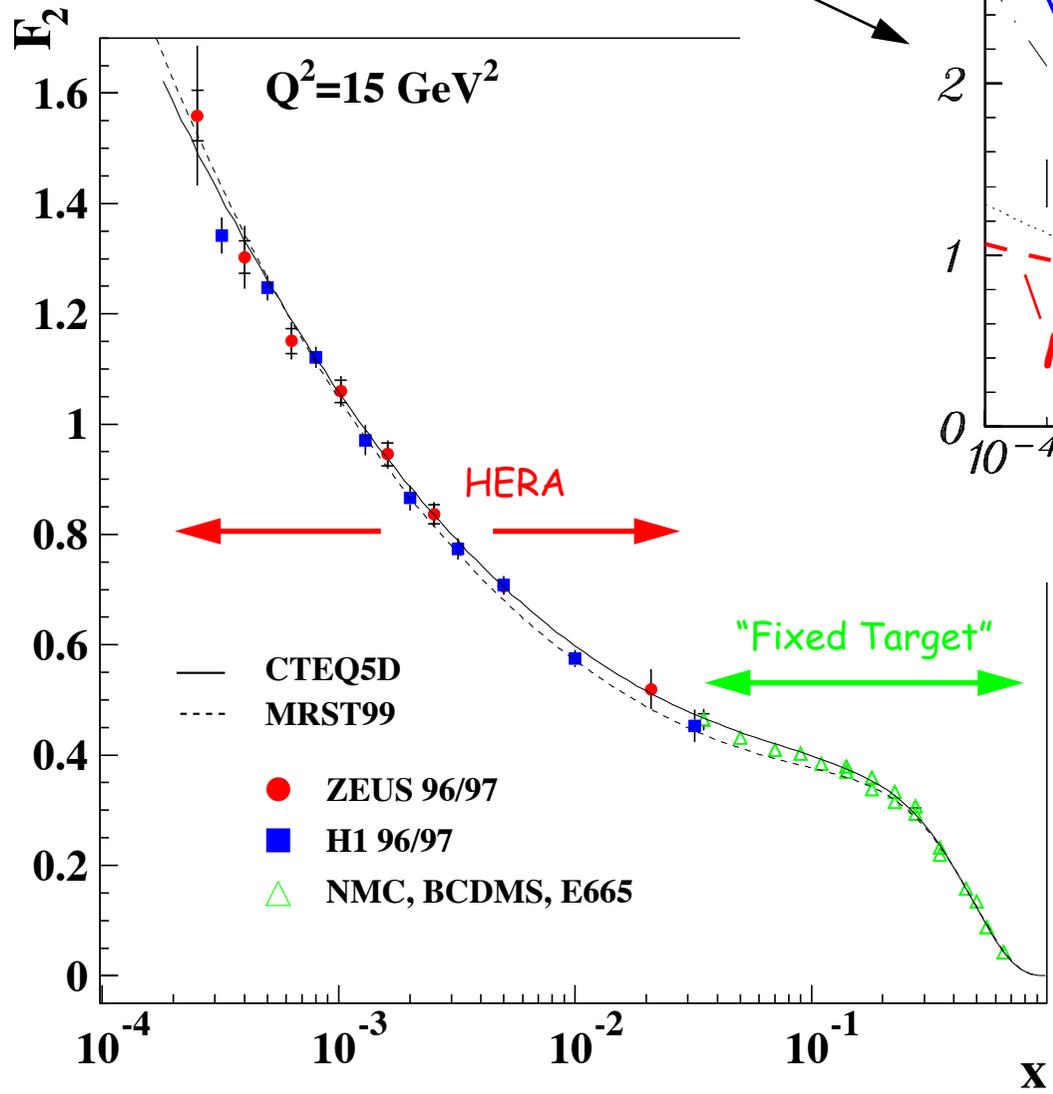
N: Number of events  
L: Luminosity

In reality much more difficult as acceptances, backgrounds, higher order corrections etc. have to be taken into account.



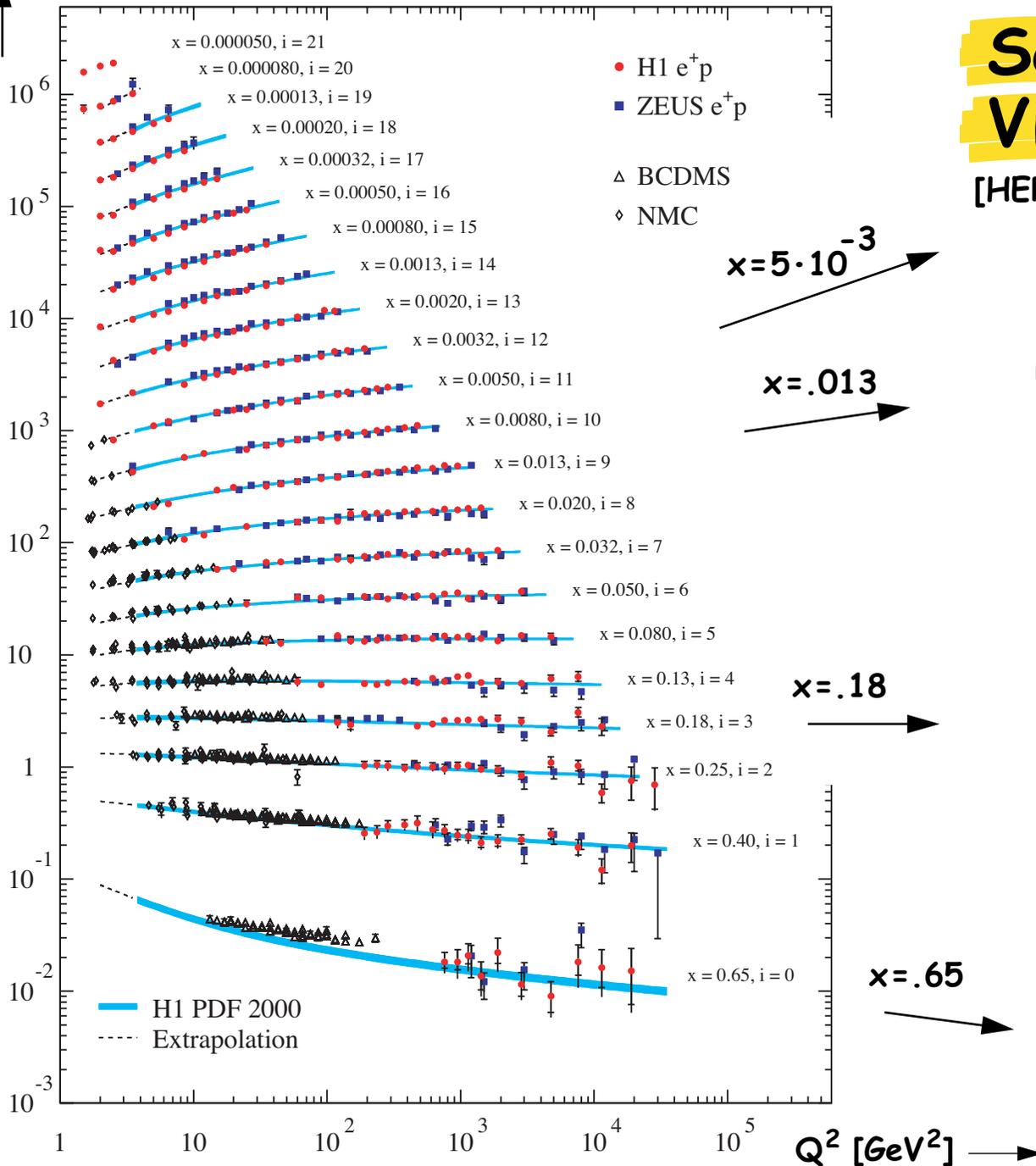
MRS D<sub>0</sub>, D<sub>-</sub>:

- Fit to fixed target data only
- Different assumptions on  $xg(x, Q^2)$



2-3%  
Precision

$F_2$   
[ $\times 2^i$ ]



# Scaling Violations

[HERA & fixed target data]

$x = 5 \cdot 10^{-3}$

$x = .013$

Precision: 2-3%  
[bulk region]

For  $x < 10^{-2}$ :

$$\frac{dF_2}{d \log Q^2} \sim g(x, Q^2) \cdot \alpha_s(Q^2)$$

$x = .18$

NLO QCD Fits:

- Quark densities
- Gluon density
- Strong coupling  $\alpha_s$

$x = .65$

# QCD Fits: Principle

## Fit Procedure

- Parametrize parton distribution functions (PDFs) at starting scale  $Q^2 = Q_0^2$  as function of  $x$ .
- Perform QCD evolution using DGLAP equations.  
[usually NLO, special treatment of heavy quark PDFs]
- Calculate predictions for experimental observables.  
[cross sections, structure functions, ...]
- Determine PDF parameters from  $\chi^2$ -fit to experimental data.

For  $p = u_v, d_v, \sum(q + \bar{q}), g$  or  $p = \bar{u} + \bar{d}, \bar{u} - \bar{d}, s$ :

$$xp(x, Q_0^2) = A_p x^{a_p} (1-x)^{b_p} P(x; c_p, \dots)$$

characterizes PDFs  
at  $x = 0$ .  
[sea:  $a_p < 0$ , valence:  $a_p > 0$ ]

characterizes PDFs  
at  $x = 1$ .  
[ $b_p > 0$  for all PDFs]

weakly  $x$ -dependent  
function.  
["fine tuning"]

# QCD Fits: Inputs

- Fixed target data —  $\ell p \rightarrow \ell p$ : BCDMS, NMC, E665 ...  
 $\ell p \rightarrow \nu p$ : CCFR, CDHS, BEBC ...
- H1, ZEUS data — structure function and cross section measurements

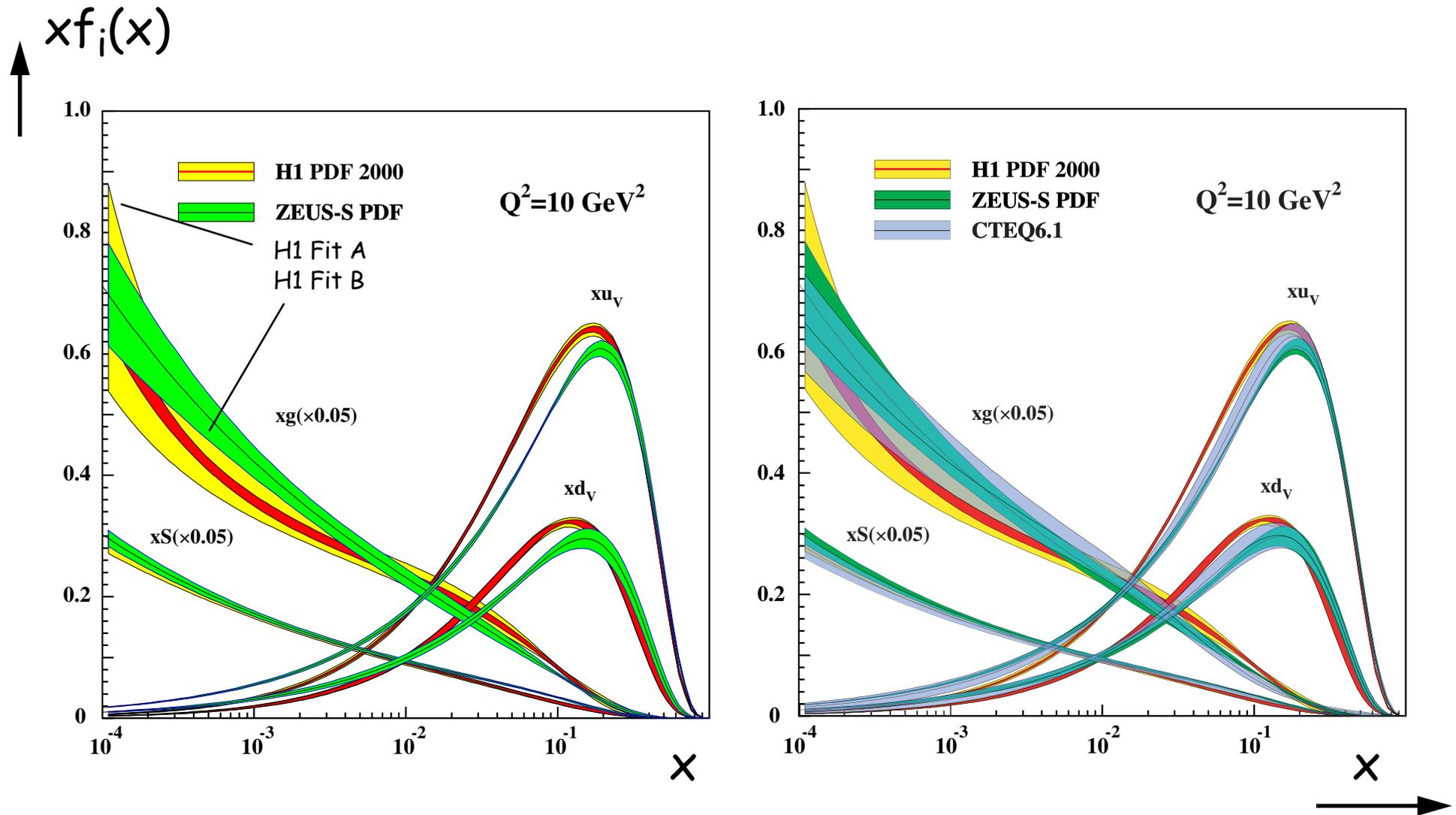
- Sum rules:  $\int u_v(x) dx = 2, \int d_v(x) dx = 1,$  Valence quarks
- $$\int dx x \left\{ g(x) + \sum [q(x) + \bar{q}(x)] \right\} = 1,$$
 Momentum sum rule
- $$I_G = \int dx (F_2^{\ell p} - F_2^{\ell n}) = \frac{1}{3} + \frac{2}{3} \int dx (\bar{u} - \bar{d}).$$
 Gottfried sum rule

[Experiment (NMC):  $I_G = 0.235 \pm 0.026 \rightarrow \bar{u} > \bar{d}$ ]

- Other experimental data:

$p\bar{p} \rightarrow W + X$	$q\bar{q} \rightarrow W$	$u, d, u/d$
$\nu N \rightarrow \mu^+ \mu^- + X$	$\nu s \rightarrow \mu c$	$s$
$pp, pN \rightarrow \ell^+ \ell^- + X$	$q\bar{q} \rightarrow \ell^+ \ell^-$	$\bar{d}/\bar{u}$
$hh \rightarrow \gamma + X$	$qg \rightarrow q\gamma$	$g$
$p\bar{p} \rightarrow \text{jets} \pm X$	$gg \rightarrow gg, qg \rightarrow \dots$	$g$

# Parton Densities — HERA Results



# Comparison H1 vs. ZEUS

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H1  $\alpha_s$  fit:

Dedicated to  $\alpha_s$  and  $g(x)$ .  
H1 ep NC data (low  $Q^2$ ) & BCDMS  $\mu p$  data.  
Parametrization of valence, sea quark and gluon.  
Starting scale:  $Q_0^2 = 4 \text{ GeV}^2$ .

$$\alpha_s = 0.1150^{+0.0019}_{-0.0018} \pm 0.005$$

scale  
uncertainty

exp. & model  
uncertainty

H1 PDF fit:

Dedicated to PDF-determination.  
Fit A: H1 data only (NC, CC, low & high  $Q^2$ ).  
Fit B: H1 data & BCDMS  $\mu p$  data.  
Parametrization of U,  $\bar{U}$ , D,  $\bar{D}$  and gluon.  
Starting scale:  $Q_0^2 = 4 \text{ GeV}^2$ .

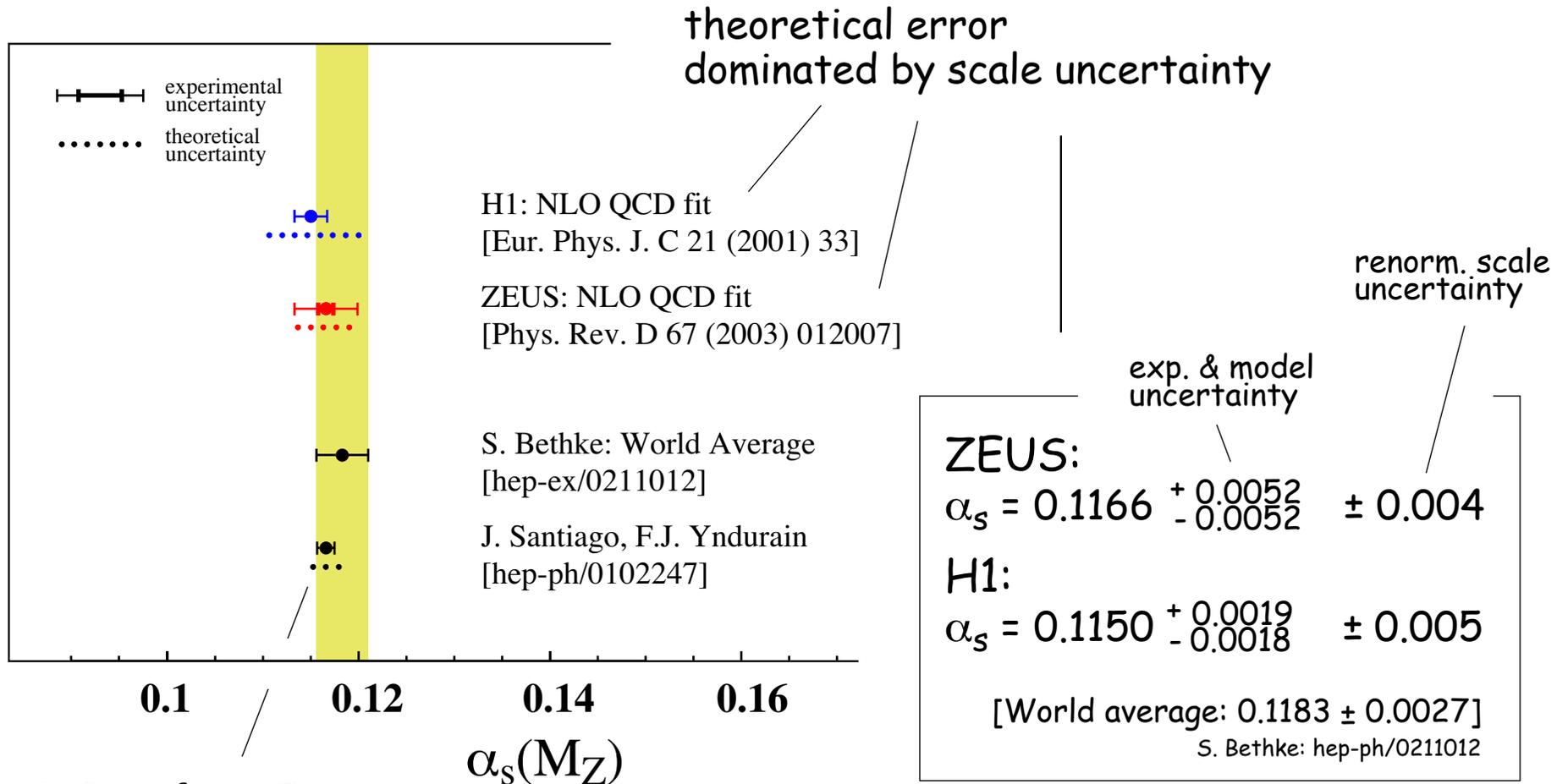
ZEUS PDF fit:

Dedicated to PDF-determination (main goal).  
Simultaneous fit to strong coupling constant.  
Data: ZEUS NC data, BCDMS, NMC, E665, CCFR.  
Starting scale:  $Q_0^2 = 7 \text{ GeV}^2$ .

$$\alpha_s = 0.1166^{+0.0052}_{-0.0052} \pm 0.004$$

exp. & model  
uncertainty

scale  
uncertainty



**NNLO  $\alpha_s$  from  $F_2$**   
 moment analysis based on Bernstein polynomials

systematic error includes:  
 NNNLO correction estimate  
 higher twist effects

**NNLO promises world beating  $\alpha_s$  from HERA**

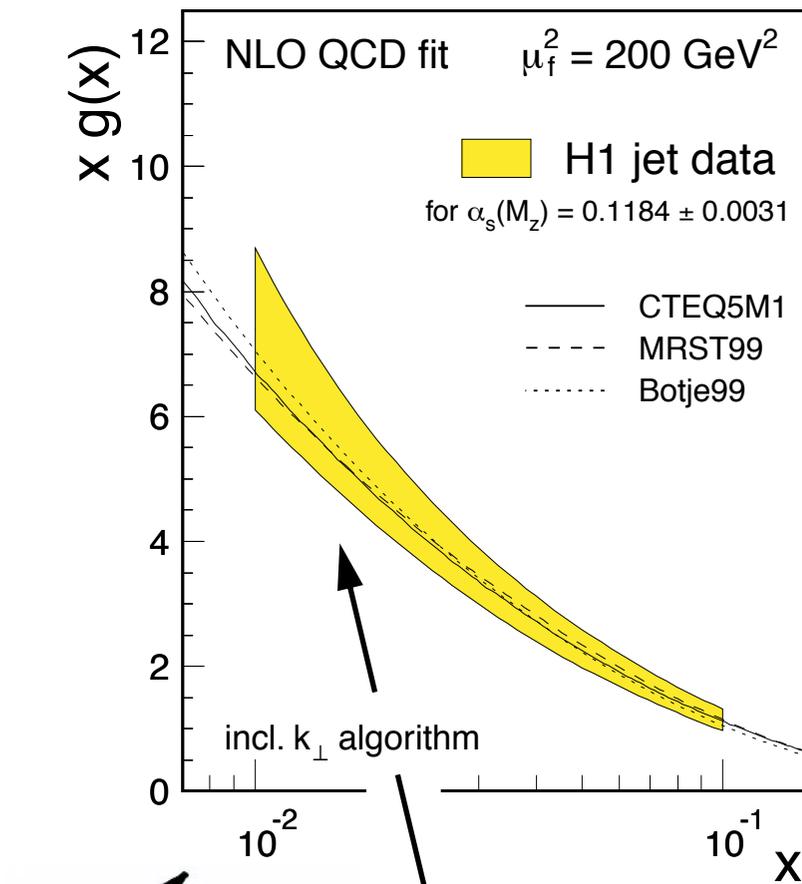
**Now available:**  
**NNLO splitting functions**

[Moch, Vermaseren, Vogt]

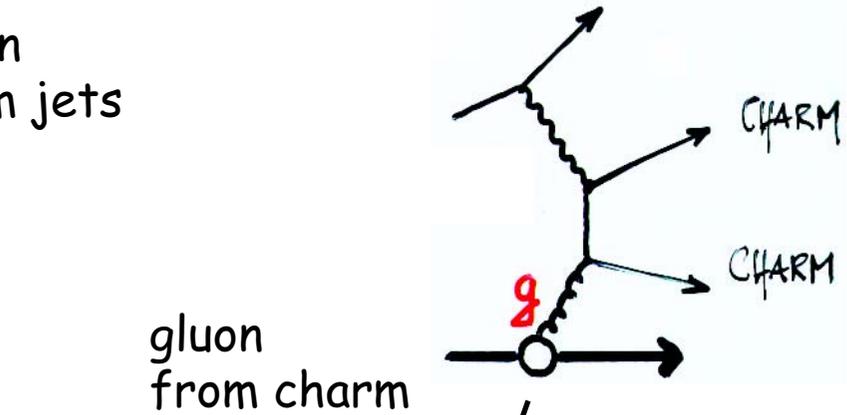
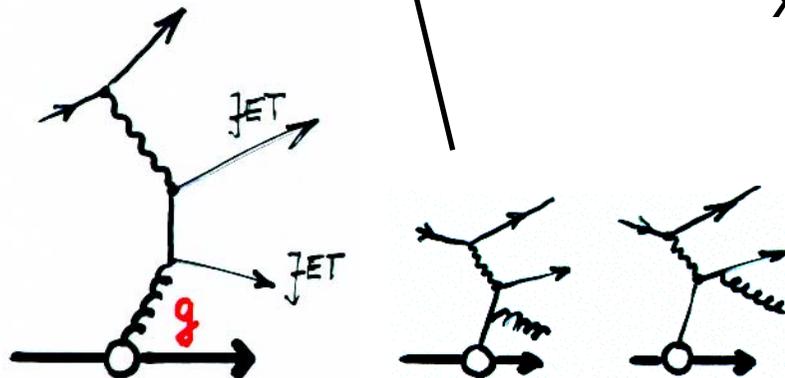
Non-singlet case: hep-ph/0403192

Singlet case: hep-ph/0404111

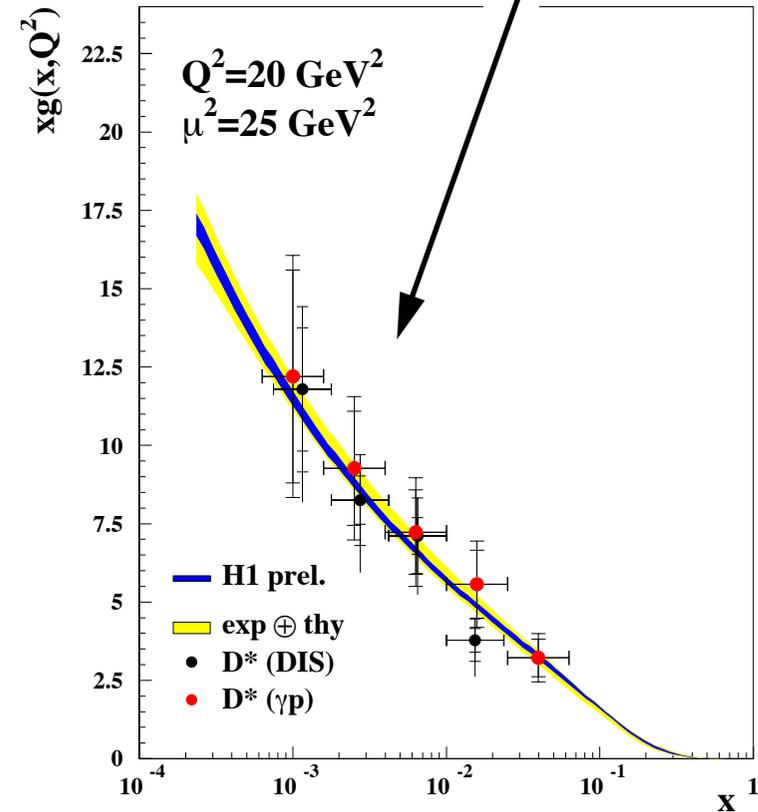
# PDFs - Are they universal?



gluon  
from jets



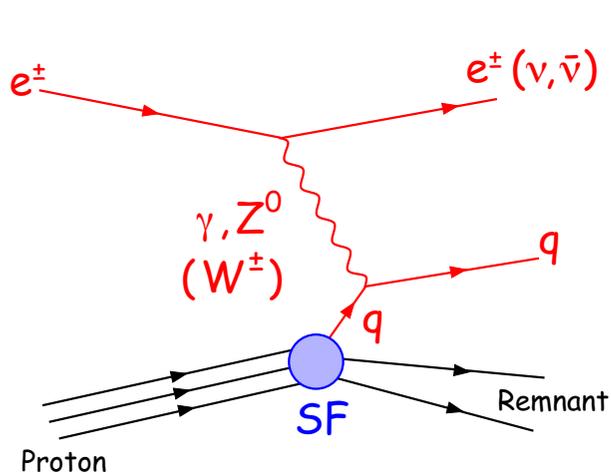
gluon  
from charm



# High $Q^2$ Physics

## Constraining Valence Quarks

# DIS Cross Section @ High $Q^2$



Influence  
only @ high  $y$

$$\frac{d^2\sigma(e^\pm)}{dx dQ^2} \sim \xi F_2 \mp \zeta x F_3 - \eta y^2 F_L$$

different contribution from  $x F_3$   
for different lepton charge

Neutral Current:

$$F_2 \sim x \sum_i [q_i + \bar{q}_i]$$

$$xF_3 \sim x \sum_i [q_i - \bar{q}_i]$$

Use  $e^+p/e^-p$  data to extract  $xF_3$   
Sensitivity to valence quark density

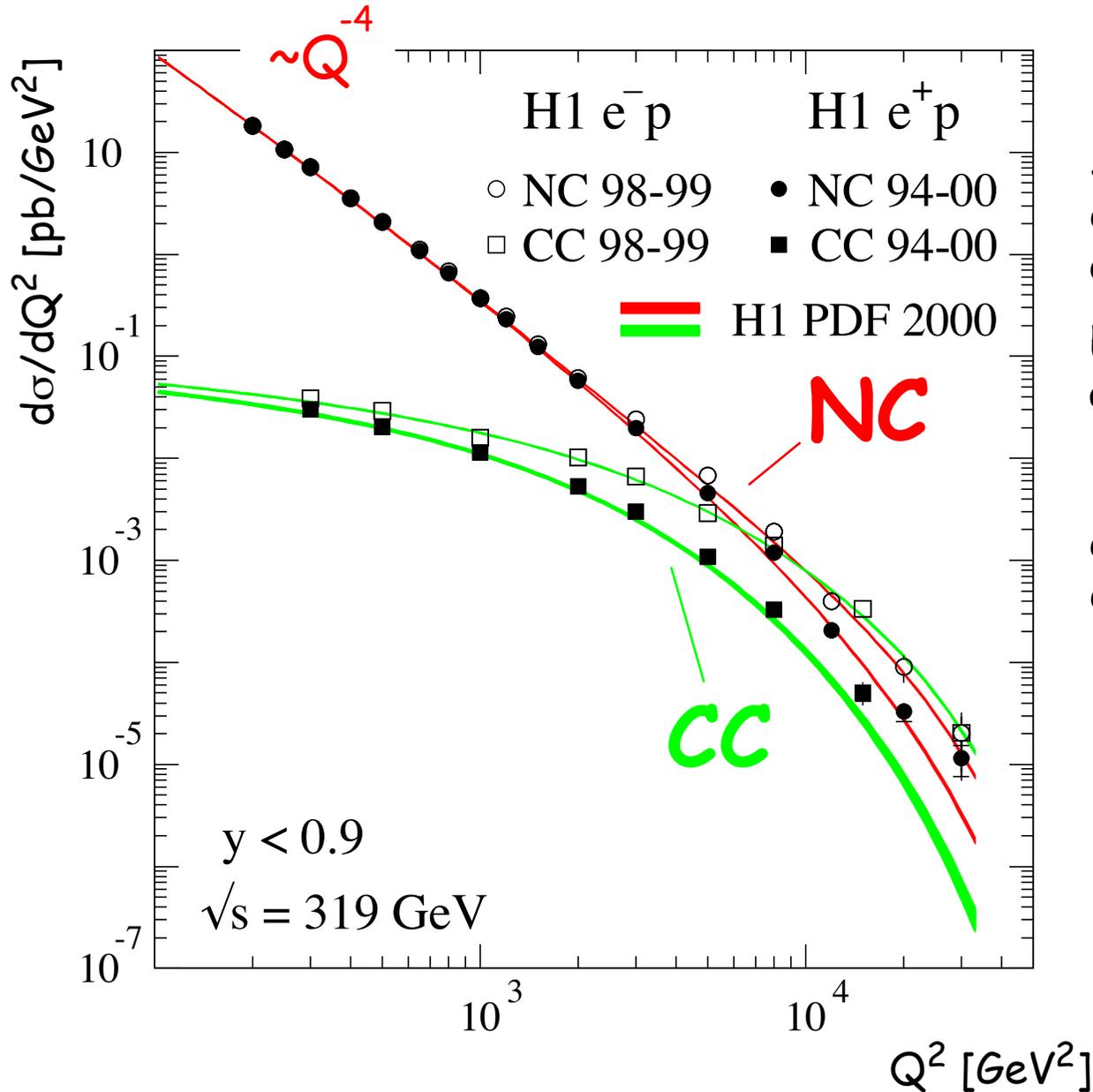
Charged Current:

$$d^2\sigma(e^+) \sim x [d + \bar{u}]$$

$$d^2\sigma(e^-) \sim x [u + \bar{d}]$$

Use  $e^+p/e^-p$  data to disentangle  
up-/down-quark content at high  $x$

# NC and CC Cross Sections



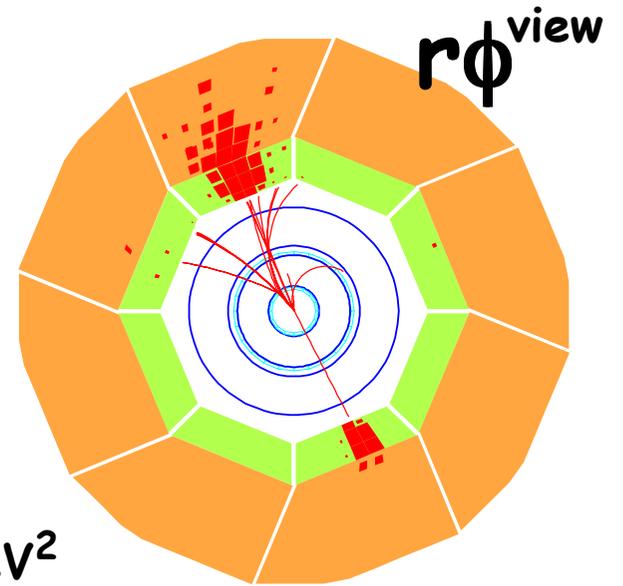
Standard Model describes cross sections over large range of  $Q^2$

Electroweak 'unification' at large  $Q^2 \sim M_Z^2$

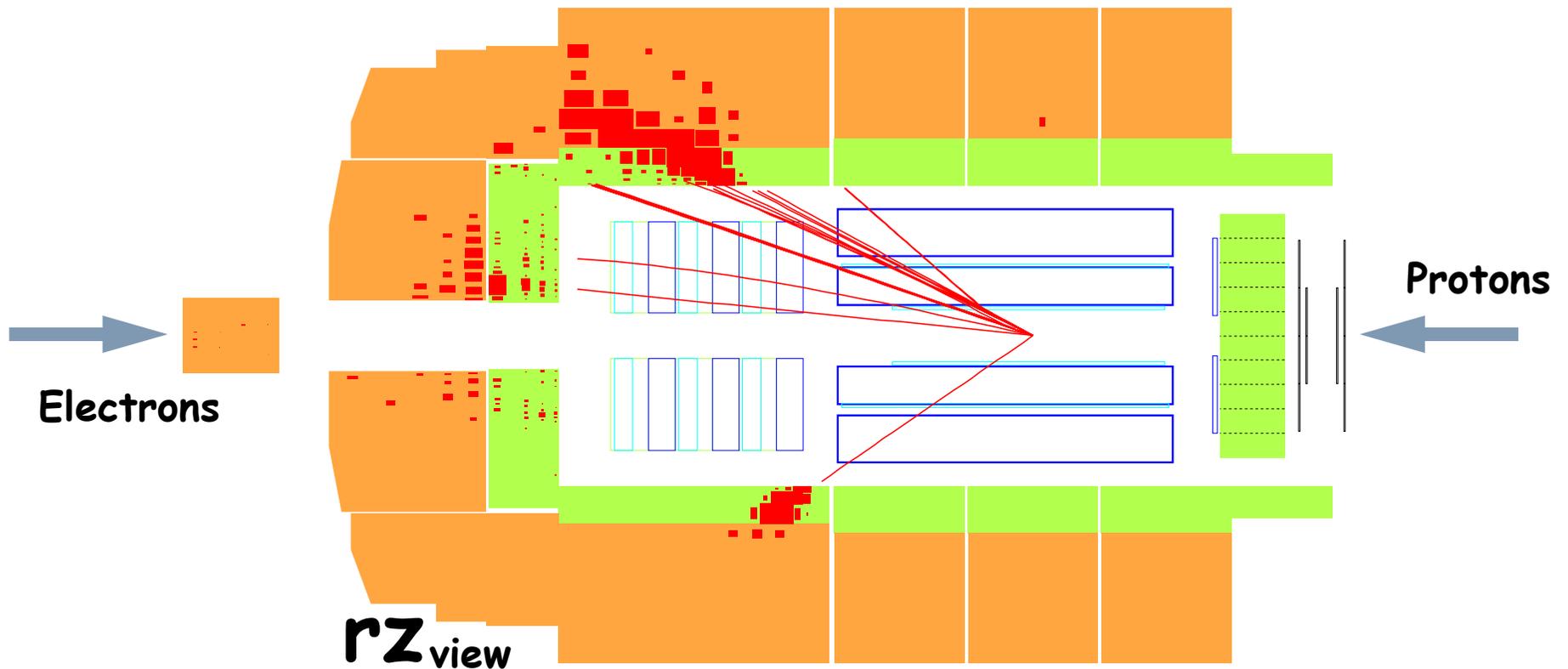
e<sup>+</sup>p/e<sup>-</sup>p cross sections differ due to different quark contributions  
 helicity structure of EW interactions

# NC DIS Event

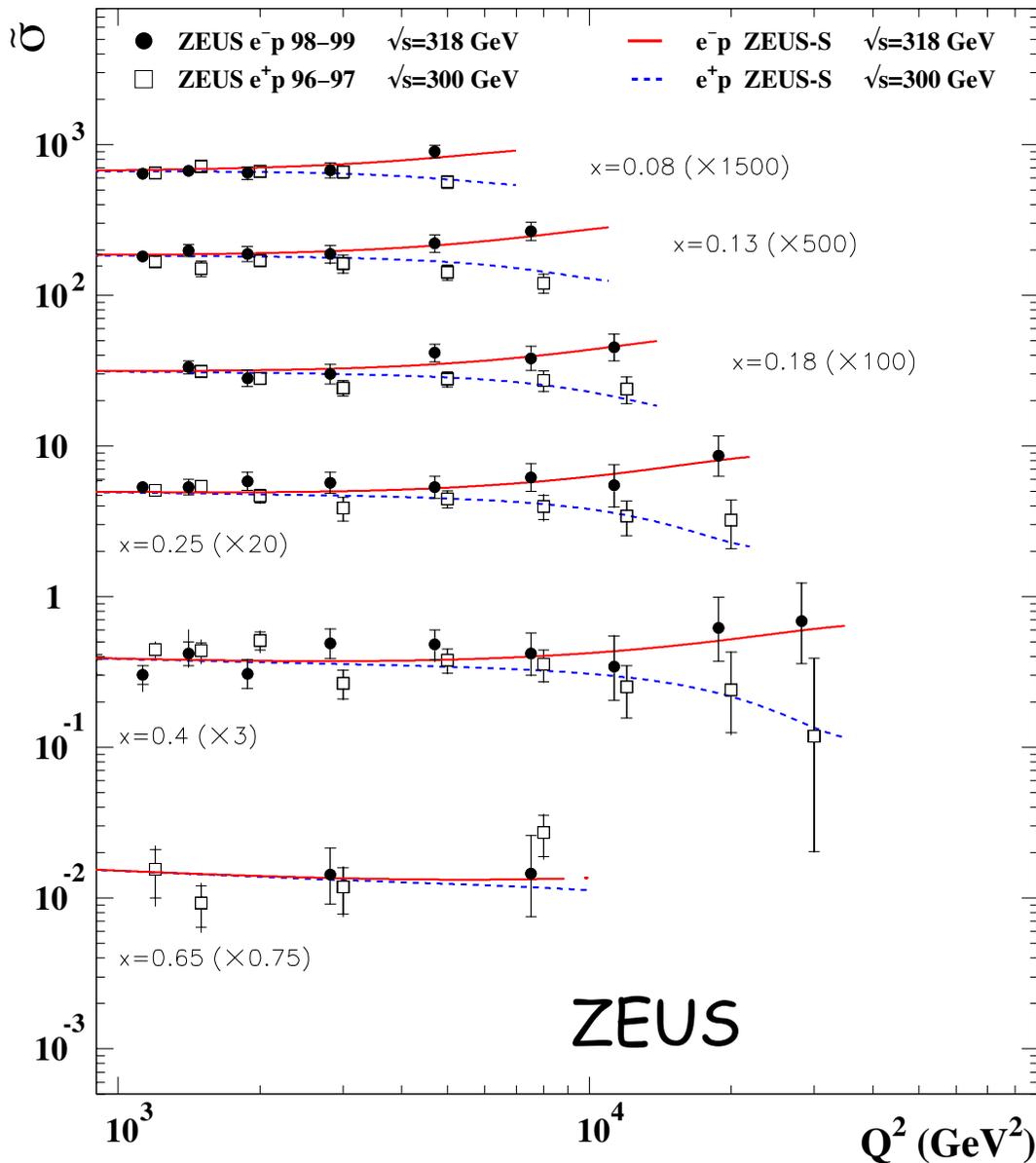
[as seen in a typical HERA detector]



$$Q^2 = 16950 \text{ GeV}^2$$



# NC Reduced Cross Section



$1/(xQ^4)$ -dependence removed

$xF_3$  Extraction:

$$\tilde{\sigma}^{\text{NC}}(e^-) = \xi F_2 + \zeta x F_3$$

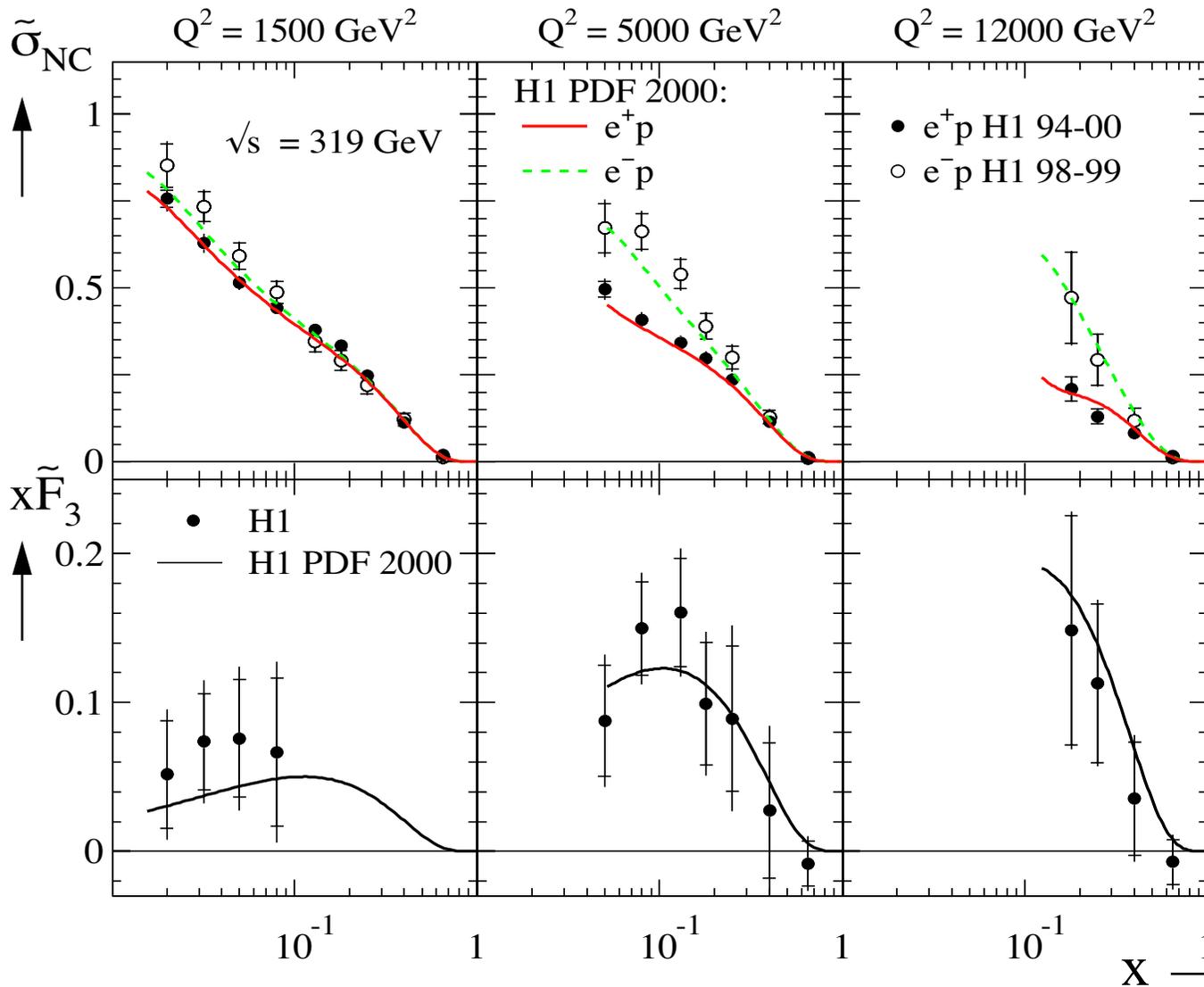
$$\tilde{\sigma}^{\text{NC}}(e^+) = \xi F_2 - \zeta x F_3$$

---


$$xF_3 = \frac{1}{2} \zeta^{-1} [\tilde{\sigma}^{\text{NC}}(e^-) - \tilde{\sigma}^{\text{NC}}(e^+)]$$

$$\sim \sum [q(x, Q^2) - \bar{q}(x, Q^2)]$$

At high  $Q^2$ : sensitivity to valence quark densities down to  $x \sim 10^{-2}$



$x\tilde{F}_3$

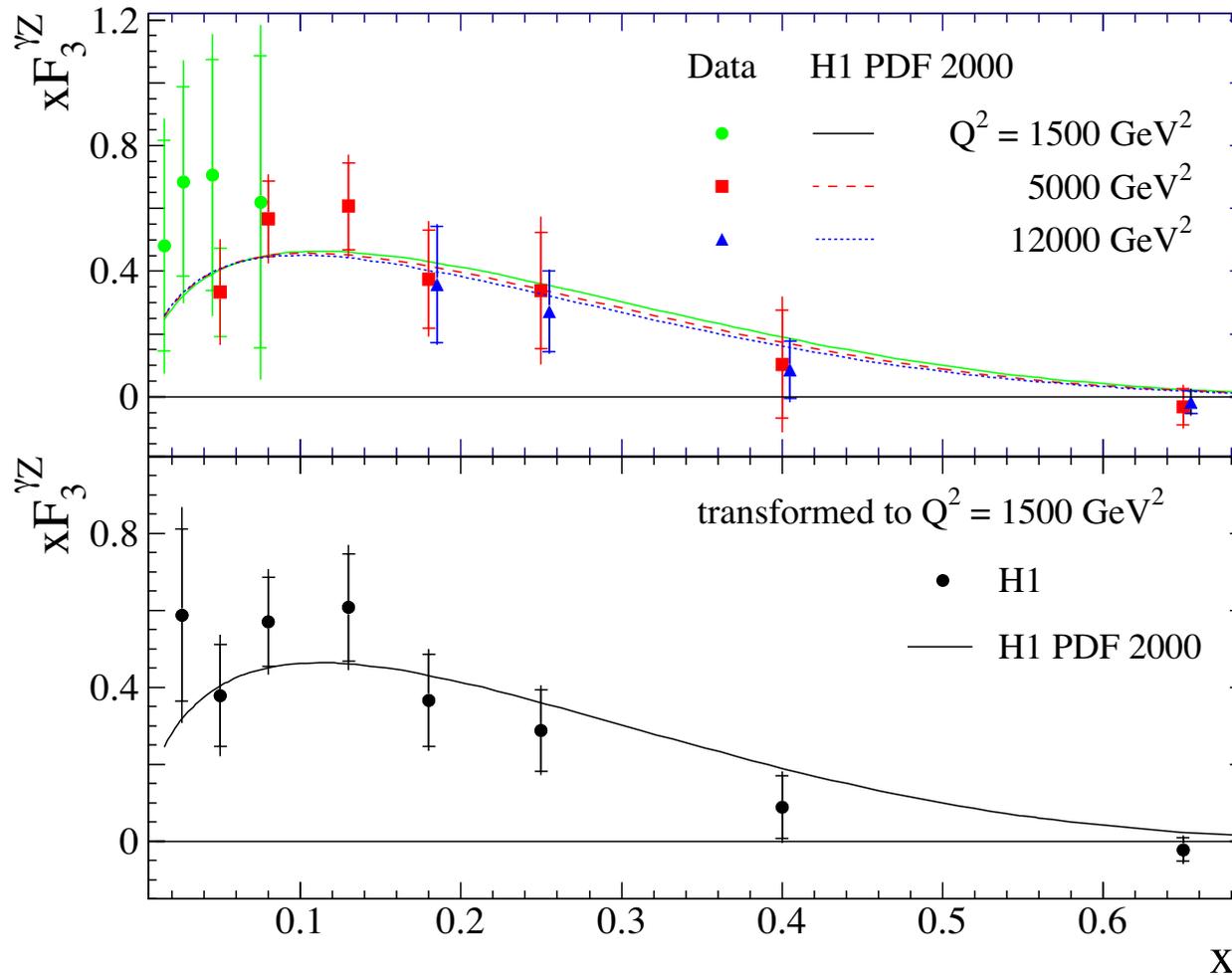
Agreement of data with QCD fit

at fixed Bjorken- $x$   
 $x\tilde{F}_3$  rises with  $Q^2$   
 due to:

$$\chi_Z = \frac{1}{4 s_W^2 c_W^2} \left( \frac{Q^2}{Q^2 + M_Z^2} \right)$$

Z-Propagator

$$x\tilde{F}_3 = Q_e a_e \left\{ \underbrace{2Q_q a_q x [q_i - \bar{q}_i]}_{\sim Q_e a_e \{x\tilde{F}_3^{\gamma Z}\}} \right\} \cdot \chi_Z + \underbrace{2v_e a_e \left\{ 2v_q a_q x [q_i - \bar{q}_i] \right\}}_{\text{contribution to } x\tilde{F}_3 < 3\%} \cdot (\chi_Z)^2$$



$x F_3^{\gamma Z}$

$$\int_{0.02}^{0.65} F_3^{\gamma Z} = 1.28 \pm 0.20$$

[H1 measurement]

$$\int_{0.02}^{0.65} F_3^{\gamma Z} = 1.06 \pm 0.02$$

[H1 PDF 2000]

$$\int_0^1 F_3^{\gamma Z} = \int_0^1 2Q_q a_q [q_i - \bar{q}_i] = 2Q_u a_u N_u + 2Q_d a_d N_d = \frac{5}{3} \cdot (1 - \alpha_s/\pi)$$

[sum rule a la Gross Llewellyn-Smith]

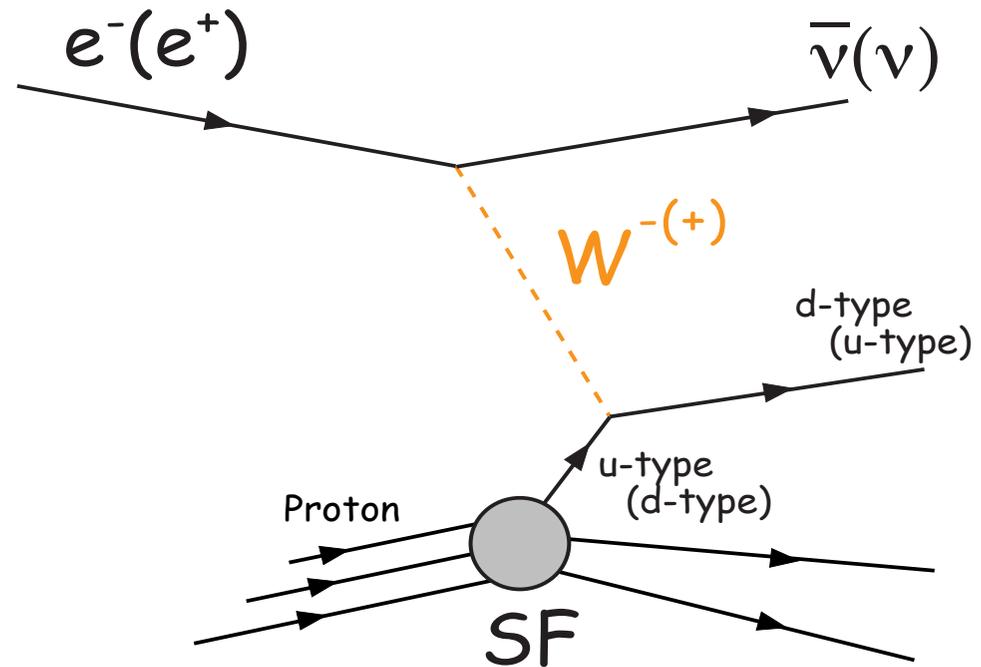
# Charged Current Cross Section

$$e^- + u \rightarrow d + \bar{\nu}$$

$$e^- + \bar{d} \rightarrow \bar{u} + \bar{\nu}$$

$$e^+ + d \rightarrow u + \nu$$

$$e^+ + \bar{u} \rightarrow \bar{d} + \nu$$



$$\frac{d^2\sigma^{CC}(e^-)}{dx dQ^2} = \frac{\pi\alpha^2}{4s_W^2} \frac{1}{(Q^2 + M_W^2)^2} [\underbrace{u + c}_{\text{Probes u-quark density}} - (1 - \gamma)^2(\bar{d} + \bar{s})]$$

$$\frac{d^2\sigma^{CC}(e^+)}{dx dQ^2} = \frac{\pi\alpha^2}{4s_W^2} \frac{1}{(Q^2 + M_W^2)^2} [\bar{u} + \bar{c} - (1 - \gamma)^2(\underbrace{d + s}_{\text{Probes d-quark density}})]$$

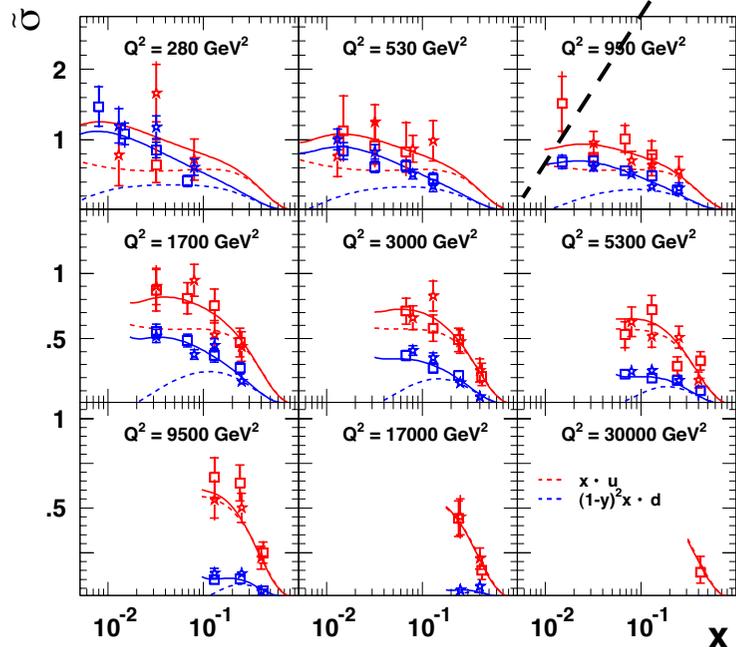
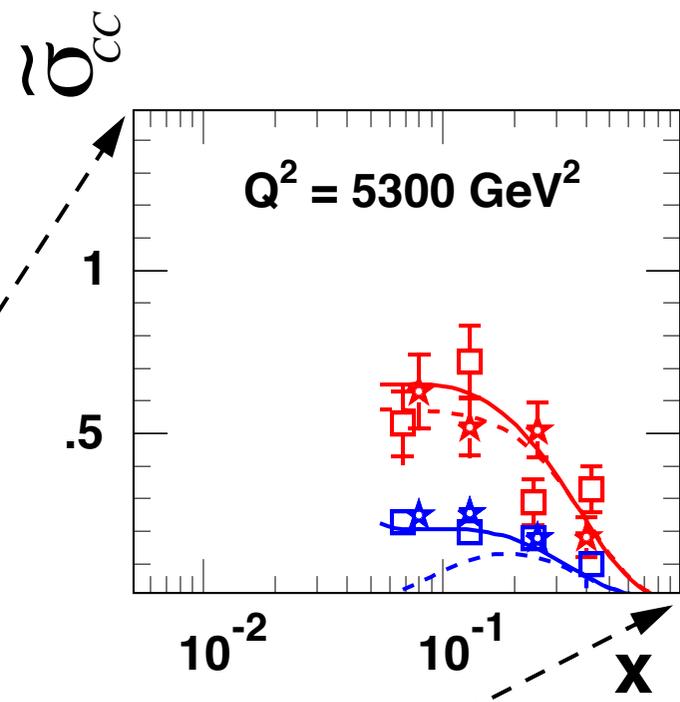
# Reduced CC Cross Section

$$\tilde{\sigma}_{CC}^{\pm} = \left[ \frac{4s_W^2(Q^2 + M_W^2)^2}{\pi\alpha^2} \right] \frac{d^2\sigma_{CC}(e^{\pm})}{dx dQ^2}$$

$$\tilde{\sigma}_{CC}^{+} = x[\bar{u} + \bar{c} + (1-y)^2(d+s)]$$

$$\tilde{\sigma}_{CC}^{-} = x[u + c + (1-y)^2(\bar{d} + \bar{s})]$$

- ★ H1 e<sup>-</sup>p
- ★ H1 e<sup>+</sup>p 94-00
- SM e<sup>-</sup>p (CTEQ6D)
- ZEUS e<sup>-</sup>p 98-99
- ZEUS e<sup>+</sup>p 99-00
- SM e<sup>+</sup>p (CTEQ6D)

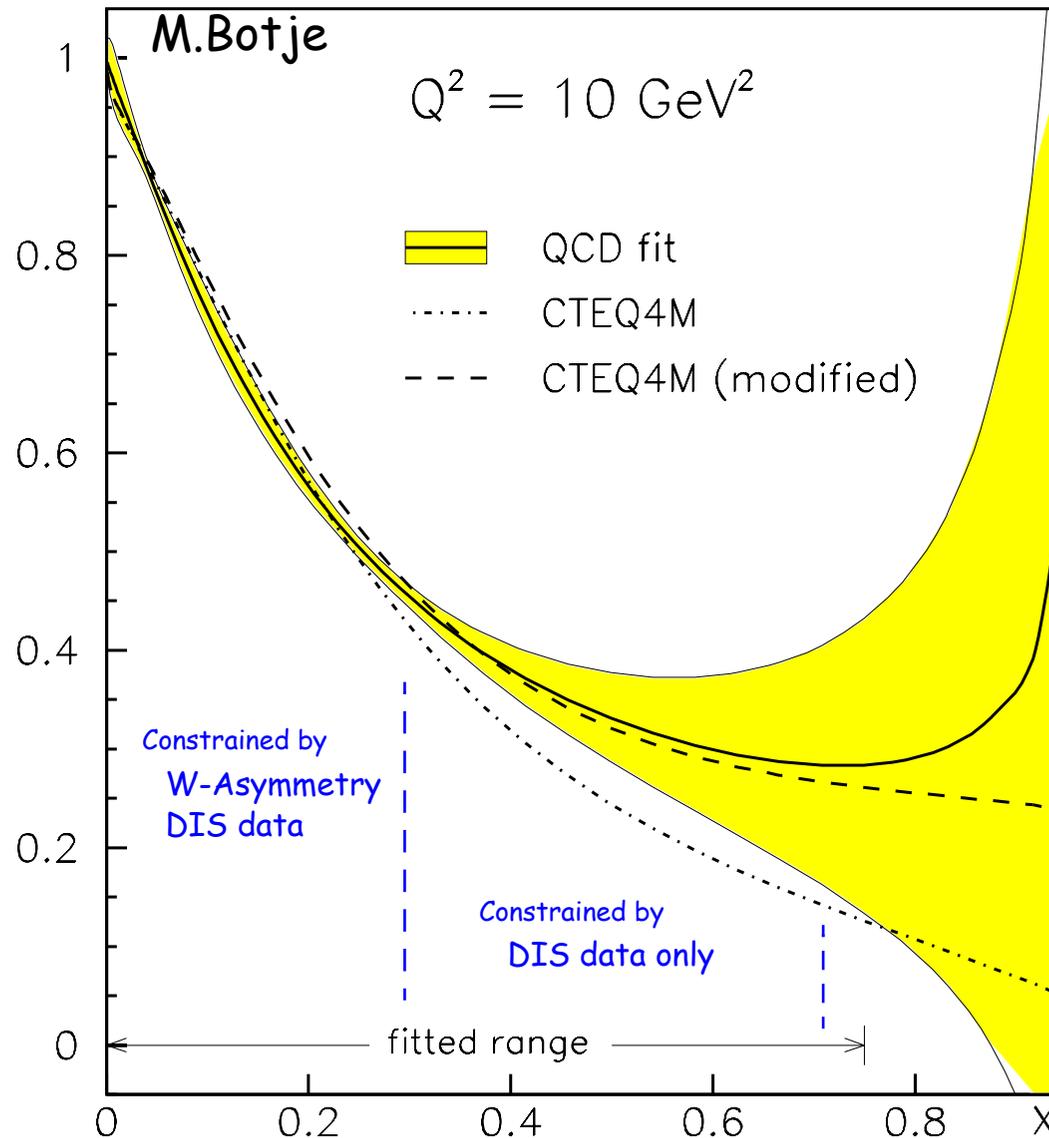


Sensitivity to u(d)-Quark density

More statistics!  
[HERA II Data]

# Knowledge of d/u Ratio

d/u



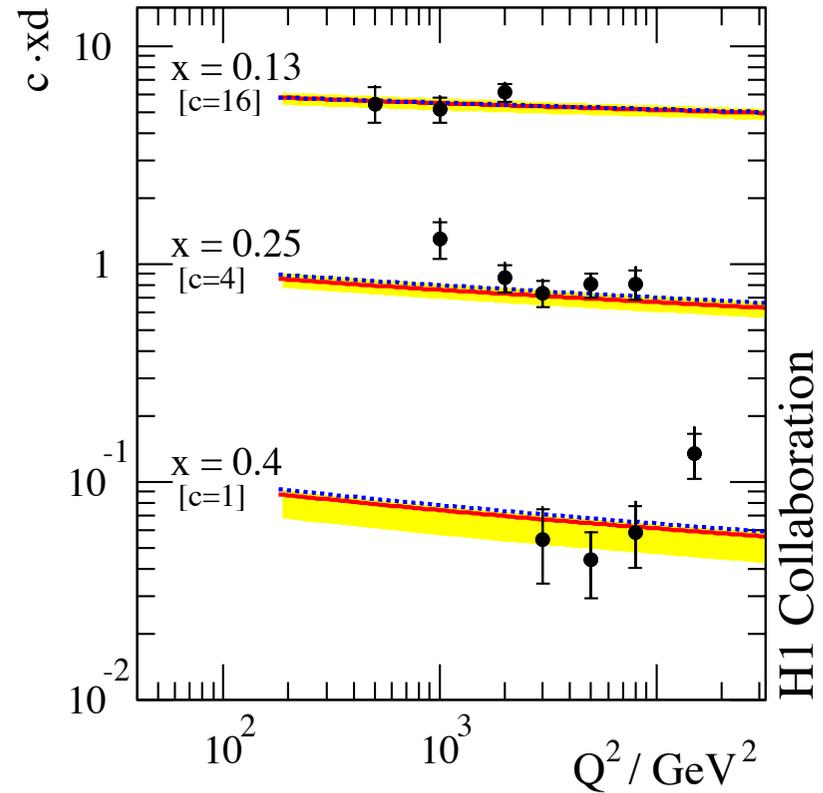
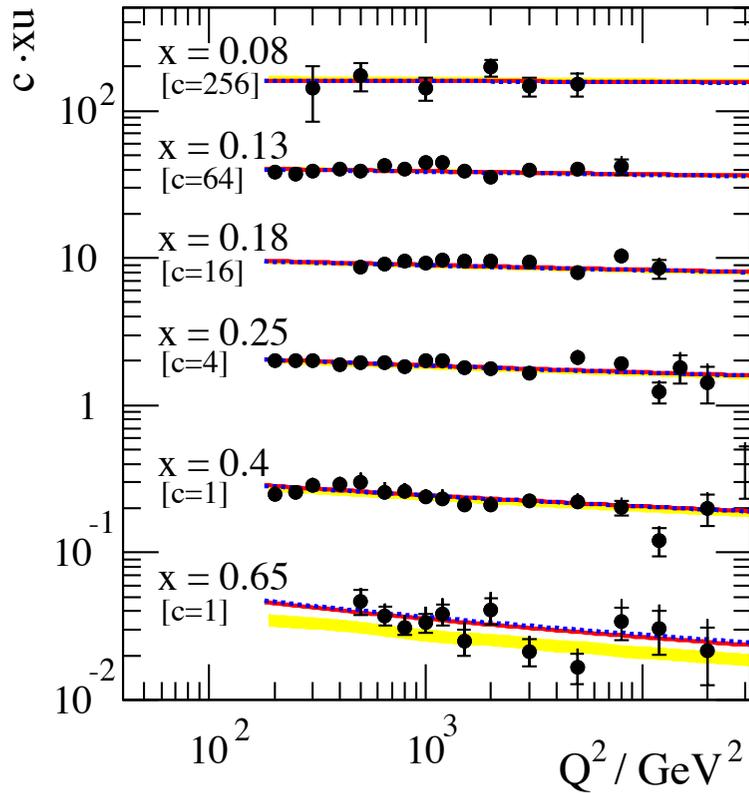
Fit to

- HERA ep data [H1 1994, ZEUS 1994]
- Fixed Target proton and deuteron data [E665, NMC, BCDMS, SLAC]
- Neutrino data [CCFR]
- Drell-Yan data [E866]

Large uncertainty at high x  
[dependence on parametrization]  
[e.g. due to nuclear corrections]

Can be further constrained  
with NC and CC HERA data.

# Valence Quark Distribution @ high x



- MRST2001
- ⋯ CTEQ6
- H1 PDF 2000

● H1 data points

determined via local extraction method ...

$$xq = \sigma_{\text{meas}} (xq/\sigma)_{\text{fit}}$$

Uses:  
 H1 high- $Q^2$  data,  
 [NC/CC  $e^+p$  and  $e^-p$  data]  
 H1 low- $Q^2$  data

To constrain  $d, u$  at high  $x$  further  
**more statistics from HERA II**  
 is needed.

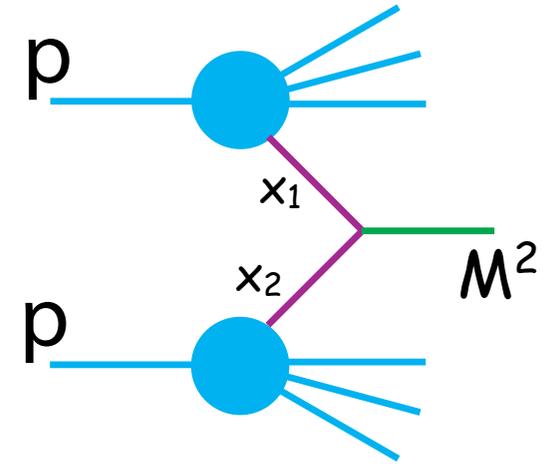
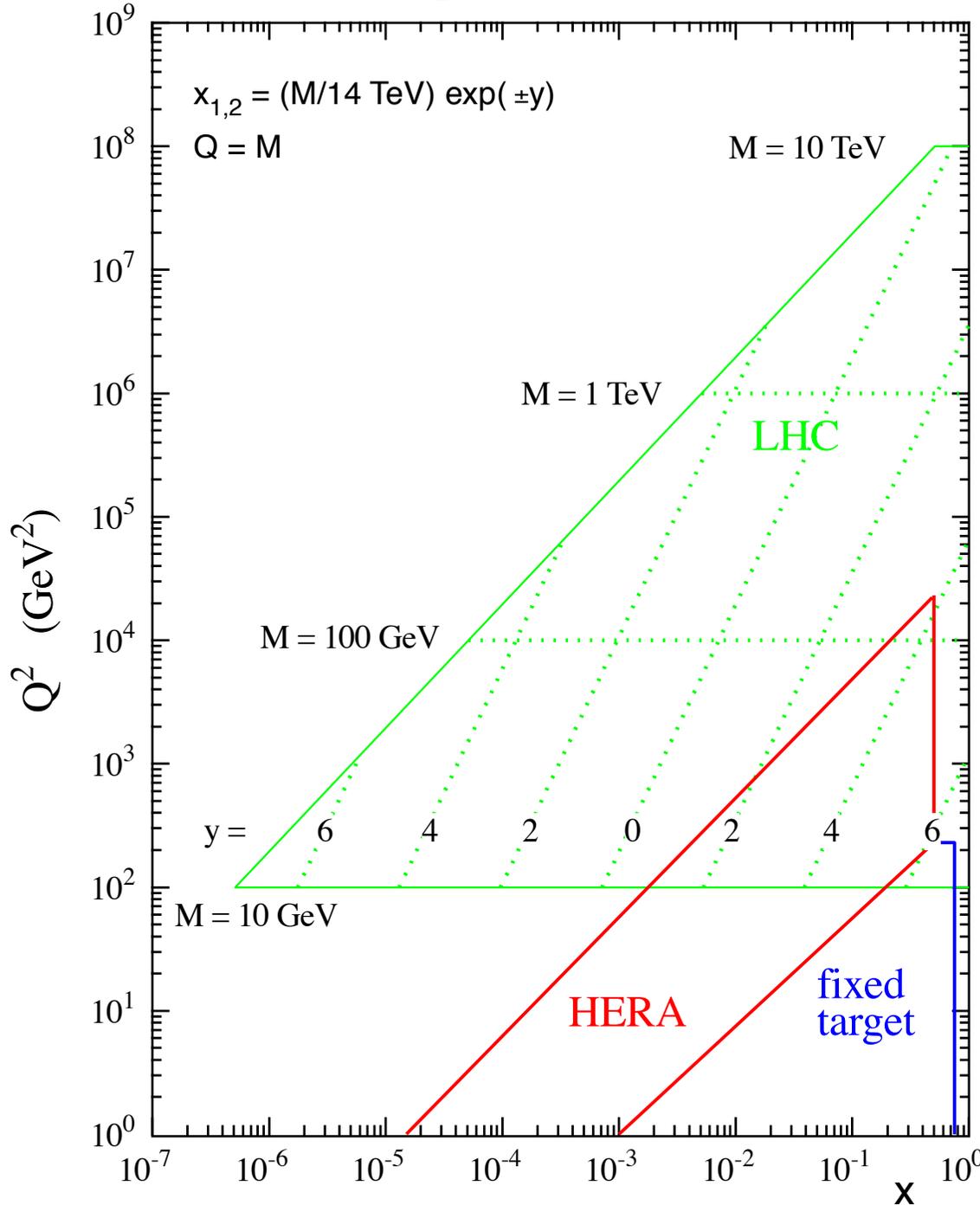
# Parton Densities @ LHC

What do we need?

How well do we know them?

How to improve?

# LHC parton kinematics



$$M^2 = x_1 x_2 s$$

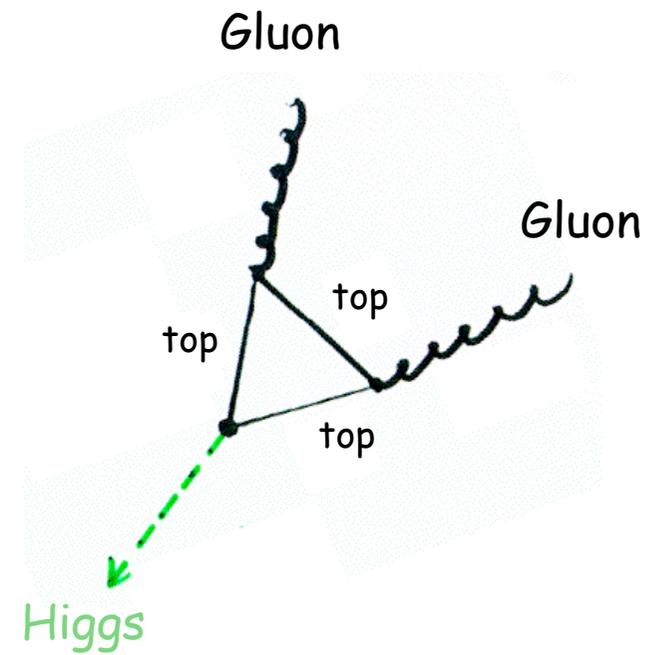
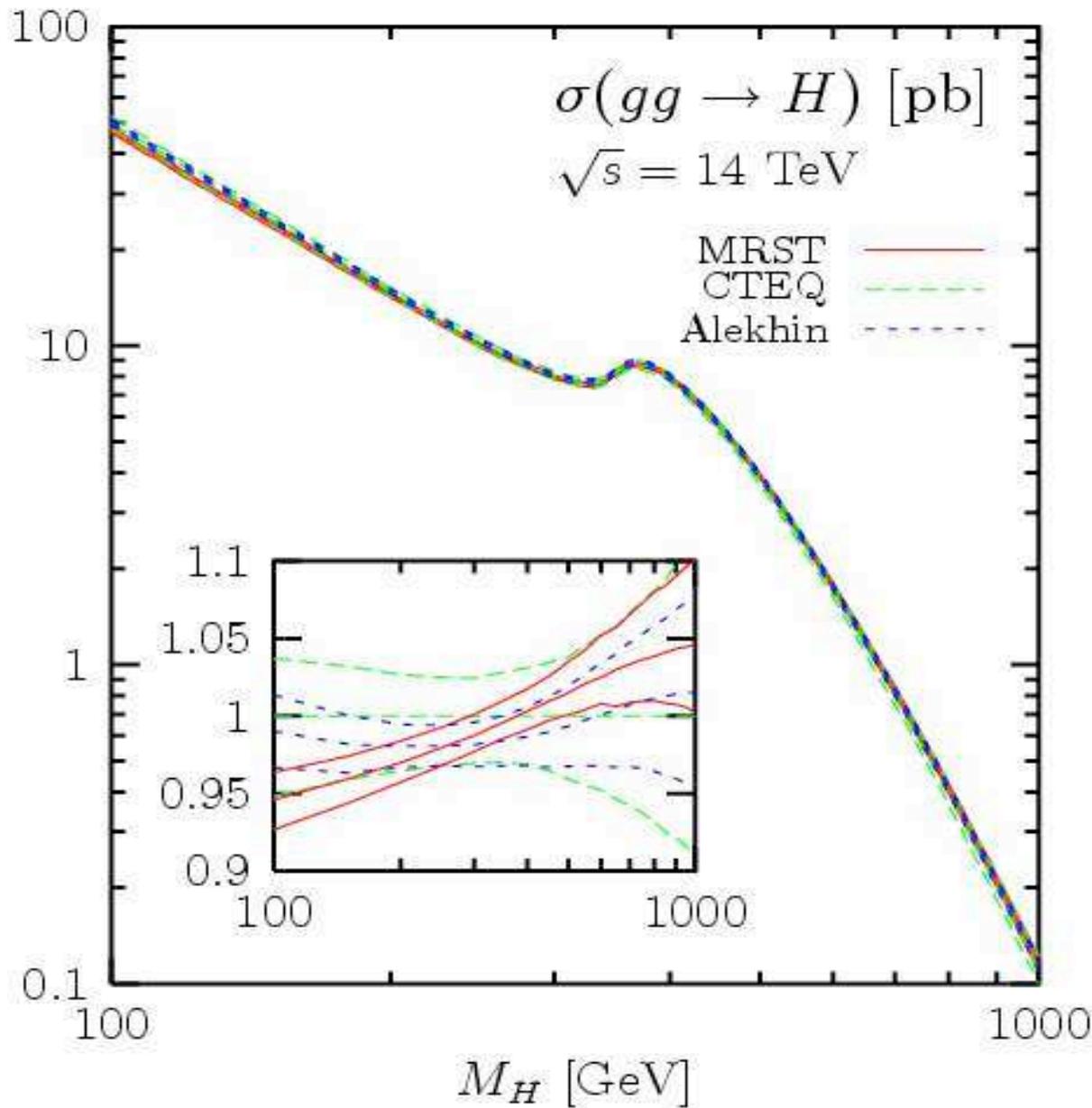
i.e. to produce a particle with mass  $M$  at LHC energies ( $\sqrt{s} = 14 \text{ TeV}$ )

$$\langle x \rangle = \sqrt{x_1 x_2} = M/\sqrt{s}$$

[ $x_1 = x_2$ : mid-rapidity]

## LHC needs:

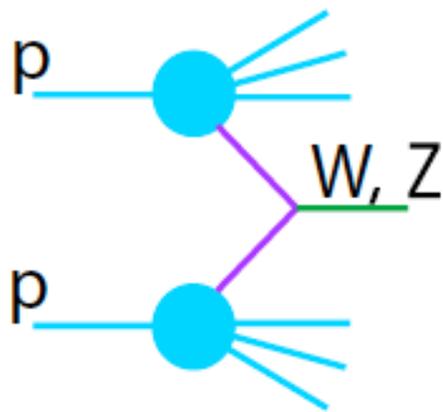
- knowledge on parton densities
- extrapolation over orders of magnitude



Simple spread of existing PDFs  
 gives a 5-10% uncertainty on  
 the Higgs cross section.

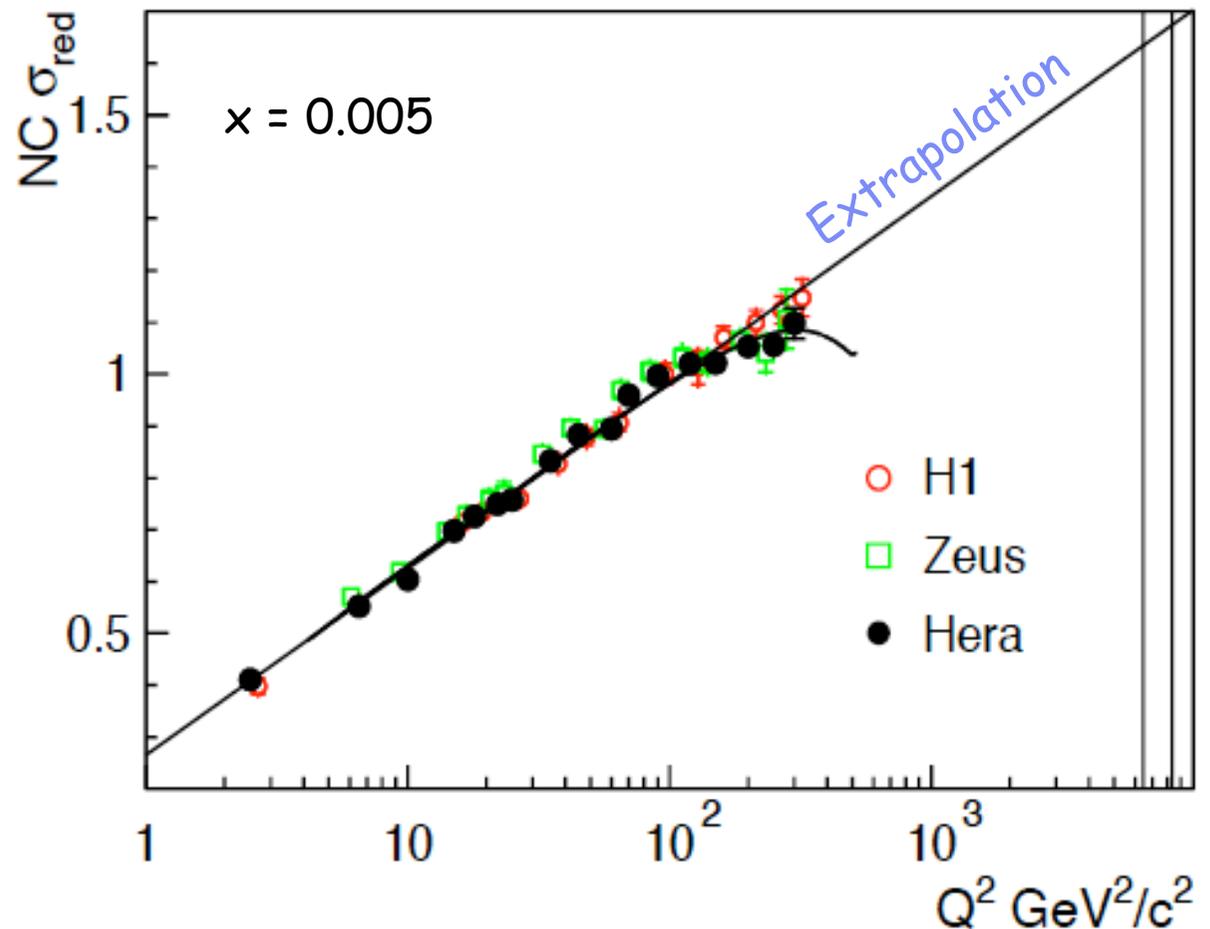
# W and Z Production @ LHC

$Q^2$  for W/Z production  
@ LHC energies



$$pp \rightarrow W + X$$

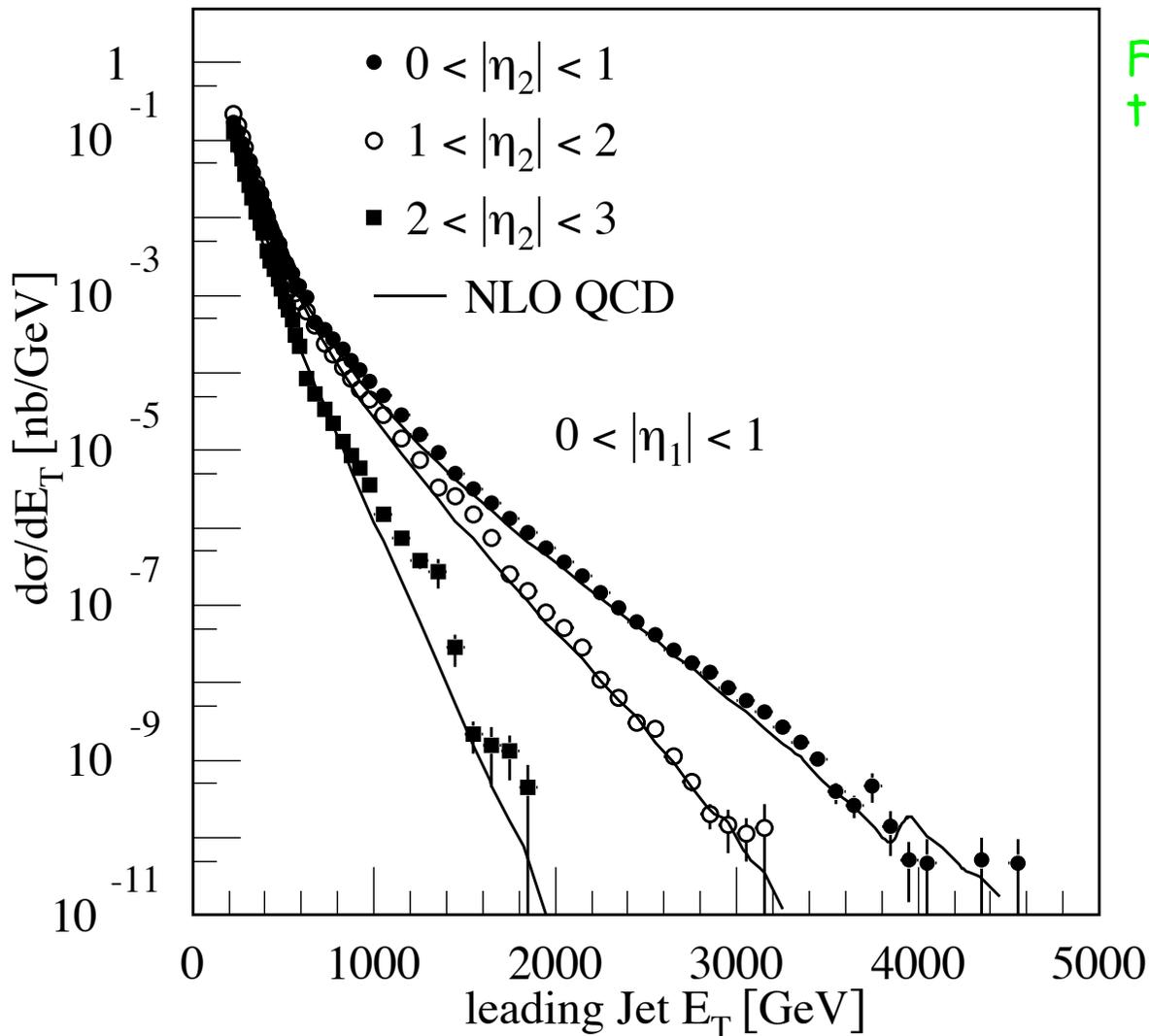
$$pp \rightarrow Z + X$$



Considered  
as luminosity monitor

# Jet Spectrum @ LHC

ATLAS TDR: Inclusive Jet  $E_T$

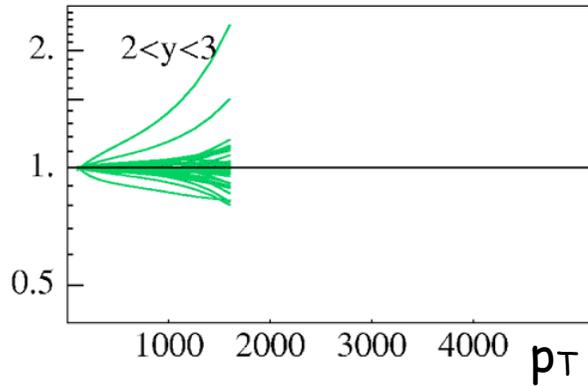
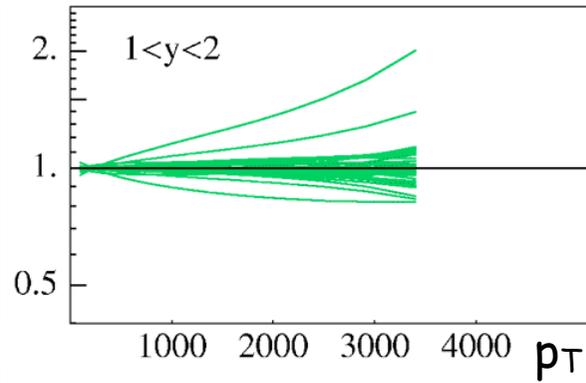
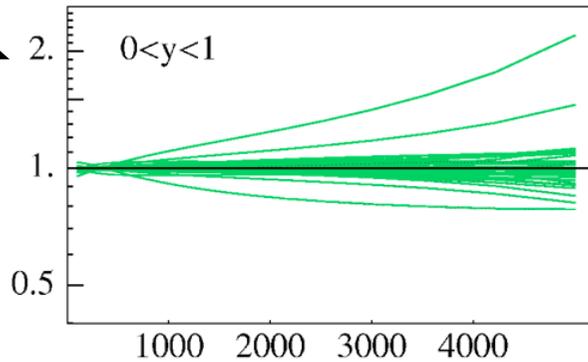


First plot  
to be made at LHC

Sensitive to:

- Parton distribution functions
- Detector performance  
[Energy scale and resolution]
- New Physics

# Relative Uncertainty [compared to CTEQ 6.1M]

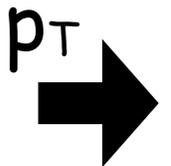
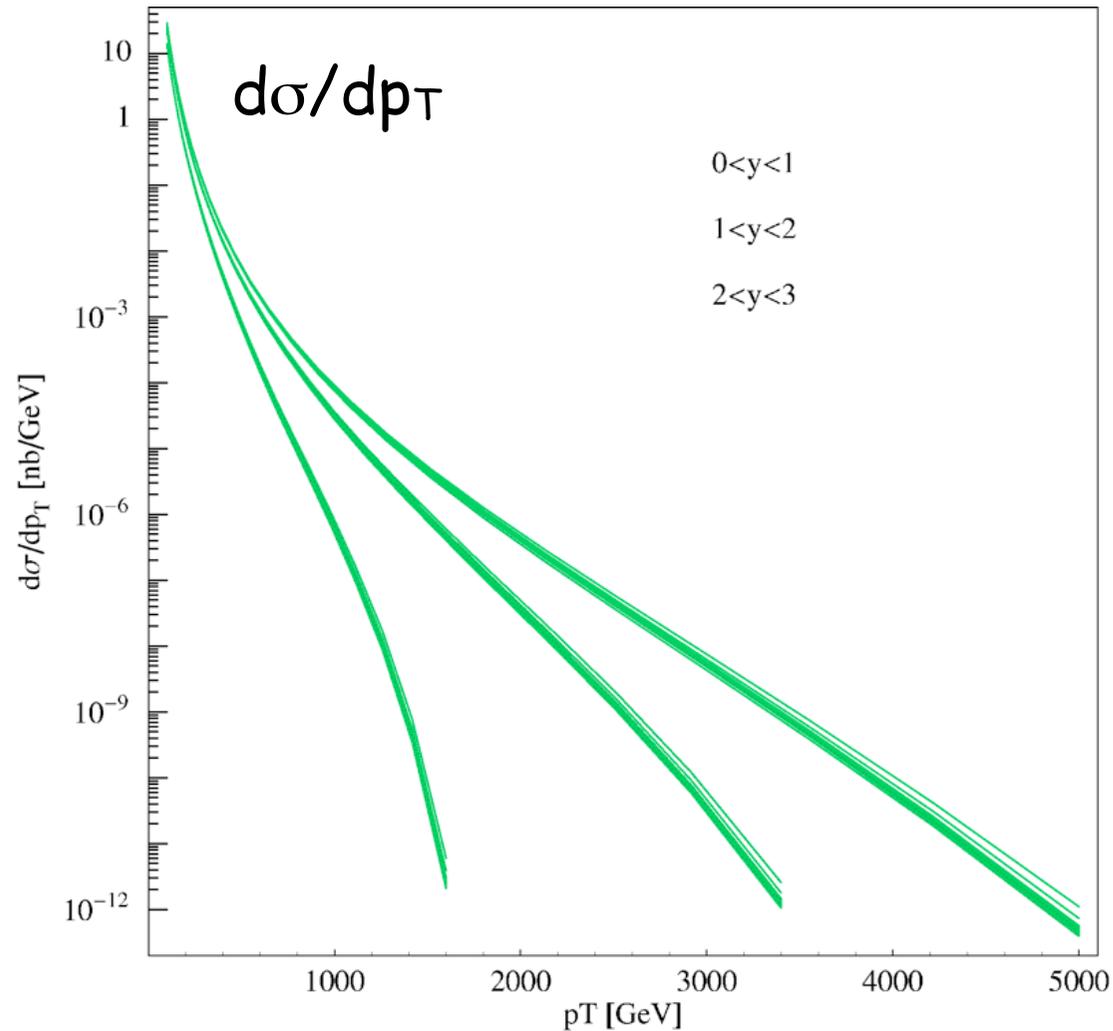


## Inclusive Jet Cross Section @ LHC

[D.Stump et al., JHEP 10 (2003) 046]

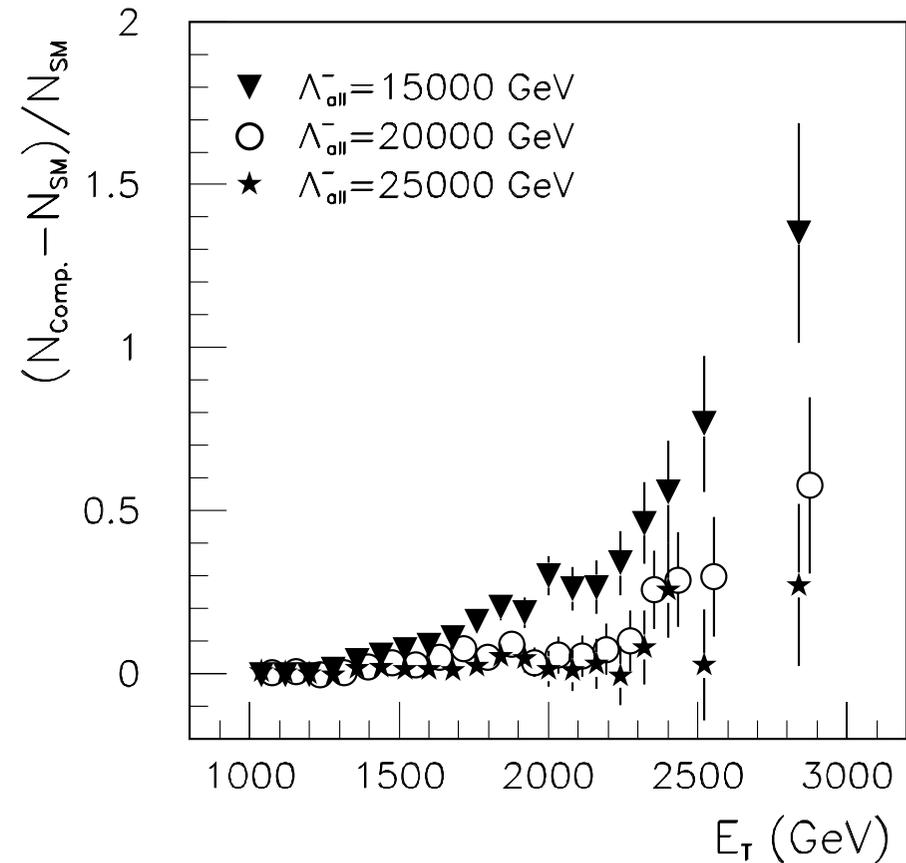
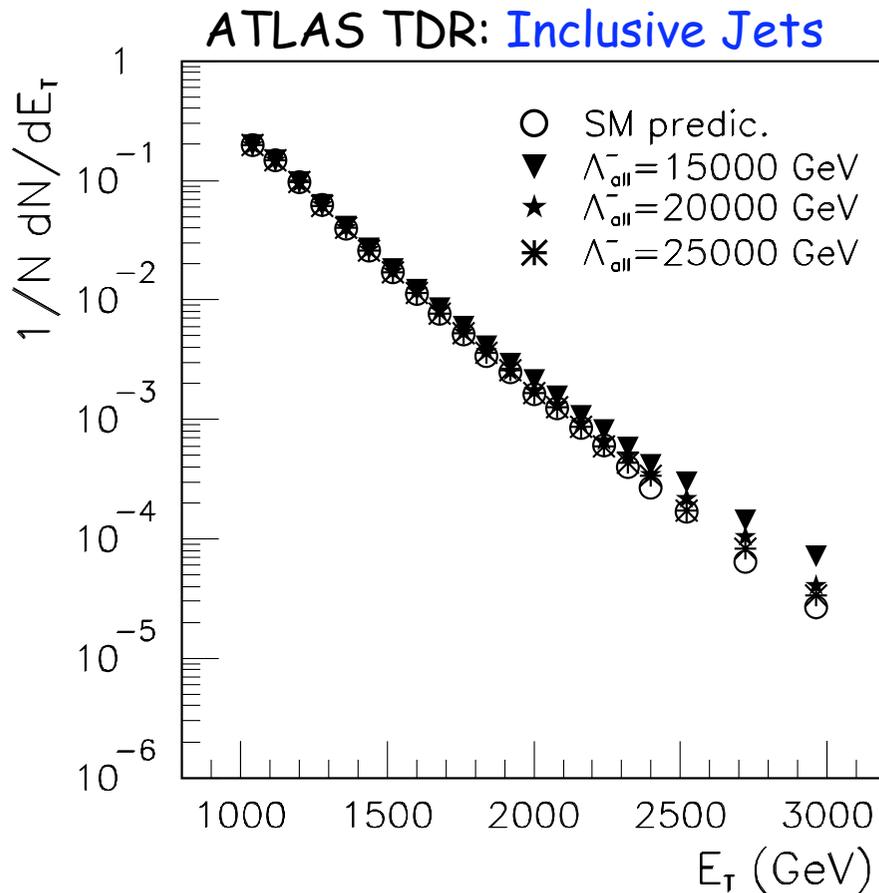
Mid-rapidity:  
100 % uncertainty  
@  $E_T \sim 5$  TeV

Forw. jets:  
100 % uncertainty  
@  $E_T \sim 2$  TeV

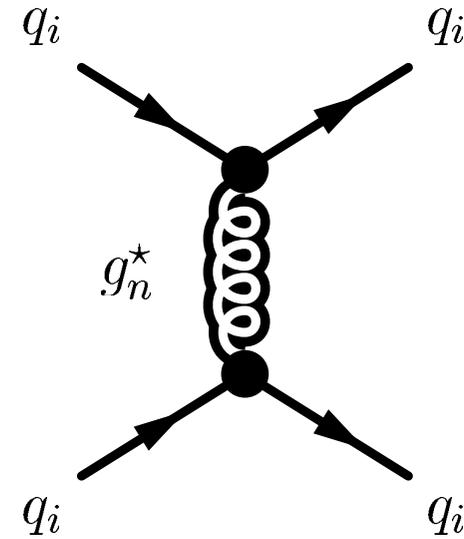
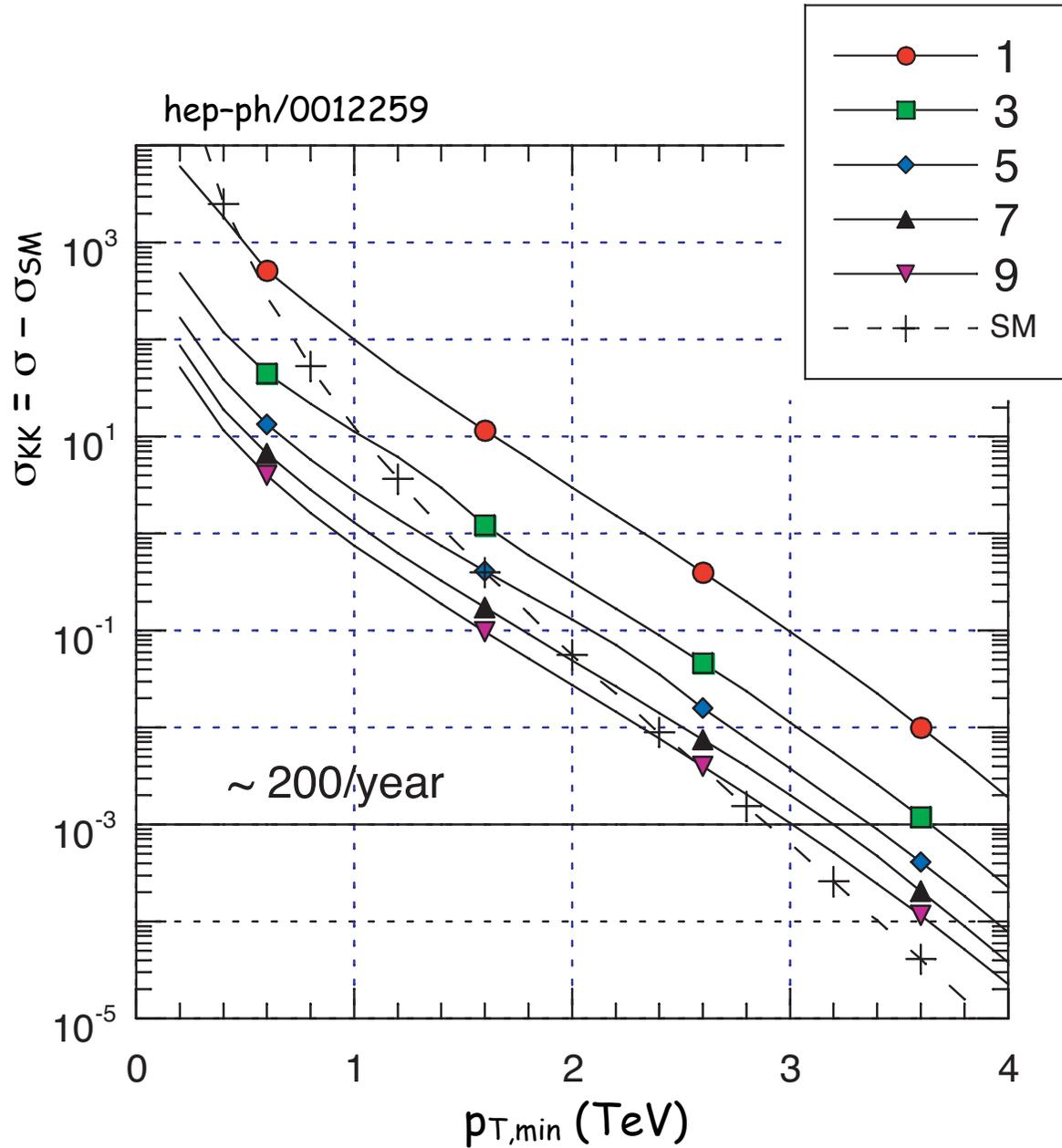


# Quark Substructure [Compositeness]

Expectation: Enhancement of  $\sigma_{jet}$  at high  $E_T$

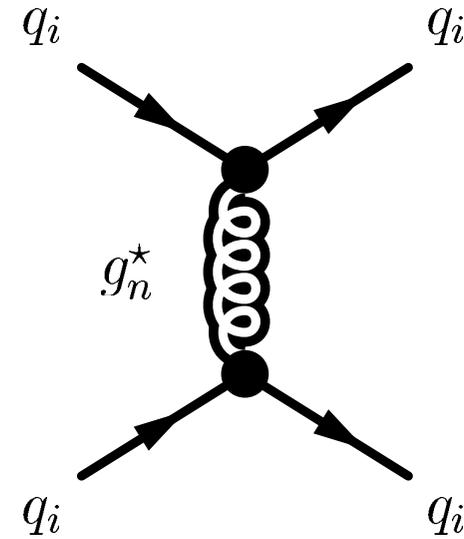
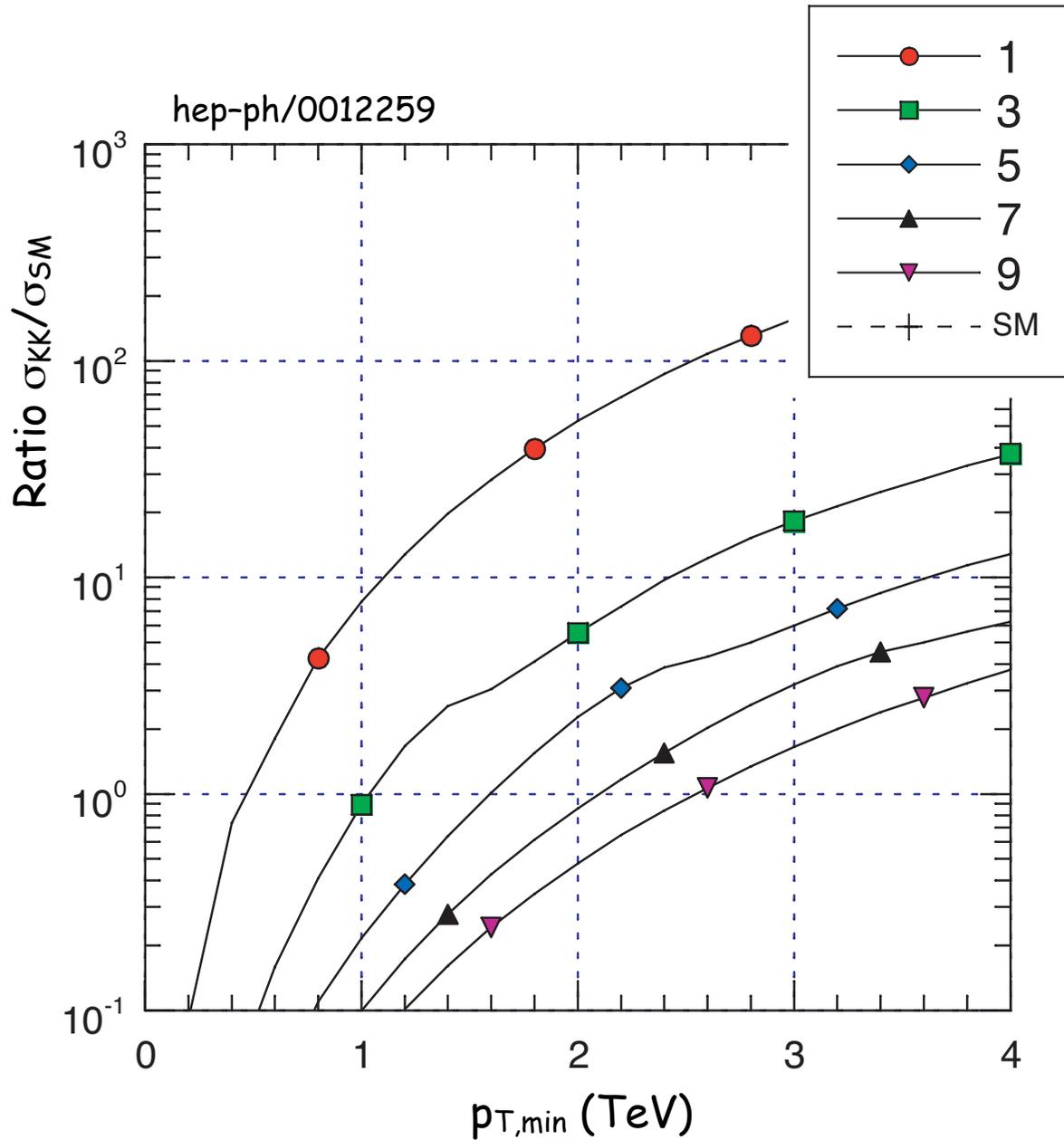


# Heavy Gluons [Extra Dimensions]



Heavy Gluons:  
Kaluza Klein Excitations  
of normal gluon  
Mass of  $g^*$ :  
Scale of Extra Dimension

# Heavy Gluons [Extra Dimensions]



Heavy Gluons:  
Kaluza Klein Excitations  
of normal gluon  
Mass of  $g^*$ :  
Scale of Extra Dimension

# HERA Parton Distributions

Present Precision

Future Perspectives

# Where HERA Data constrain PDFs

---

Valence Quarks:

High  $Q^2$ , high  $x$

HERA II

NC/CC ep cross section

[HERA I: statistics limited]

Sea Quarks:

Low- $x$ : inclusive NC DIS

[HERA I 2000 data to be published]

Gluon:

Low- $x$ : scaling violations

Mid- $x$ : jet data

heavy flavours

High- $x$ : momentum sum rules

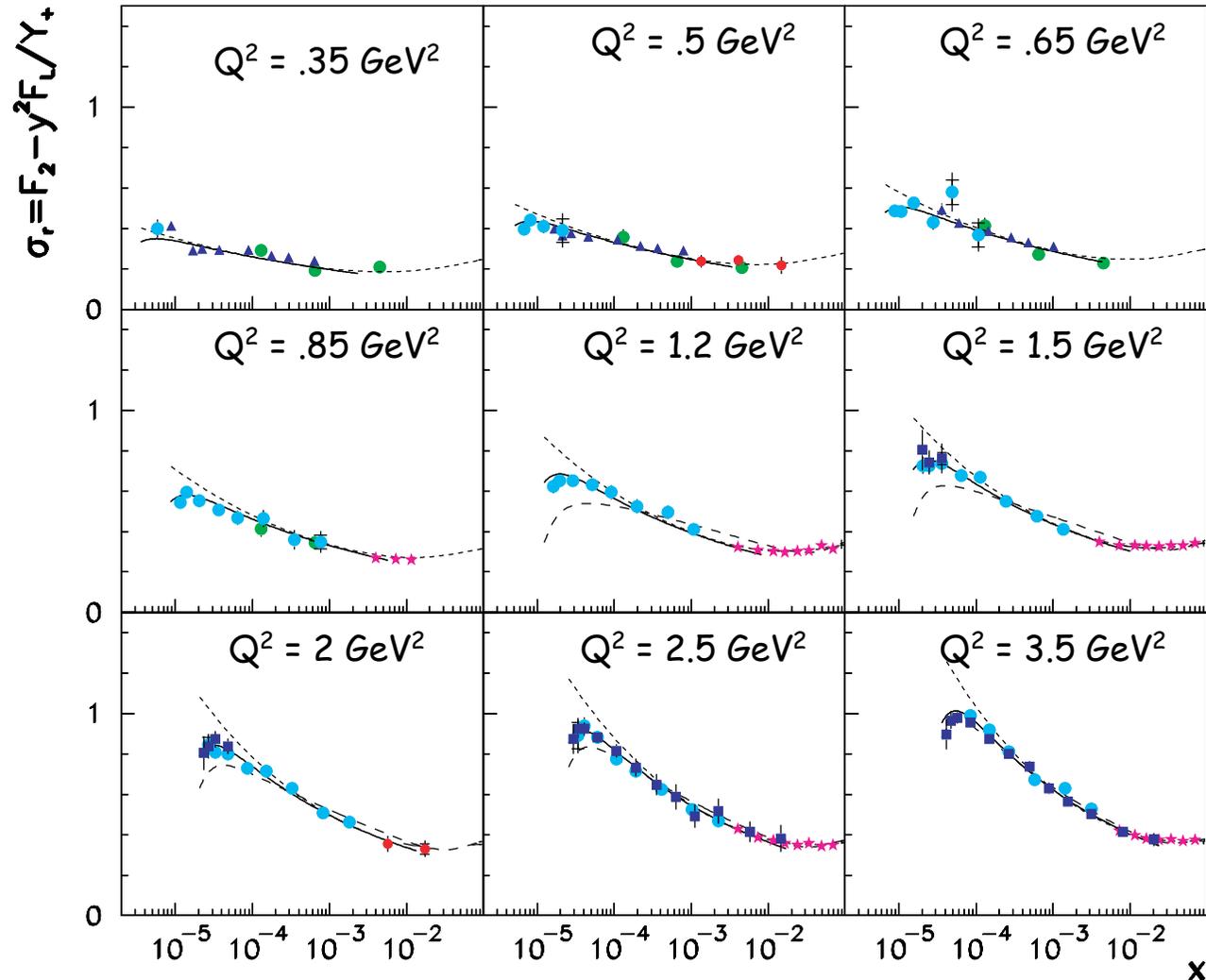
[HERA I statistics limited at high  $E_T$ ]

[HERA II: jets, heavy flavours]

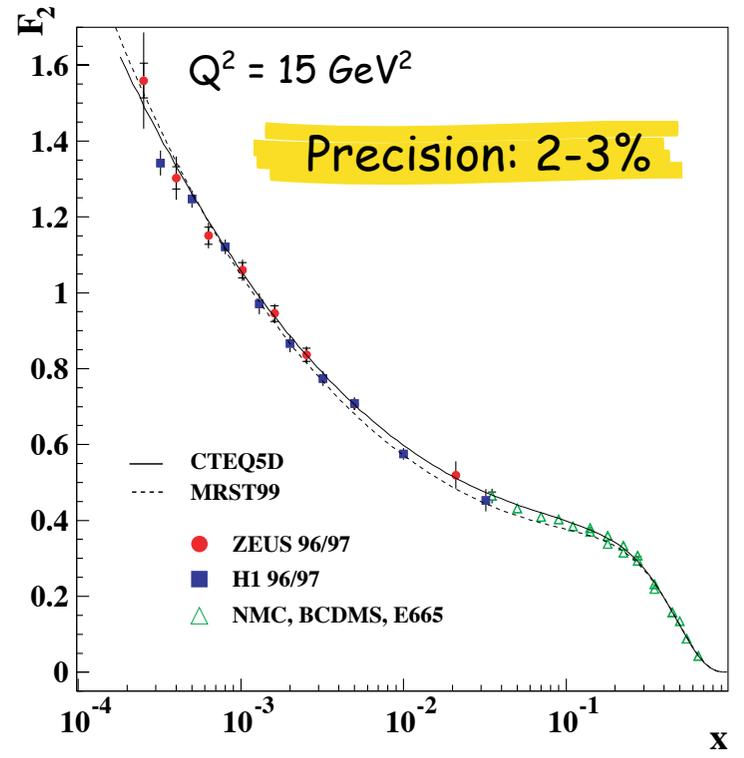
HERA II

# New H1 Low- $Q^2$ Results

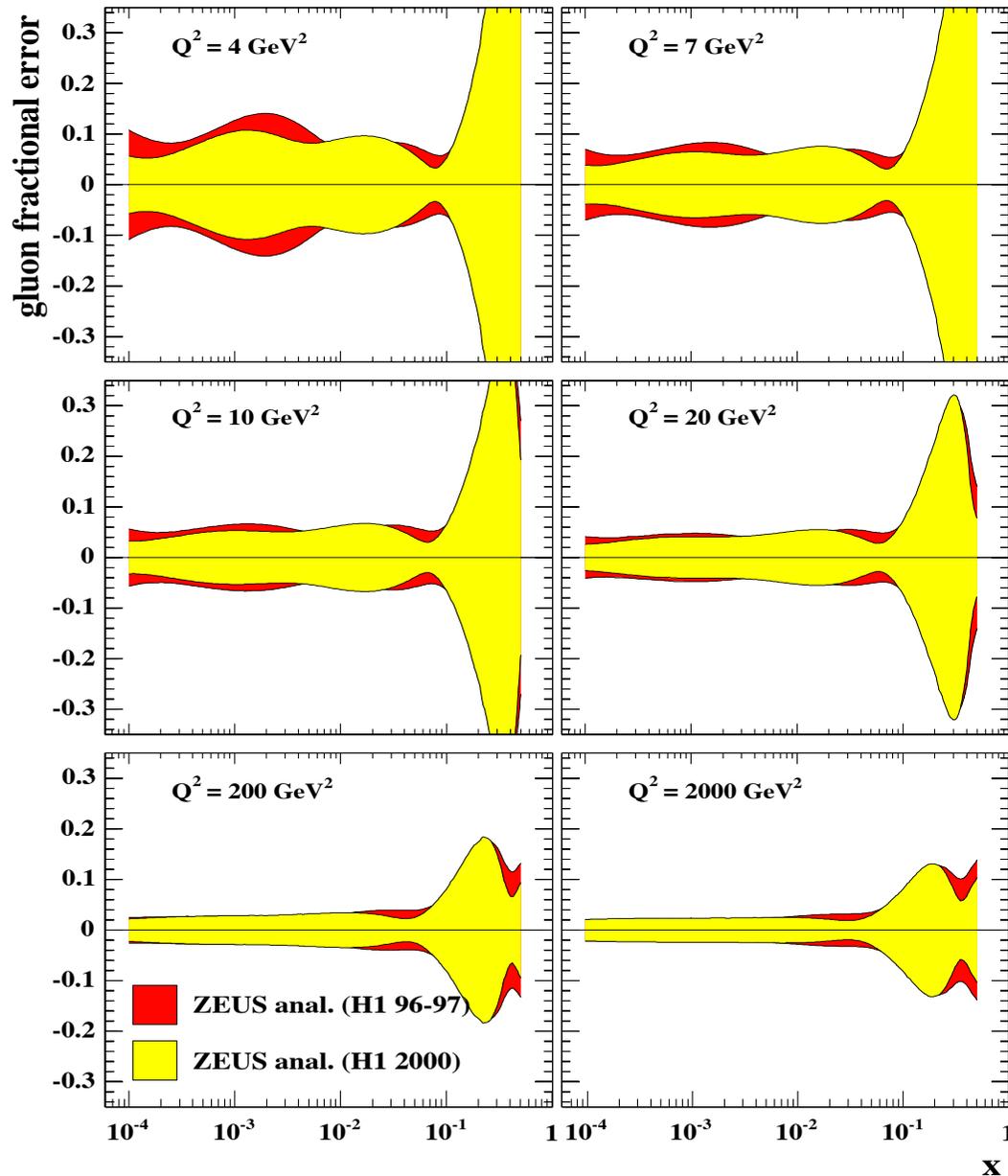
- H1 svtx00 ISR prel.
- ▲ ZEUS BPT97
- ★ NMC
- H1 QEDC97
- H1 svtx00 prel.
- H1 99 prel.
- Fractal fit  $F_2$  and dipol  $F_L$
- ⋯⋯ ALLM 97
- - - H1 QCD fit 97
- $Q^2_{\min} = 3.5 \text{ GeV}^2$



Precision of 2-3%  
down to  $Q^2 = 0.35$



# Impact of 'New' HERA low- $Q^2$ data



ZEUS Fit to H1 Data

- High  $Q^2$  NC/CC Data 94-00  
Low  $Q^2$  NC 94-97 (published)
- High  $Q^2$  NC/CC Data 94-00  
Low  $Q^2$  NC 2000 (estimate)

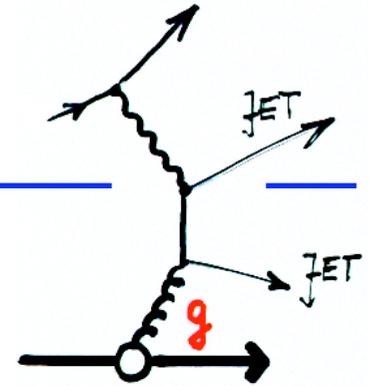
- improved knowledge of gluon at low  $x$  and low  $Q^2$
- some reduction also at higher  $x$

C.Gwenlan

[HERA/LHC Workshop]

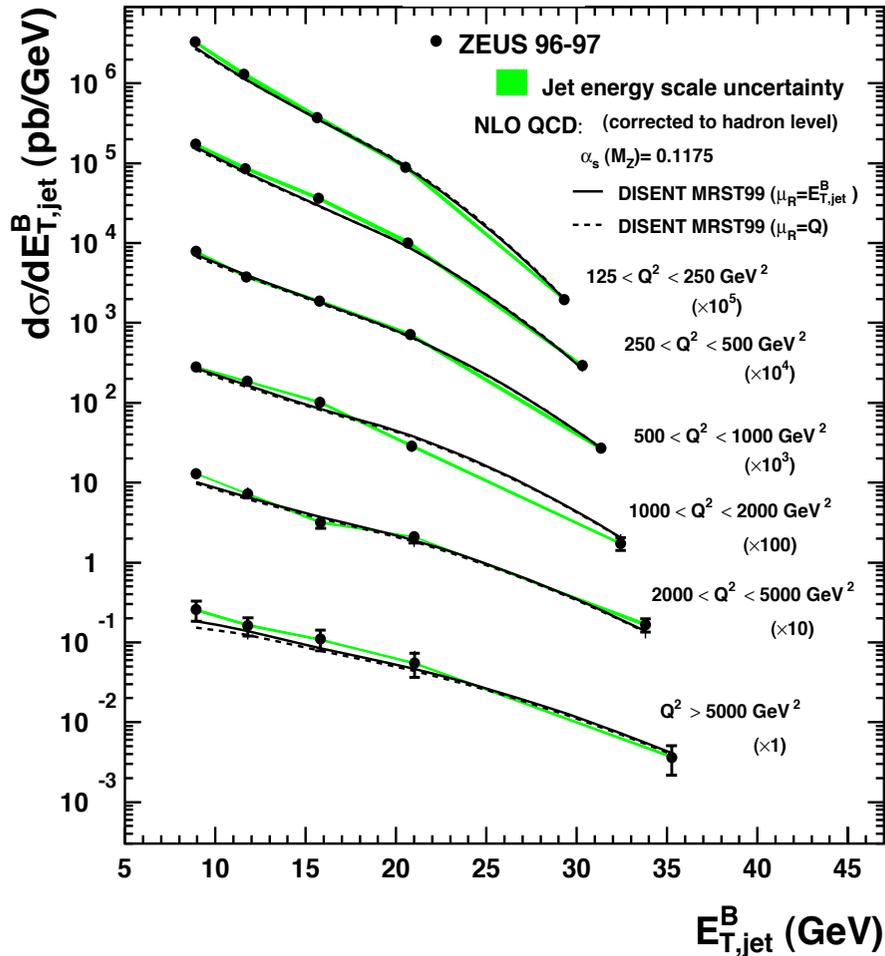
"only"  
**Moderate impact on  $xg(x)$**   
 from extra precision on low  $Q^2$  data

# Jet Data

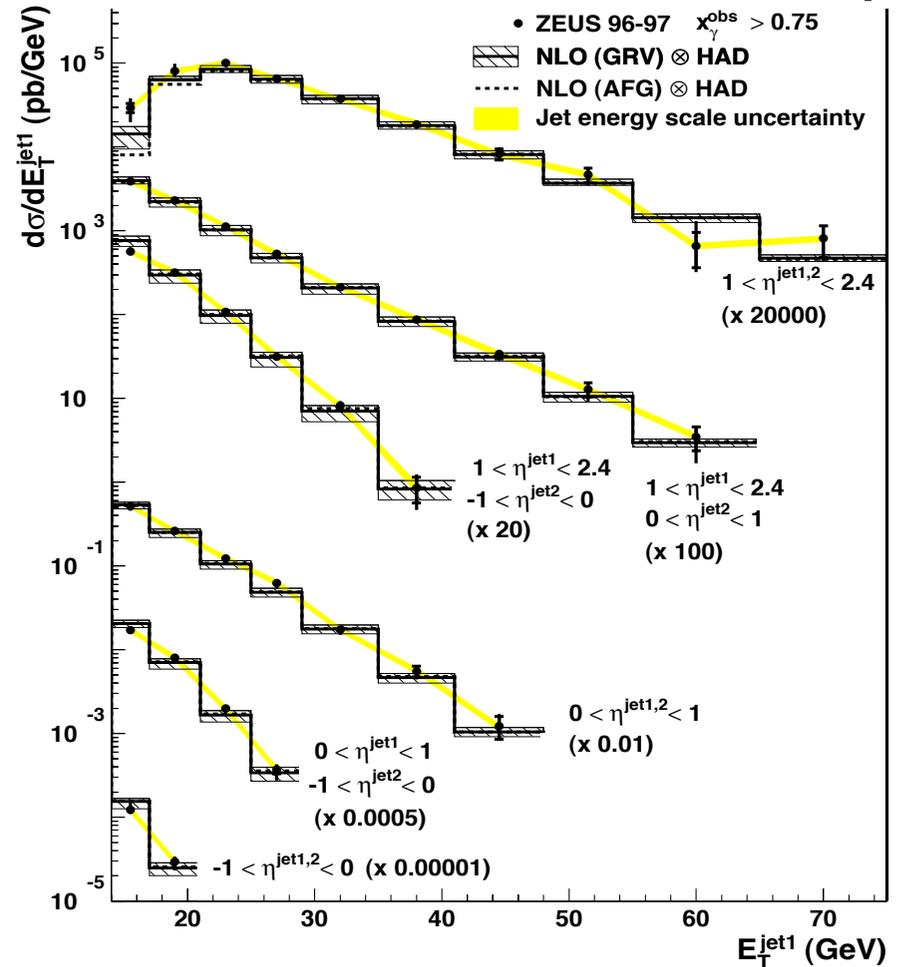


Examples: HERA-I high  $E_T$  jet measurements  
in DIS and Photoproduction ( $Q^2 \sim 0$ )

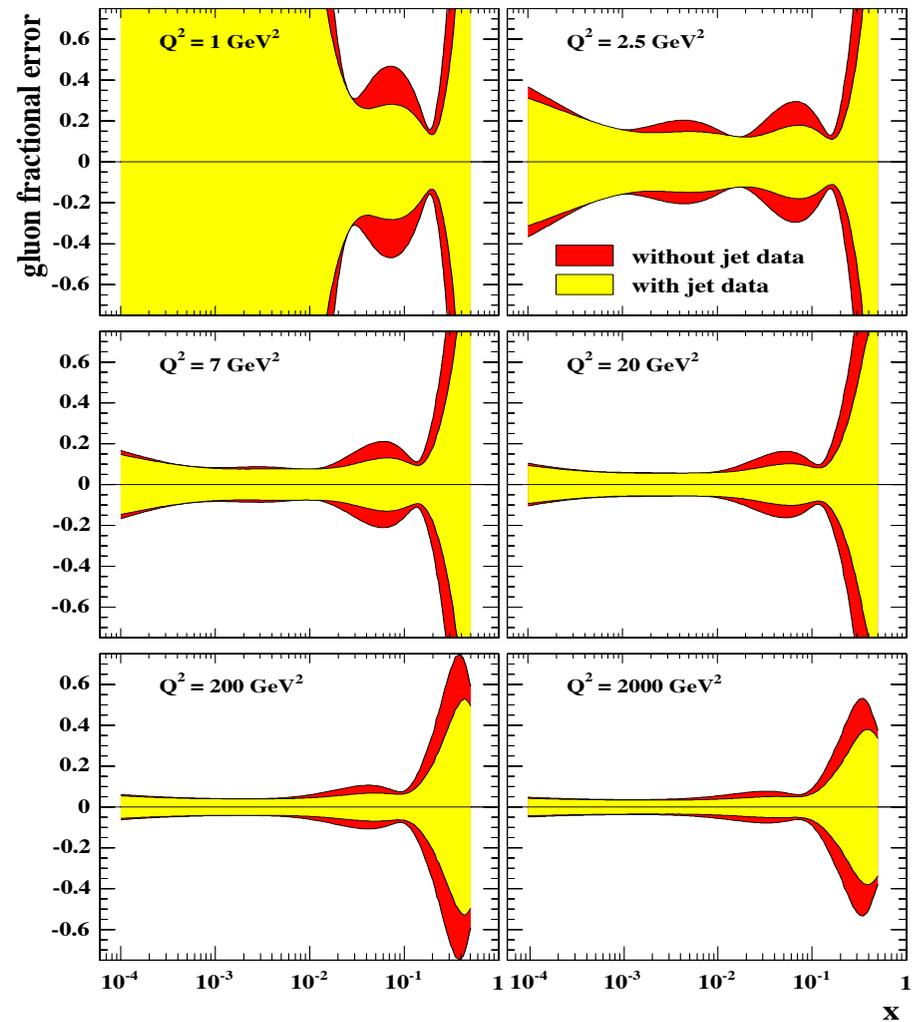
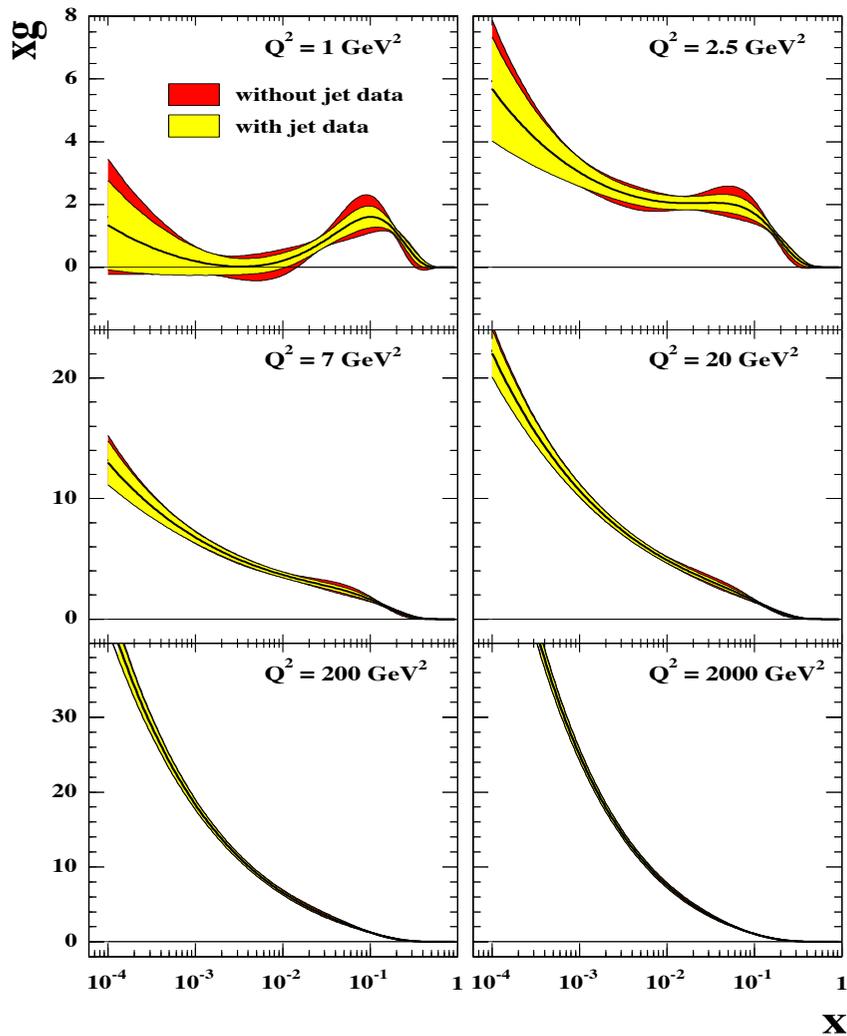
## HERA-I: ZEUS inclusive jets in DIS



## HERA-I: ZEUS two-jet $\gamma p$ at high- $E_T$

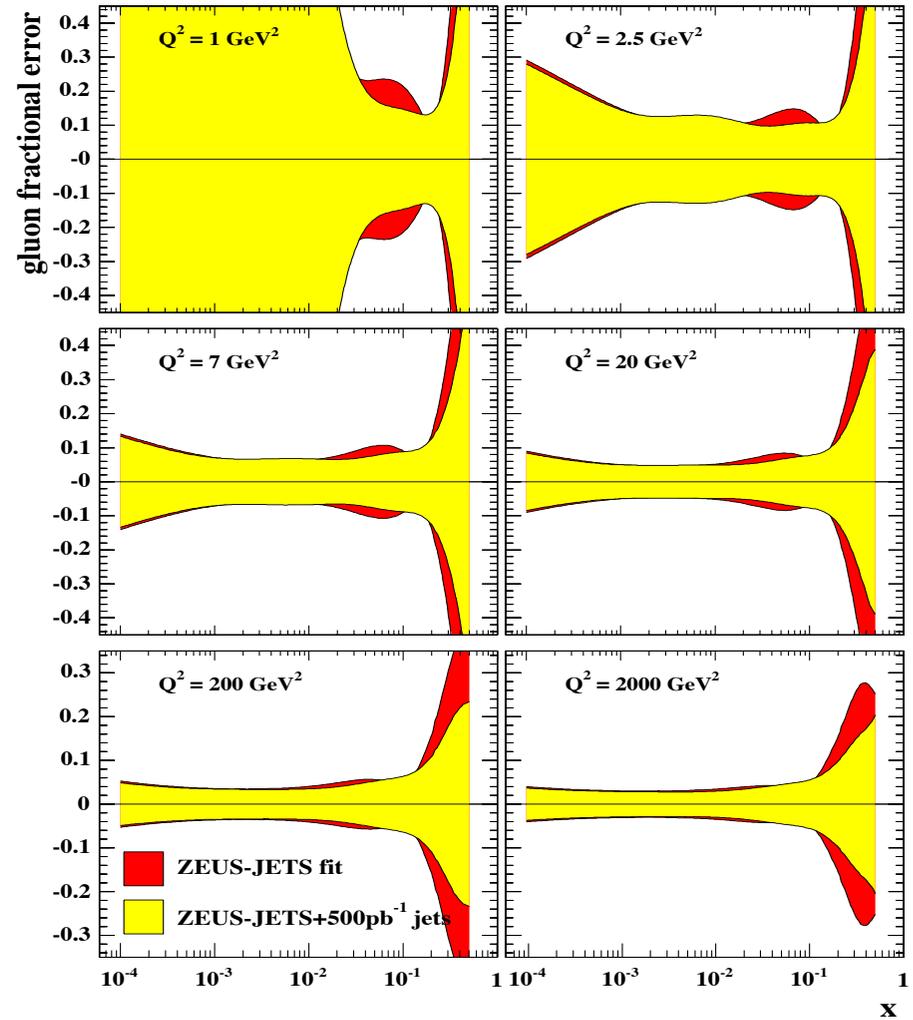
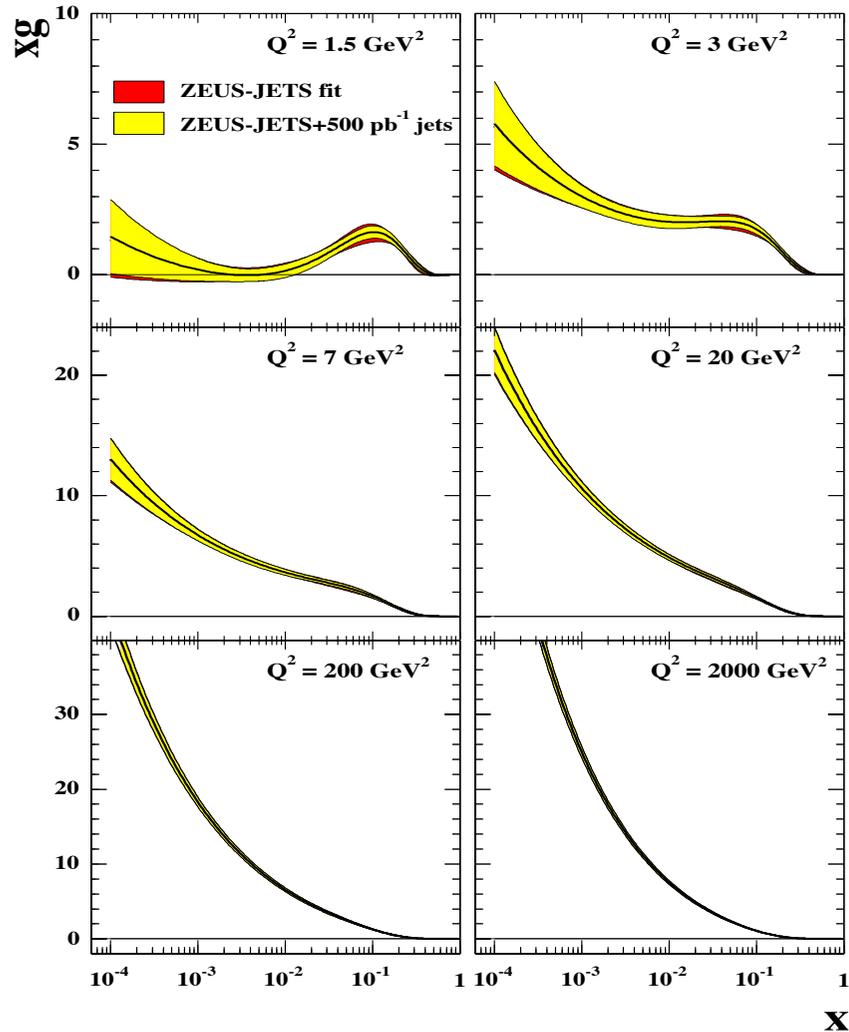


# Impact of Jet Data on Gluon PDF



Clear improvement of  $xg(x)$  at  $x \sim 0.01 - 0.1$

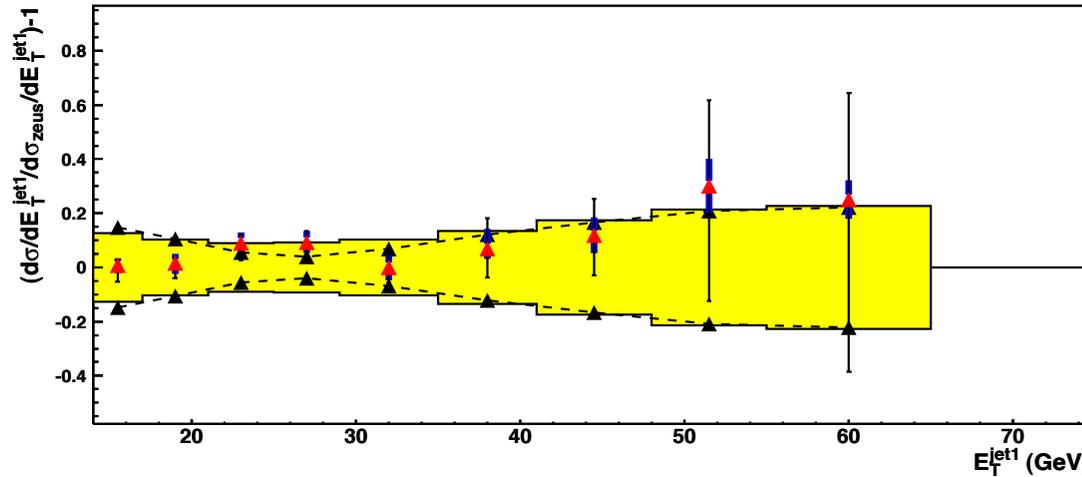
# Impact of 500 pb<sup>-1</sup> Jet Data



Further improvement of  $xg(x)$  at  $x \sim 0.01 - 0.1$

# HERA prospects using jets

## by optimizing selection cuts

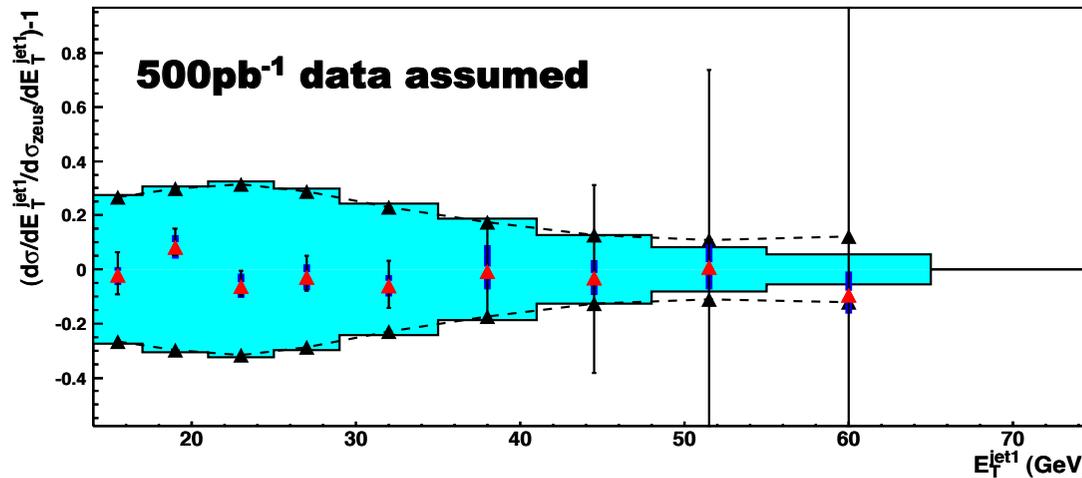


$$E_T^{jet1} > 14 \text{ GeV}, E_T^{jet2} > 11 \text{ GeV}$$

$$x_\gamma > 0.75, 1 < \eta^{jet1} < 2.4, 0 < \eta^{jet2} < 1$$

**Published**

- ▲ All flavors up/down error
- ZEUS gluon up/down error
- ▲ Data+stat+syst errors
- ▲ Data+energy scale uncertainty



**500pb<sup>-1</sup> data assumed**

$$E_T^{jet1} > 15 \text{ GeV}, E_T^{jet2} > 10 \text{ GeV}$$

$$x_\gamma < 0.75, 2 < \eta^{jet1} < 3, 2 < \eta^{jet2} < 3$$

**Optimised**

- ▲ All flavors up/down error
- ZEUS gluon up/down error
- ▲ Data+stat+syst errors (est)
- ▲ Data+energy scale uncertainty (est)

Significant improvement seems possible.

# Impact of HERA II

[case study using current running scenario]

Data sample	L of HERA-I measurement (pb <sup>-1</sup> )	assumed L of HERA-II measurement (pb <sup>-1</sup> )	Central values taken from...	Systematics taken from...
High-Q <sup>2</sup> NC e <sup>+</sup>	63	350	existing data	existing data
High-Q <sup>2</sup> NC e <sup>-</sup>	16	350	existing data	existing data
High-Q <sup>2</sup> CC e <sup>+</sup>	61	350	existing data	existing data
High-Q <sup>2</sup> CC e <sup>-</sup>	16	350	existing data	existing data
Inclusive DIS jets	37	500	existing data	existing data
Dijets in $\gamma p$	37	500	existing data	existing data
Optimised dijets in $\gamma p$	-	500	NLO QCD	NOT INCLUDED

statistically limited data-sets

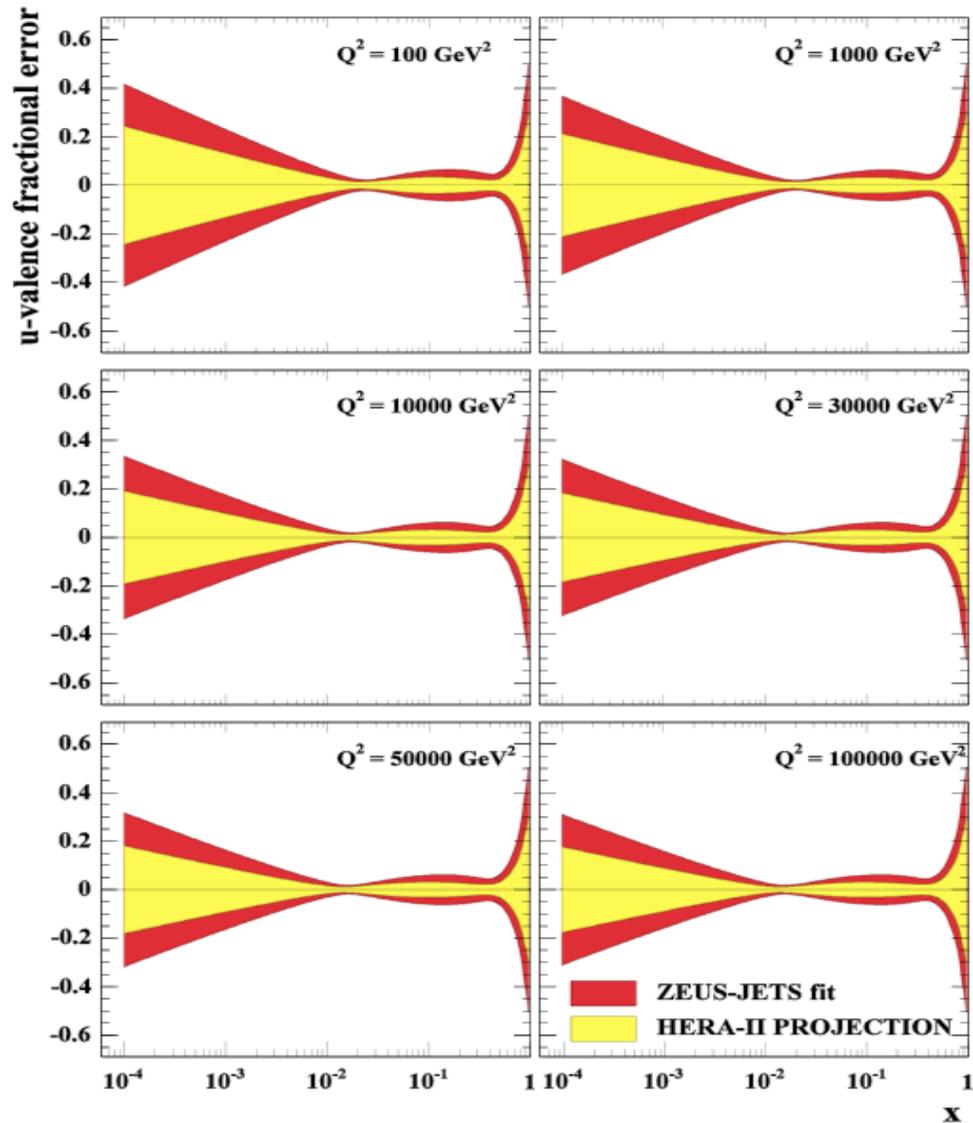
- scale statistical uncertainties on existing data assuming max. 700 pb<sup>-1</sup> (equally between e<sup>+</sup>/e<sup>-</sup>)
- systematic uncertainties taken from existing data

optimised jet cross sections

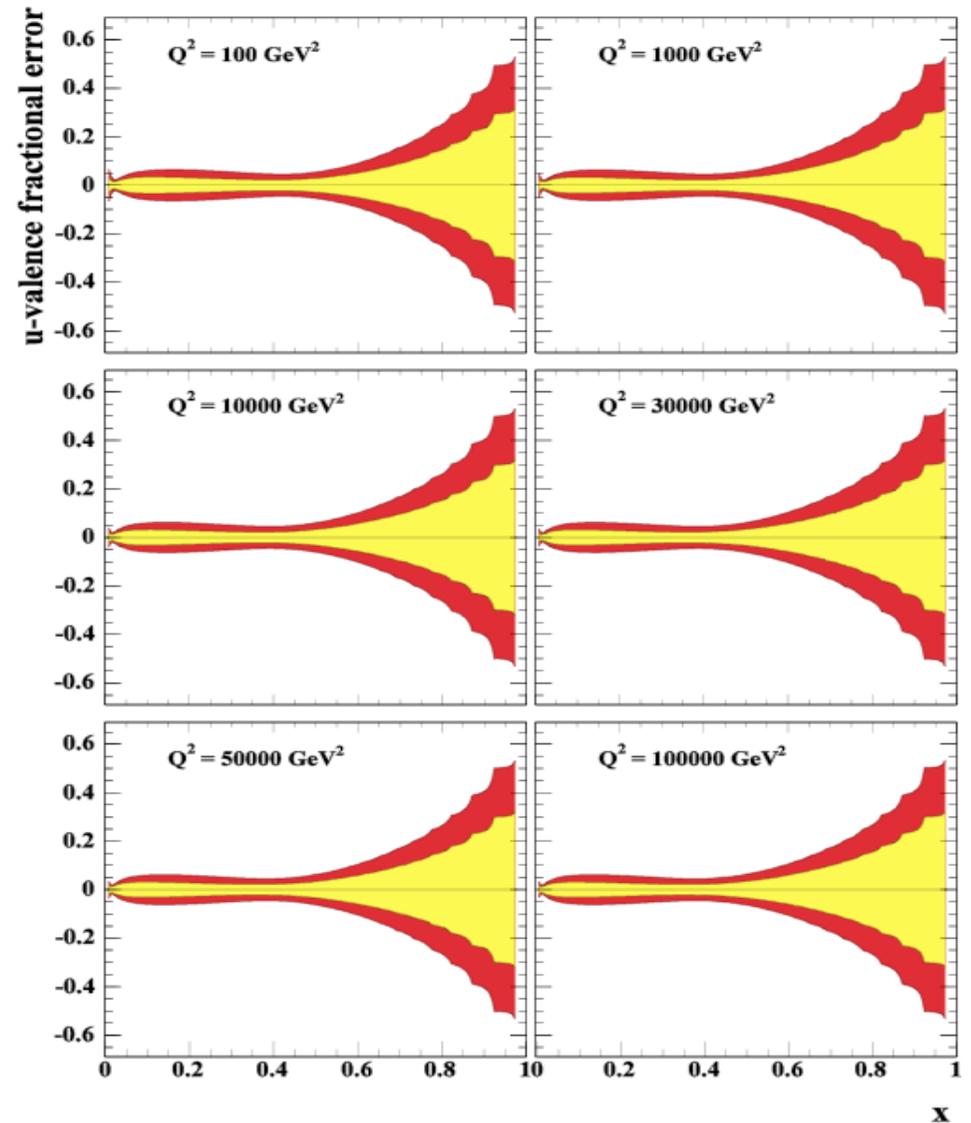
- include simulated data-points from NLO QCD, statistical uncertainties assume 500 pb<sup>-1</sup>
- no systematics included

# u-Valence Uncertainties

log-x scale (low-x region)

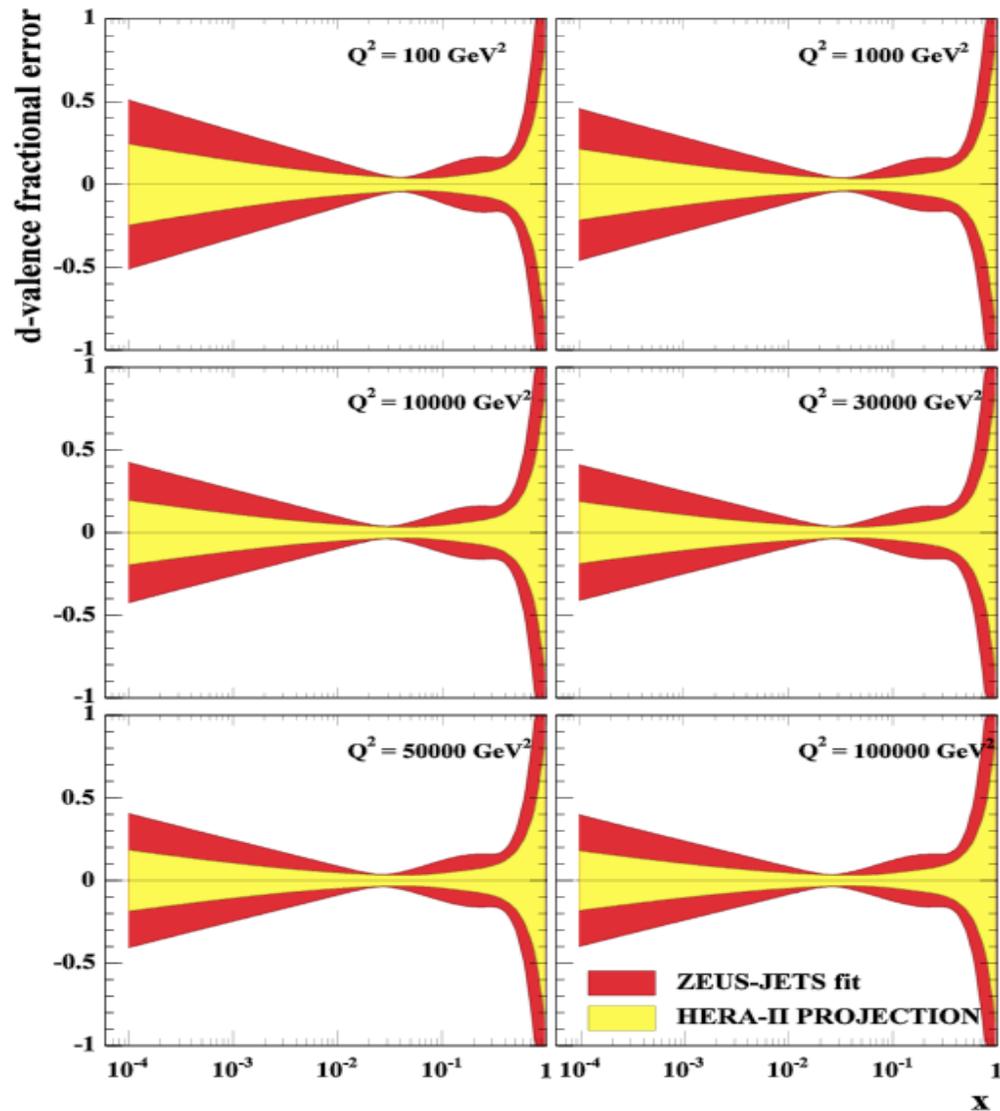


linear-x scale (high-x region)

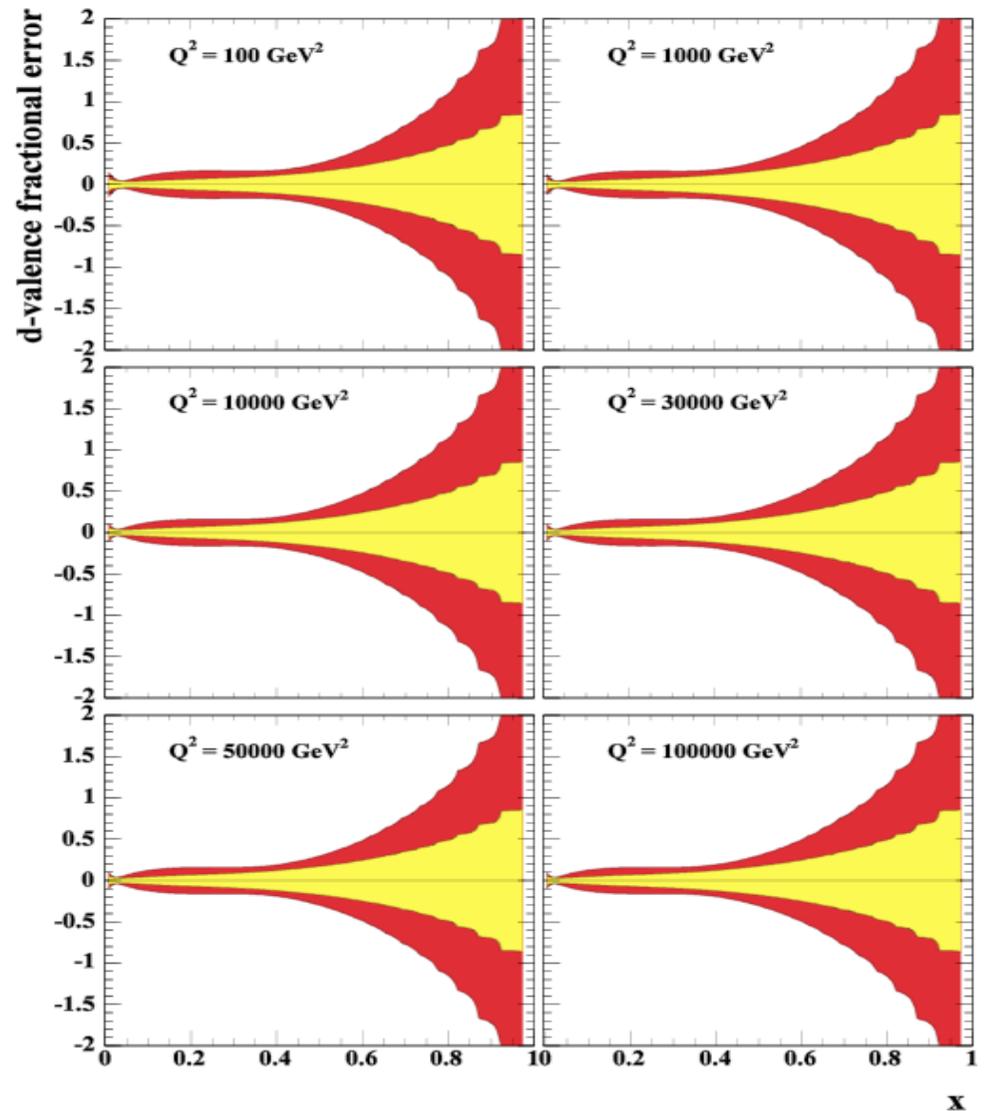


# d-Valence Uncertainties

log-x scale (low-x region)

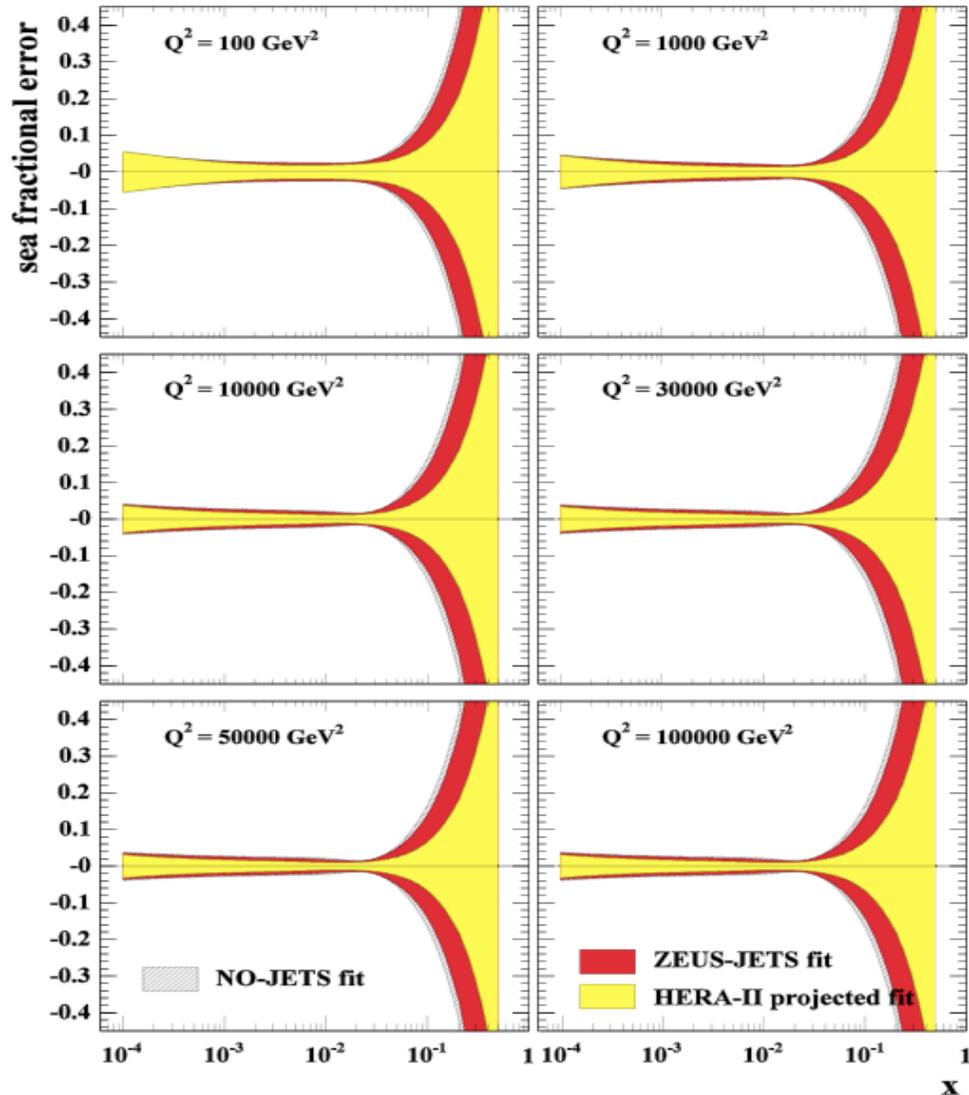


linear-x scale (high-x region)

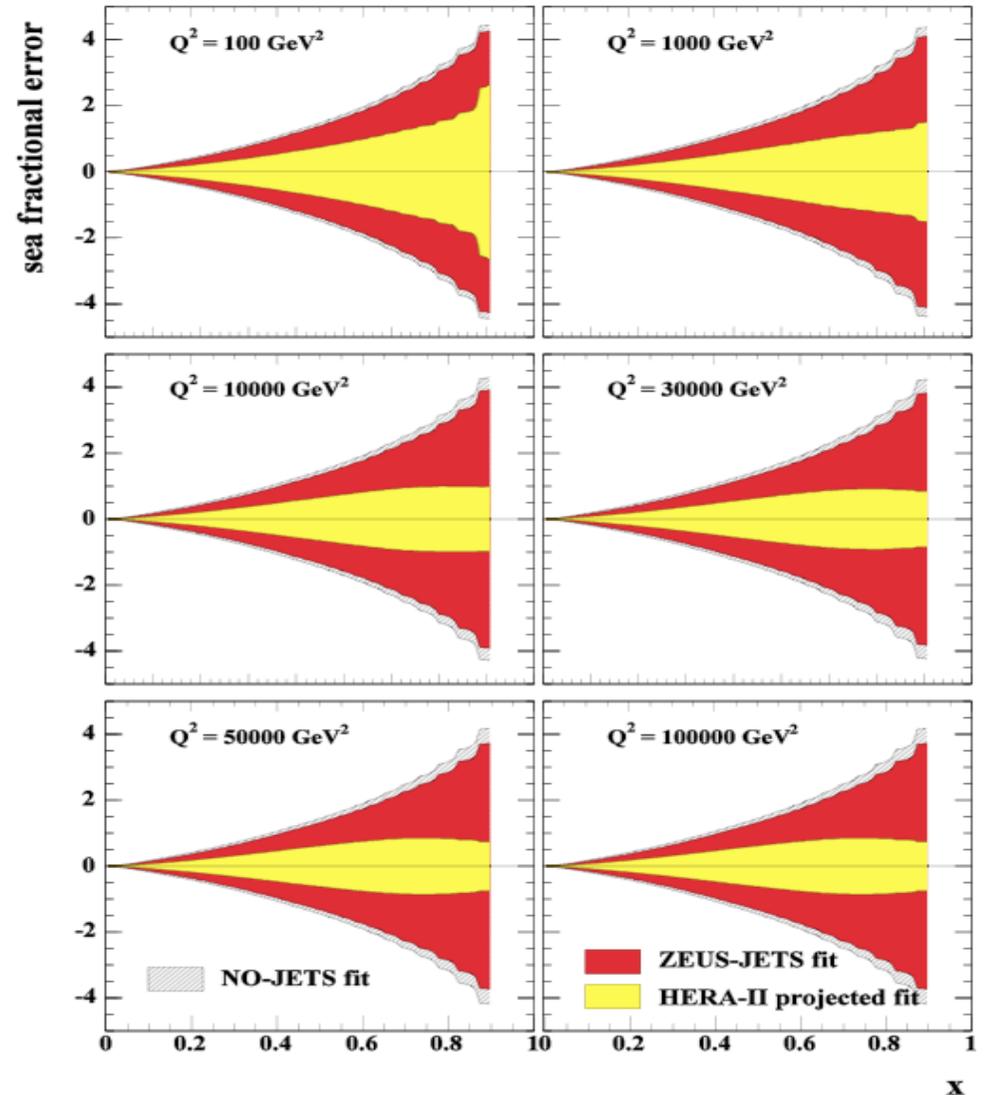


# Sea Quark Uncertainties

log-x scale (low-x region)



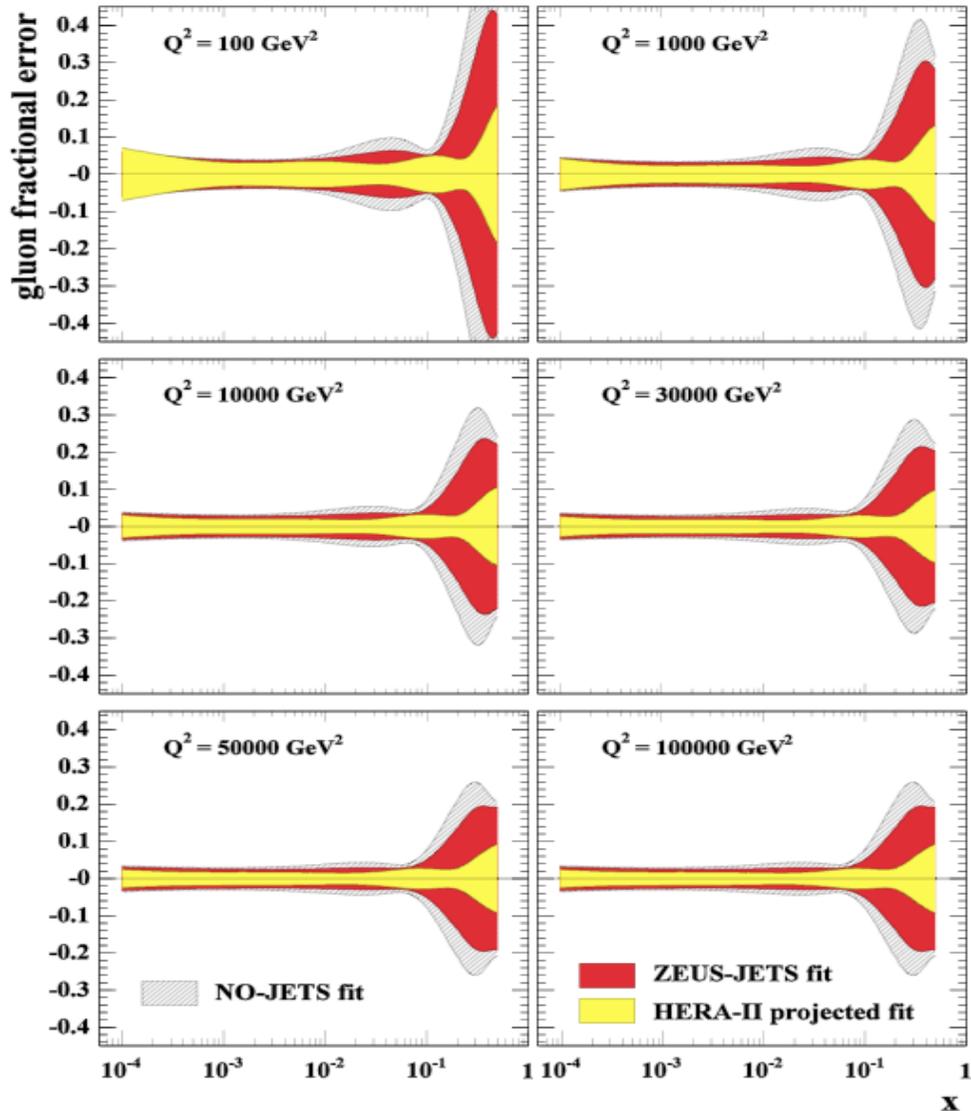
linear-x scale (high-x region)



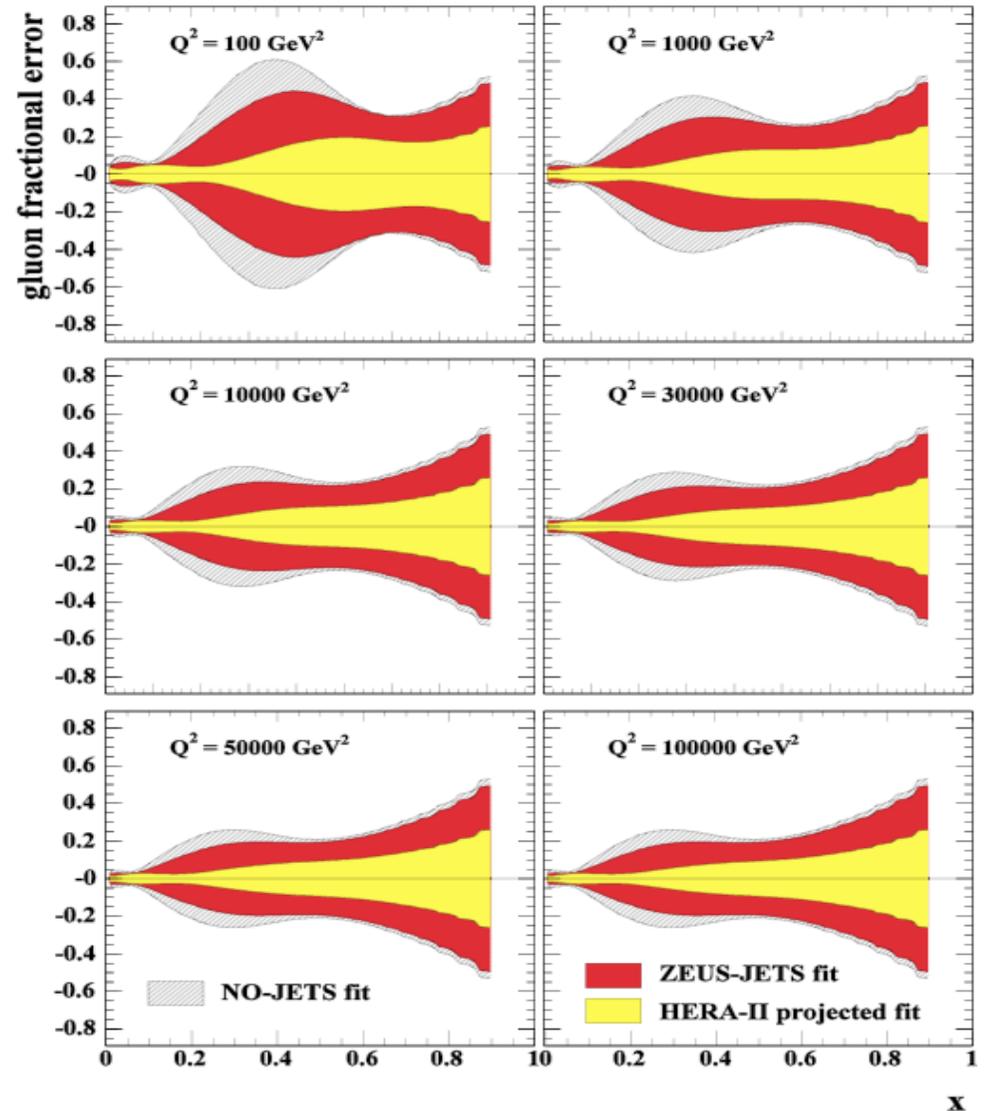
→ most significant improvement from increased statistics at HERA-II

# Gluon Uncertainties

log-x scale (low-x region)



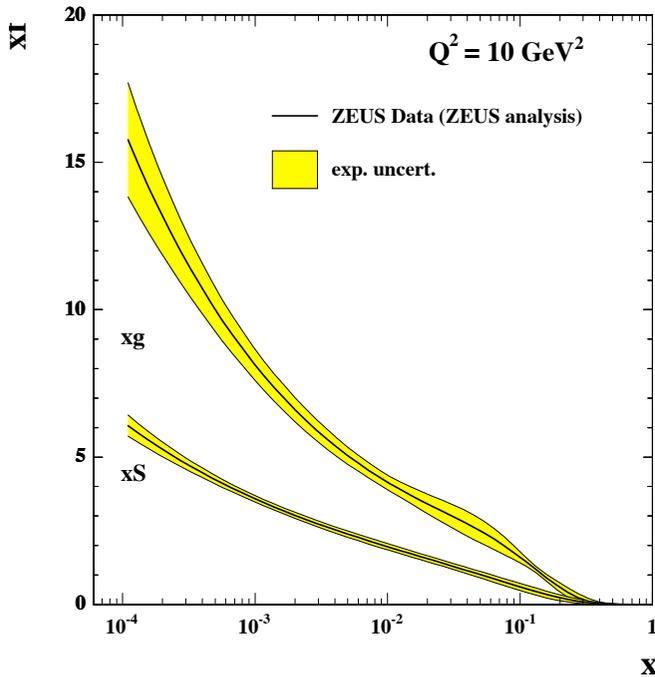
linear-x scale (high-x region)



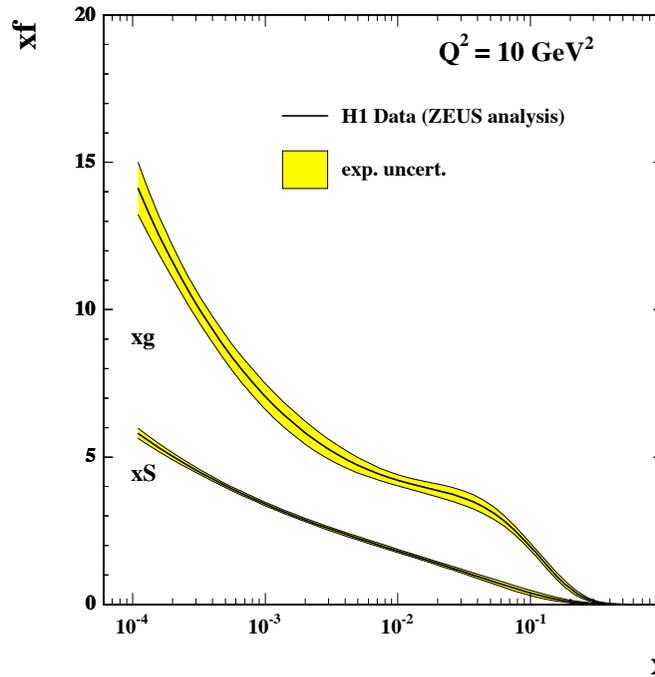
→ most significant improvement from optimized jet analysis

# Caveats

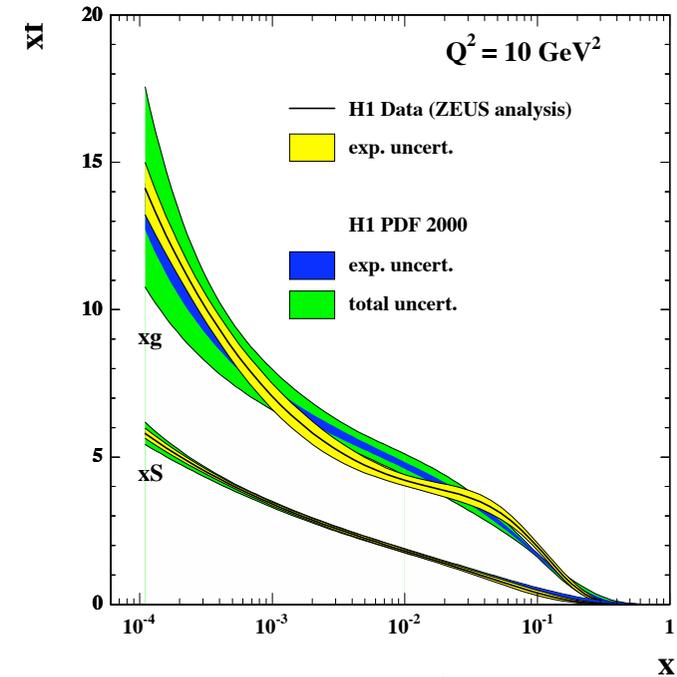
# Comparison of H1 and ZEUS



ZEUS analysis/ ZEUS data



ZEUS analysis/ H1 data



ZEUS analysis/H1 data  
H1 analysis/H1 data

Here we see the effect of differences in the data;  
recall that the gluon is not directly measured (no jets).

The data differences are most notable in the large 96/97 NC  
samples at low- $Q^2$ .

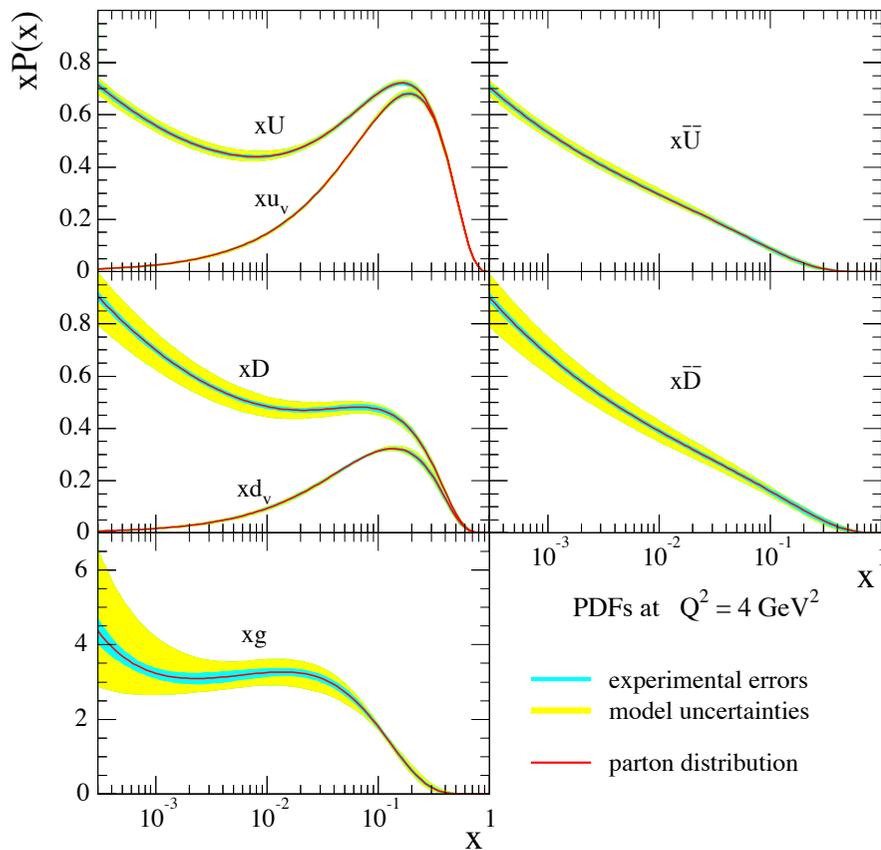
If a fit is done to ZEUS and H1 together the  $\chi^2$  for both these  
data sets rises compared to when they are fitted separately ...

Here we see the effect due  
to differences in the  
analysis choice

e.g. parametrization at  $Q_0^2$  ...

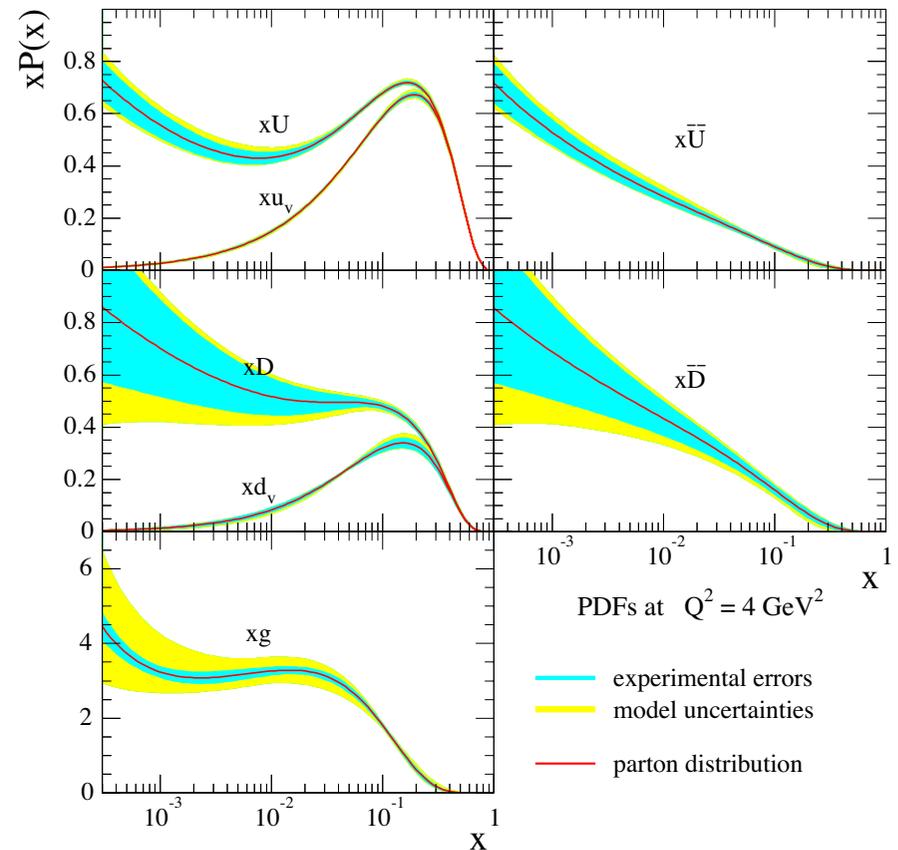
# Possible Impact of $\bar{d}-\bar{u}$ Asymmetries

H1 + BCDMS  
[ $a_{\bar{u}}$ ,  $a_{\bar{d}}$ ,  $b_{\bar{u}}$ ,  $b_{\bar{d}}$  constrained]



Enforce:  $x(\bar{d} - \bar{u}) \xrightarrow{x \rightarrow 0} 0$

H1 + BCDMS  
[ $a_{\bar{u}}$ ,  $a_{\bar{d}}$ ,  $b_{\bar{u}}$ ,  $b_{\bar{d}}$  unconstrained]

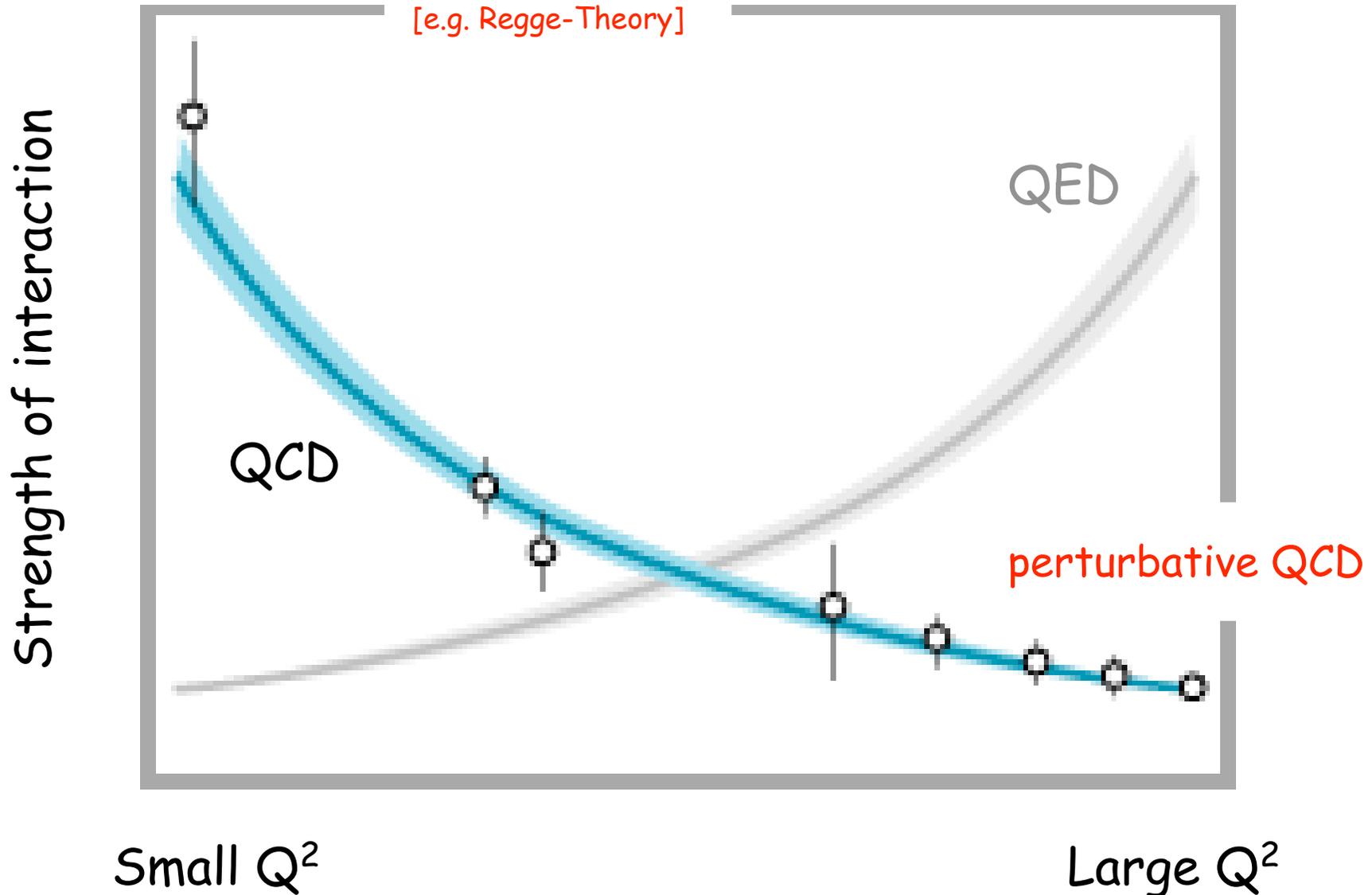


$a_{\bar{u}}$ ,  $a_{\bar{d}}$ ,  $b_{\bar{u}}$ ,  $b_{\bar{d}}$  : free parameters

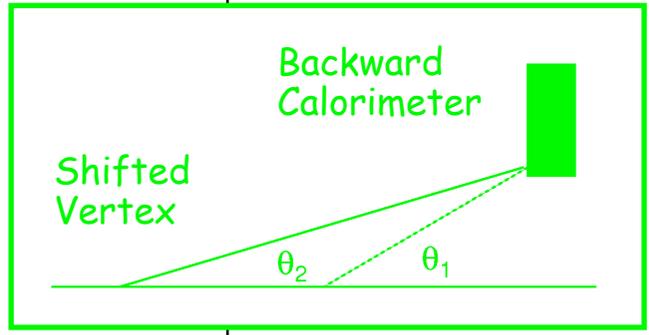
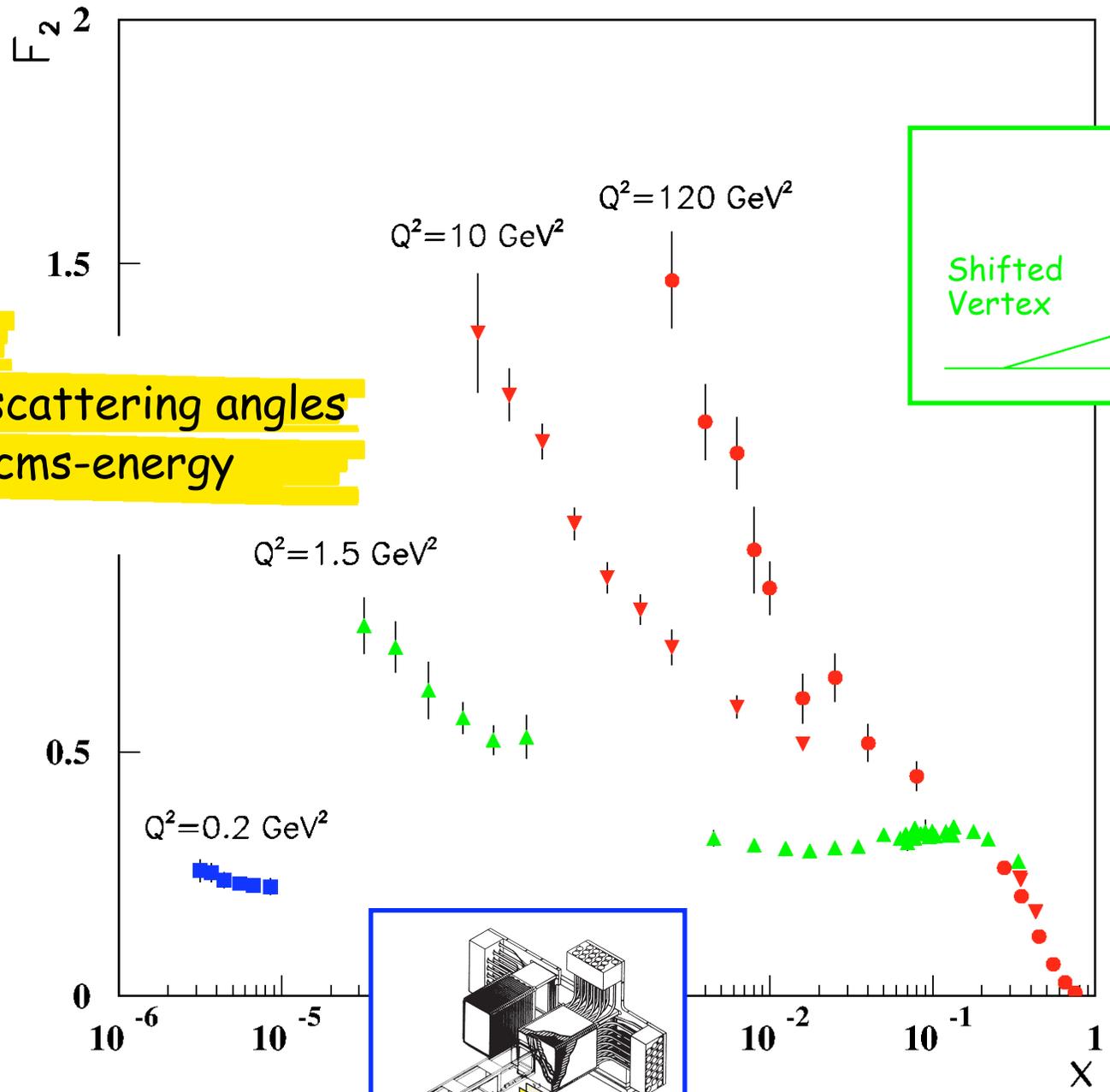
# $F_2$ @ low $Q^2$

non-perturbative region  
phenomenological description

[e.g. Regge-Theory]

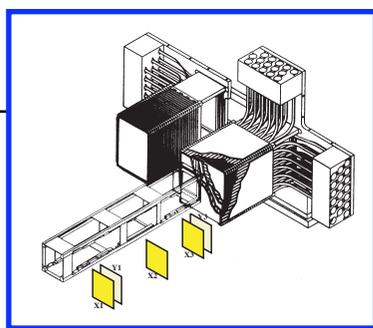


Small  $Q^2$   
 $\leftrightarrow$  small scattering angles  
 $\leftrightarrow$  lower cms-energy



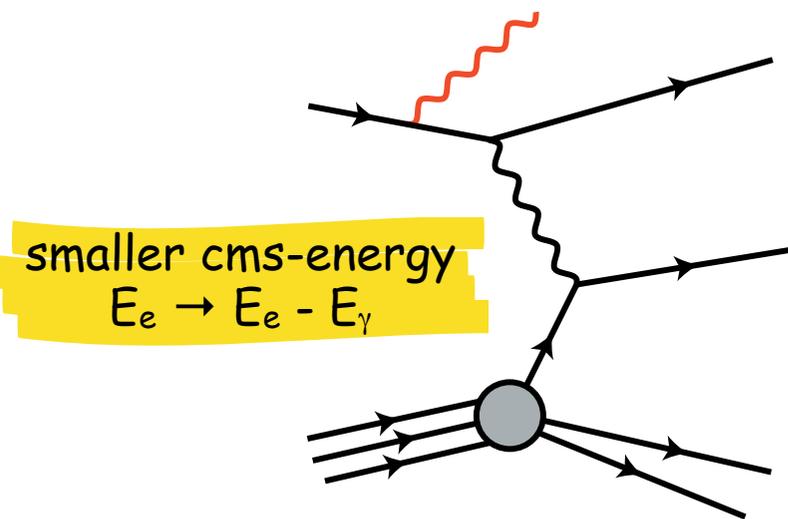
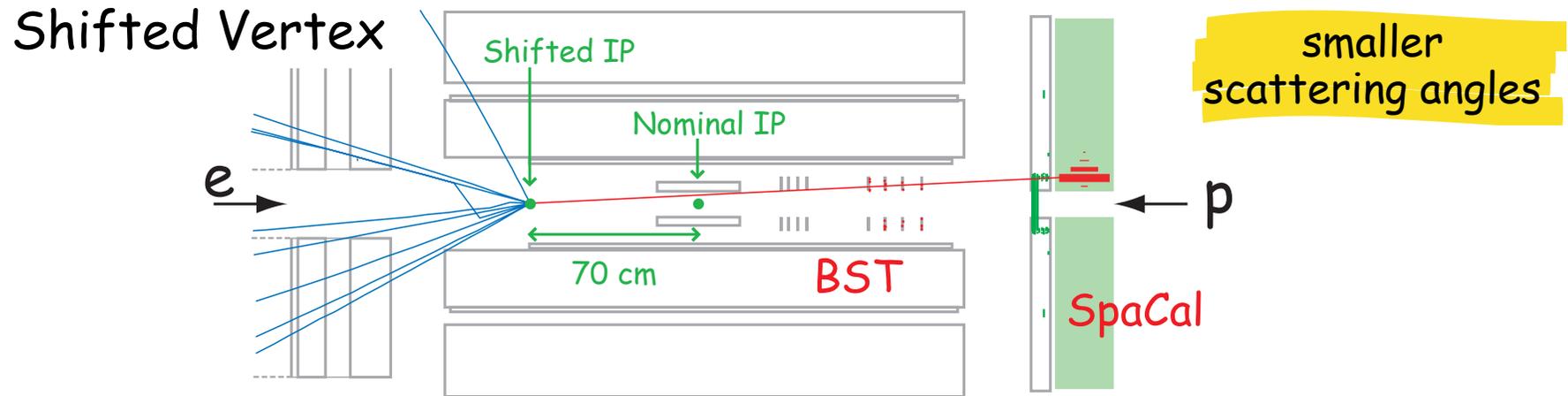
Special data taking period with shifted vertex

+ ISR  
 QEDC

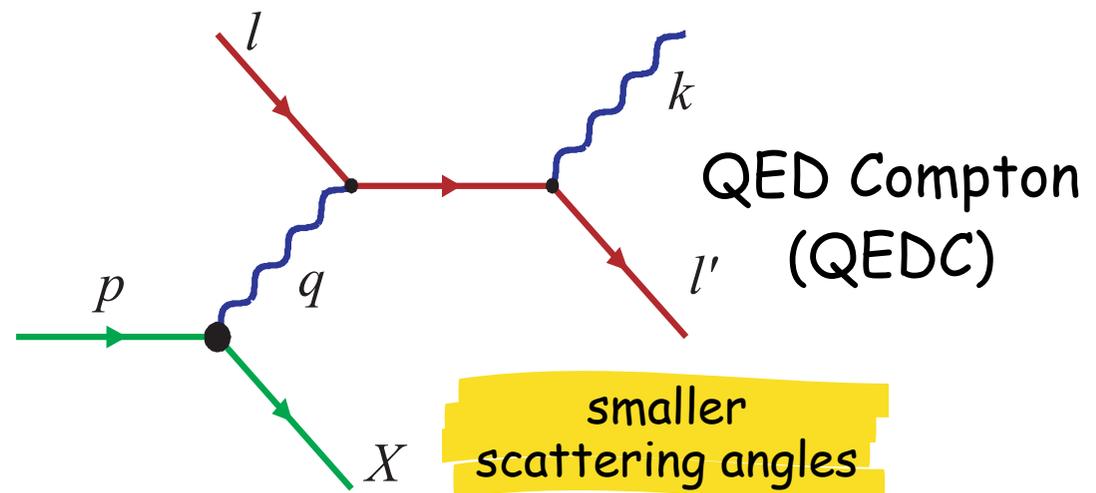


Small angle detector [ZEUS BPT]

# Experimental Technics [to Access Low $Q^2$ ]



Initial State Radiation (ISR)



● H1 svtx00 ISR prel.

● H1 QEDC97

— Fractal fit  $F_2$  and dipol  $F_L$

▲ ZEUS BPT97

● H1 svtx00 prel.

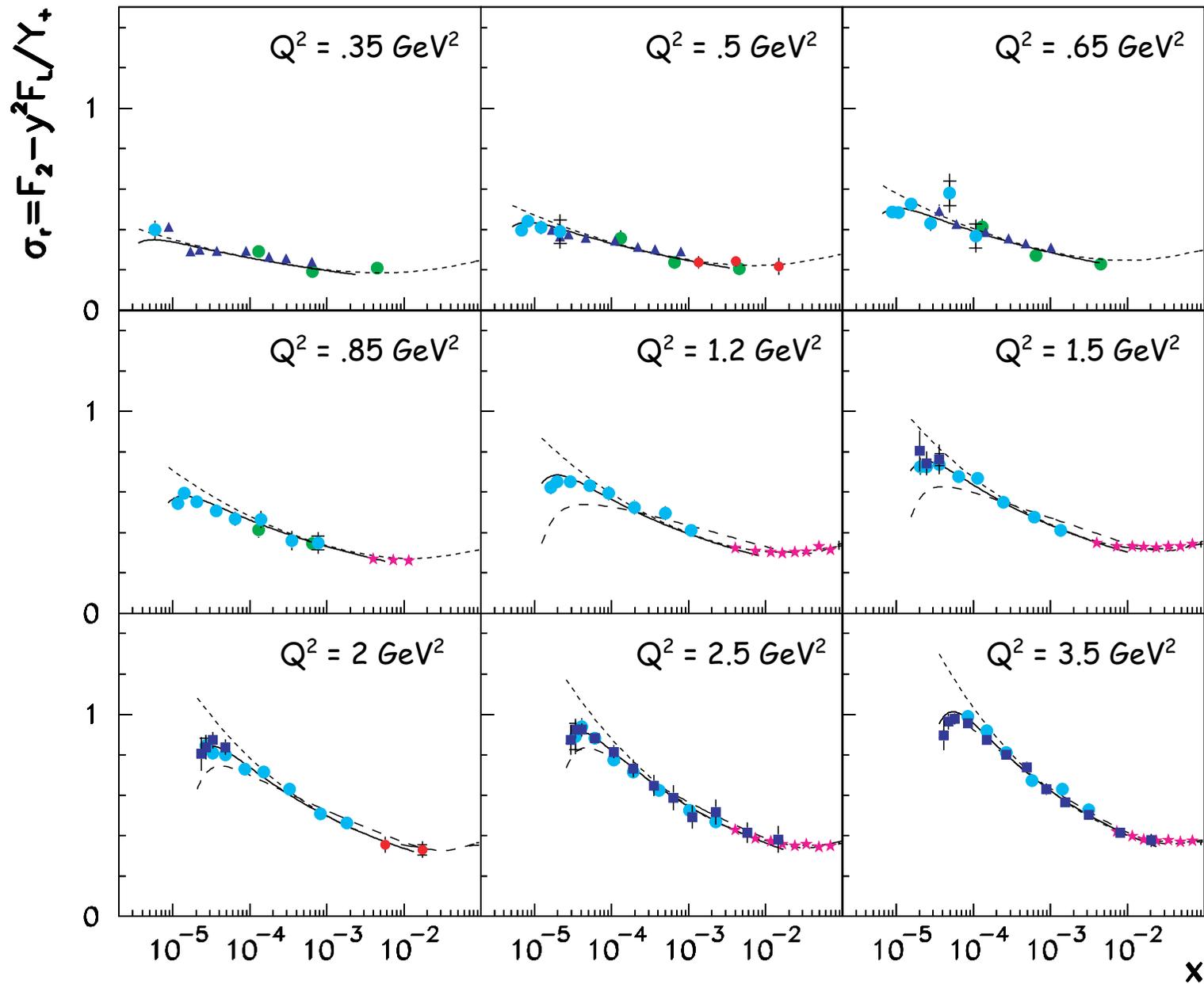
⋯ ALLM 97

★ NMC

■ H1 99 prel.

- - - H1 QCD fit 97

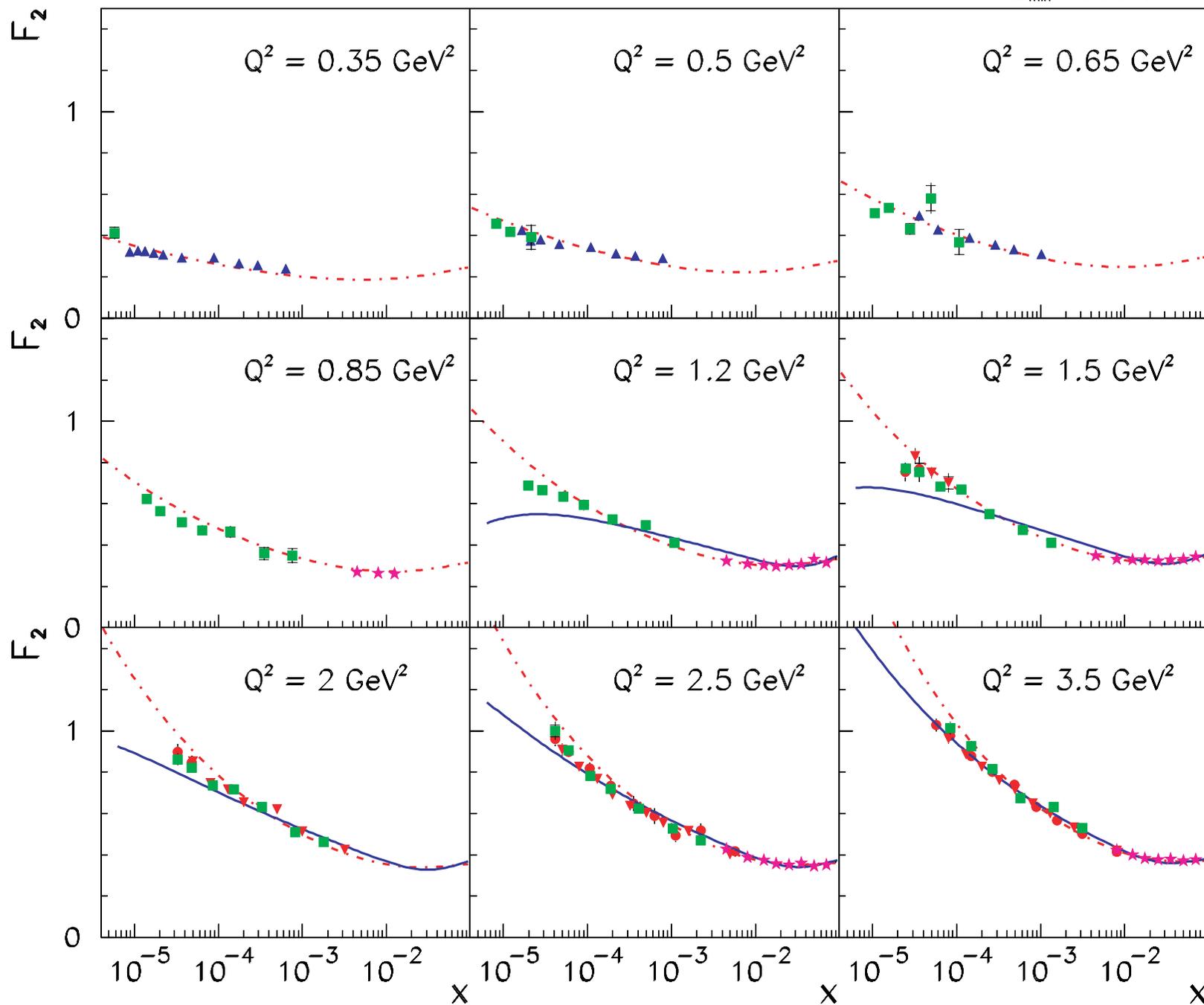
$Q^2_{\min} = 3.5 \text{ GeV}^2$



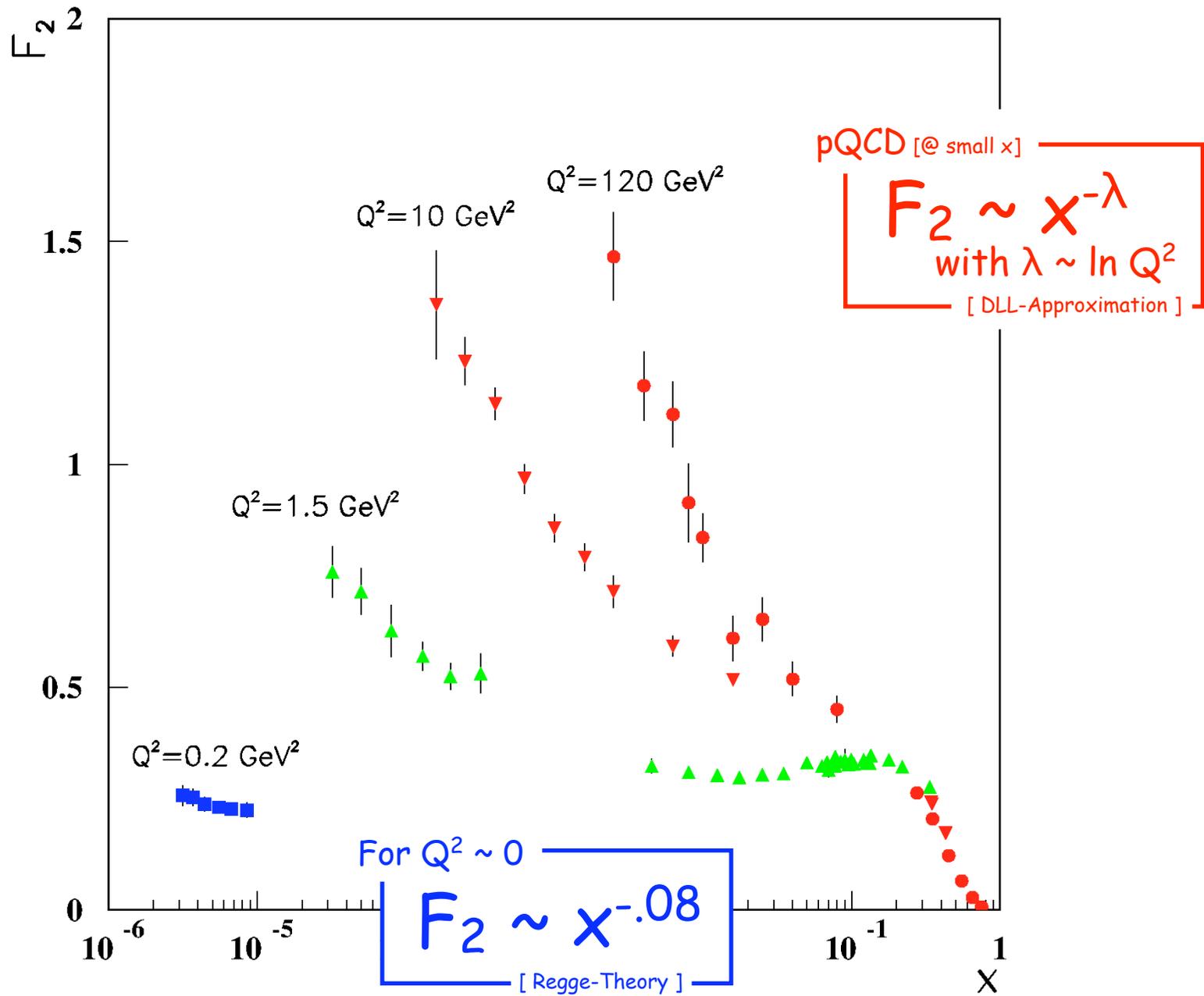
■ H1 svtx00 prel.  
● H1 99 prel.  
▼ H1 97

★ NMC  
▲ ZEUS BPT97

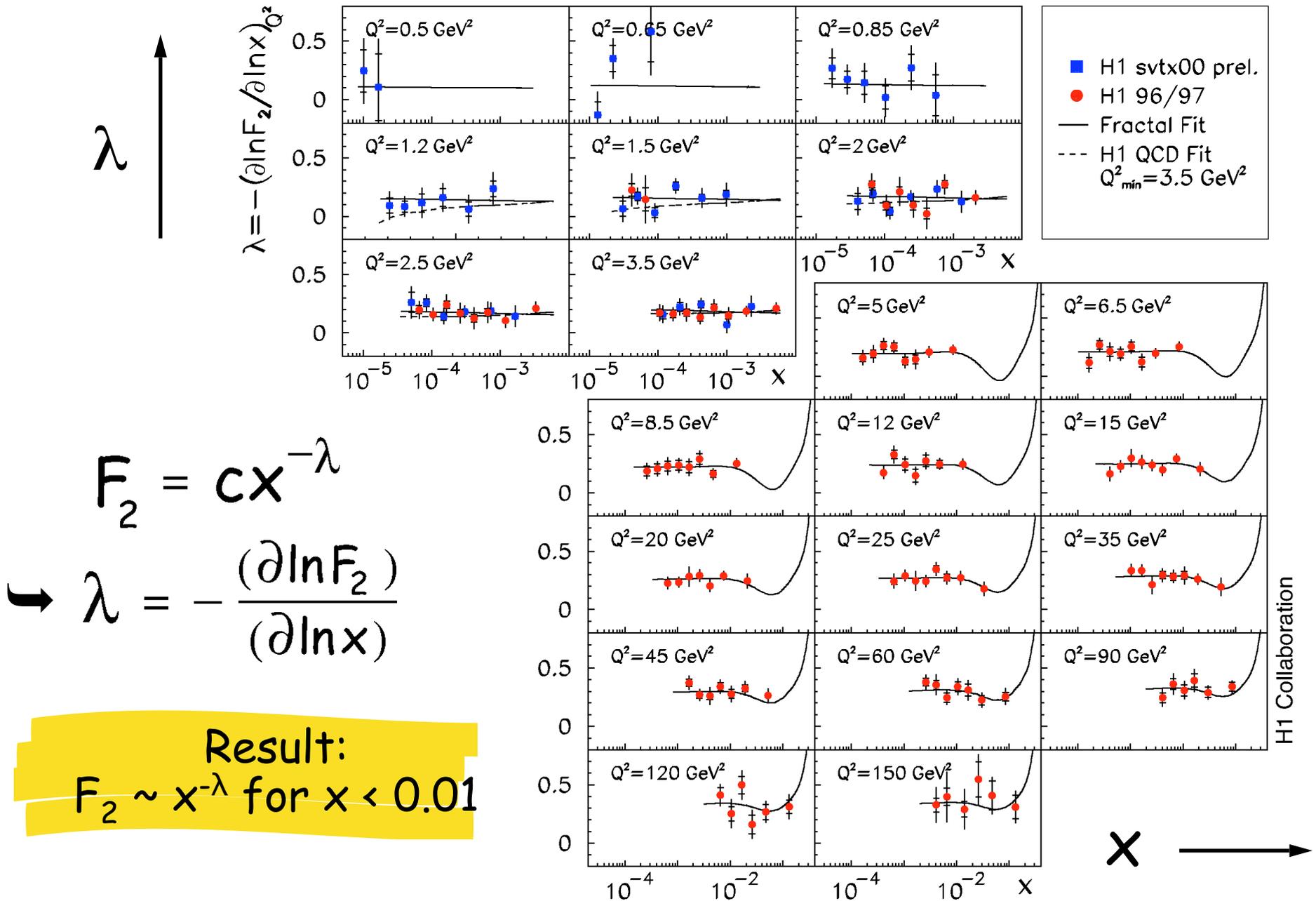
--- ALLM97  
— H1 QCD Fit  
 $Q^2_{\min} = 3.5 \text{ GeV}^2$



H1 Collaboration



# Determination of $\lambda$



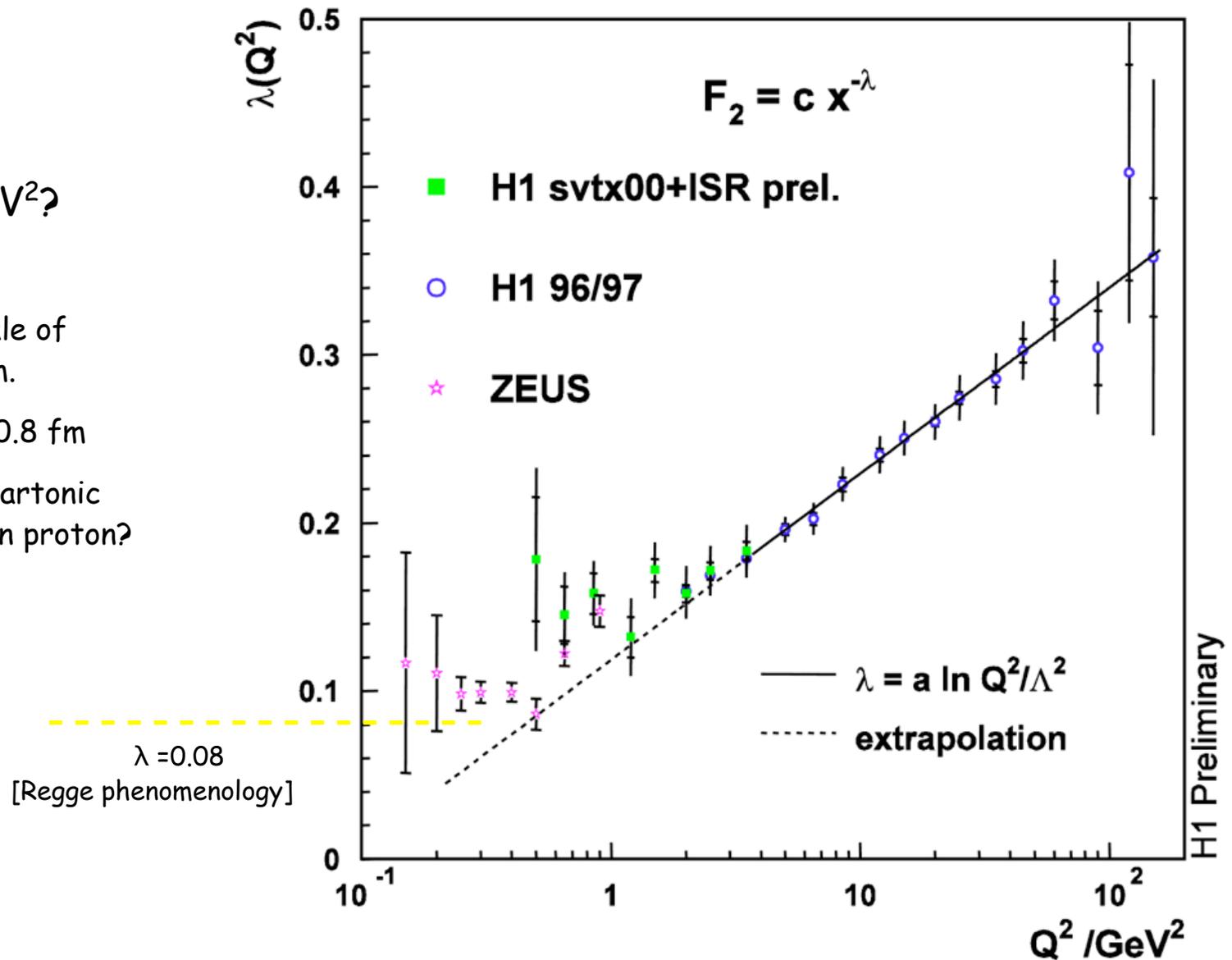
# Q<sup>2</sup>-Dependence of F<sub>2</sub>-Slope

What happens  
at Q<sup>2</sup> ~ 0.5 GeV<sup>2</sup>?

corresponds to scale of  
r ≈ ħ/Q ≈ 0.3 fm.

proton radius: r ≈ 0.8 fm

Evidence for non-partonic  
substructure within proton?



# $Q^2$ -Dependence of $F_2$ -Slope

What happens  
at  $Q^2 \sim 0.5 \text{ GeV}^2$ ?

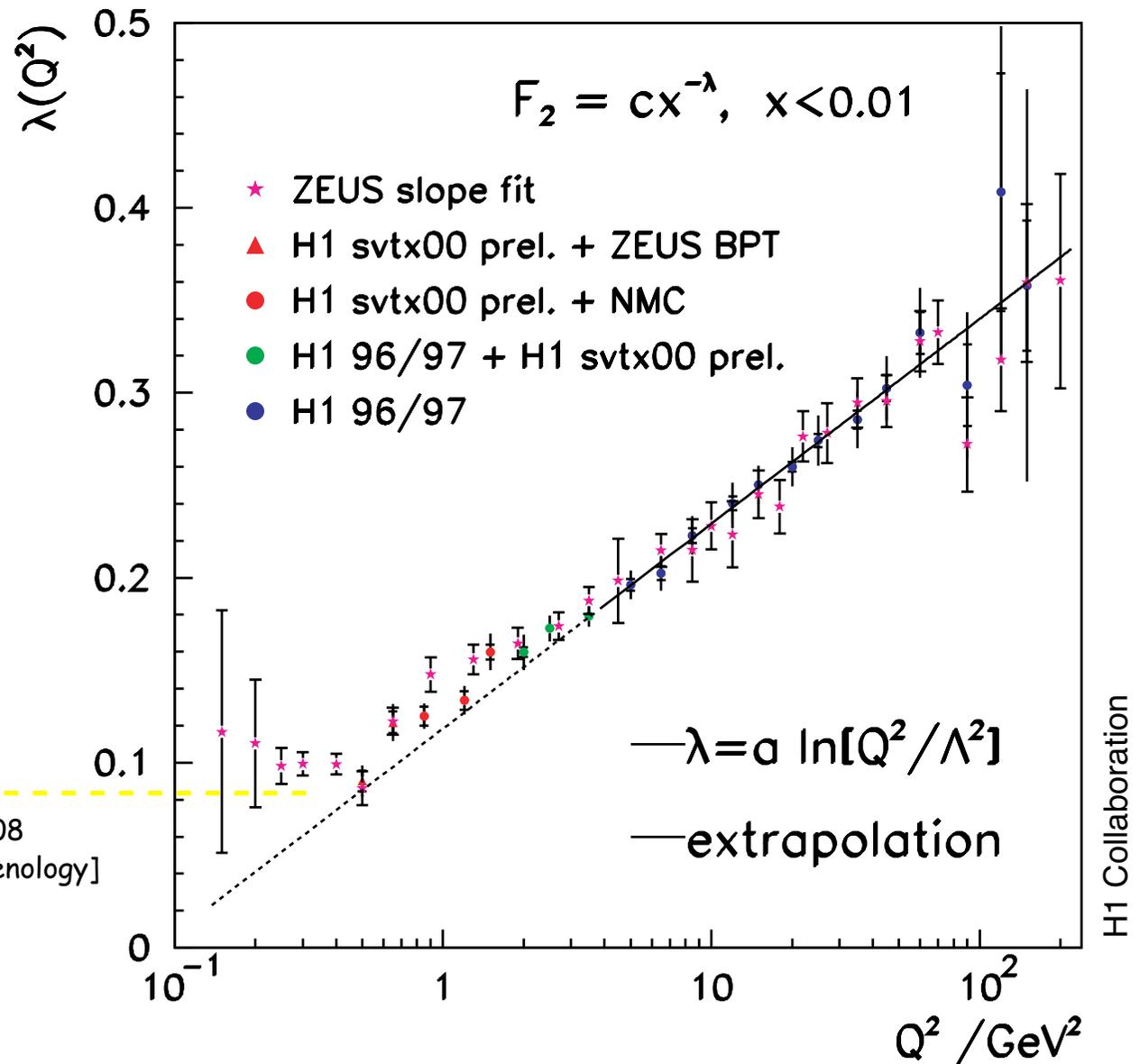
corresponds to scale of  
 $r \approx -h/Q \approx 0.3 \text{ fm}$ .

proton radius:  $r \approx 0.8 \text{ fm}$

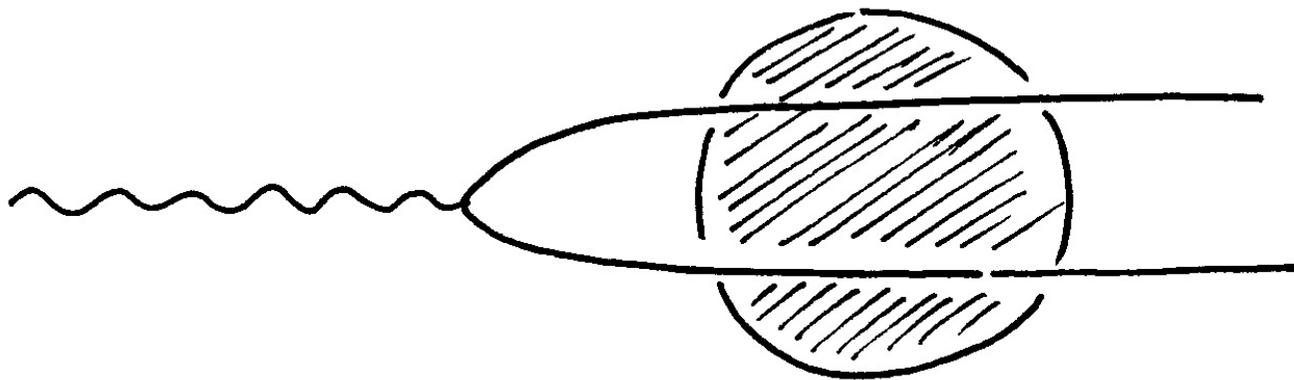
Evidence for non-partonic  
substructure within proton?

$\lambda = 0.08$   
[Regge phenomenology]

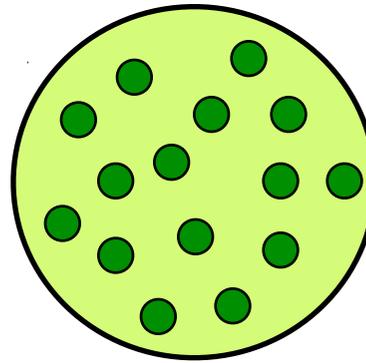
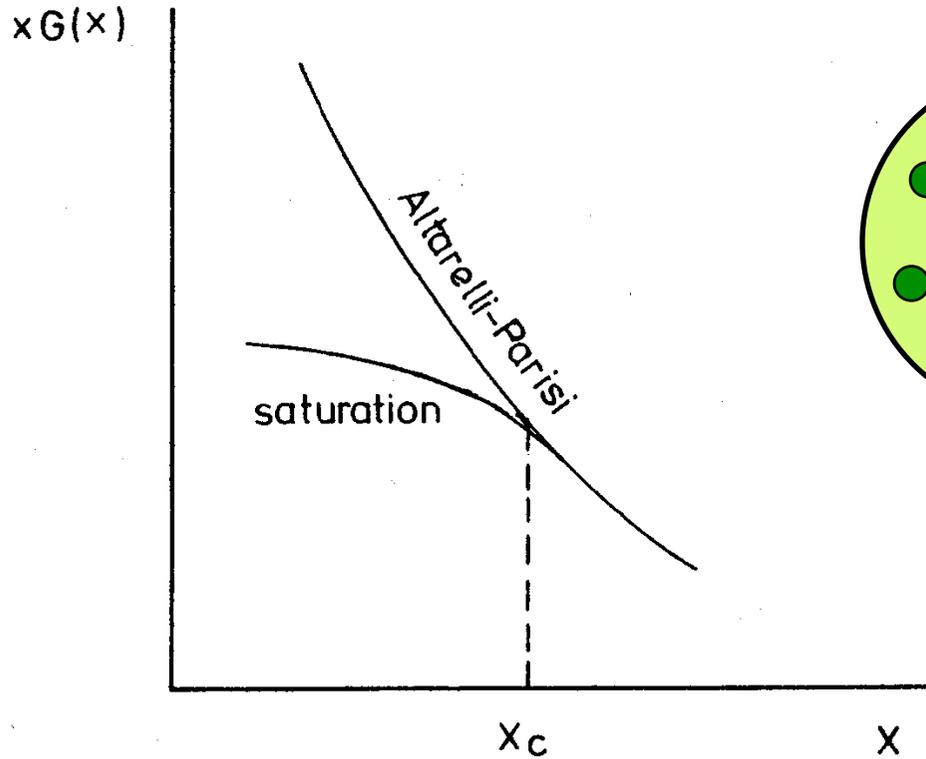
More precision  
from combined data ...



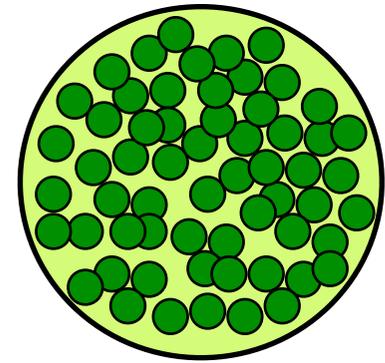
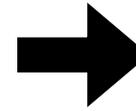
From hard to soft physics  
Do we see saturation?



# Saturation



$$x \gg x_c$$



$$x \ll x_c$$

Unitarity consideration:  
Rise towards small  $x$  has to  
stop somewhere

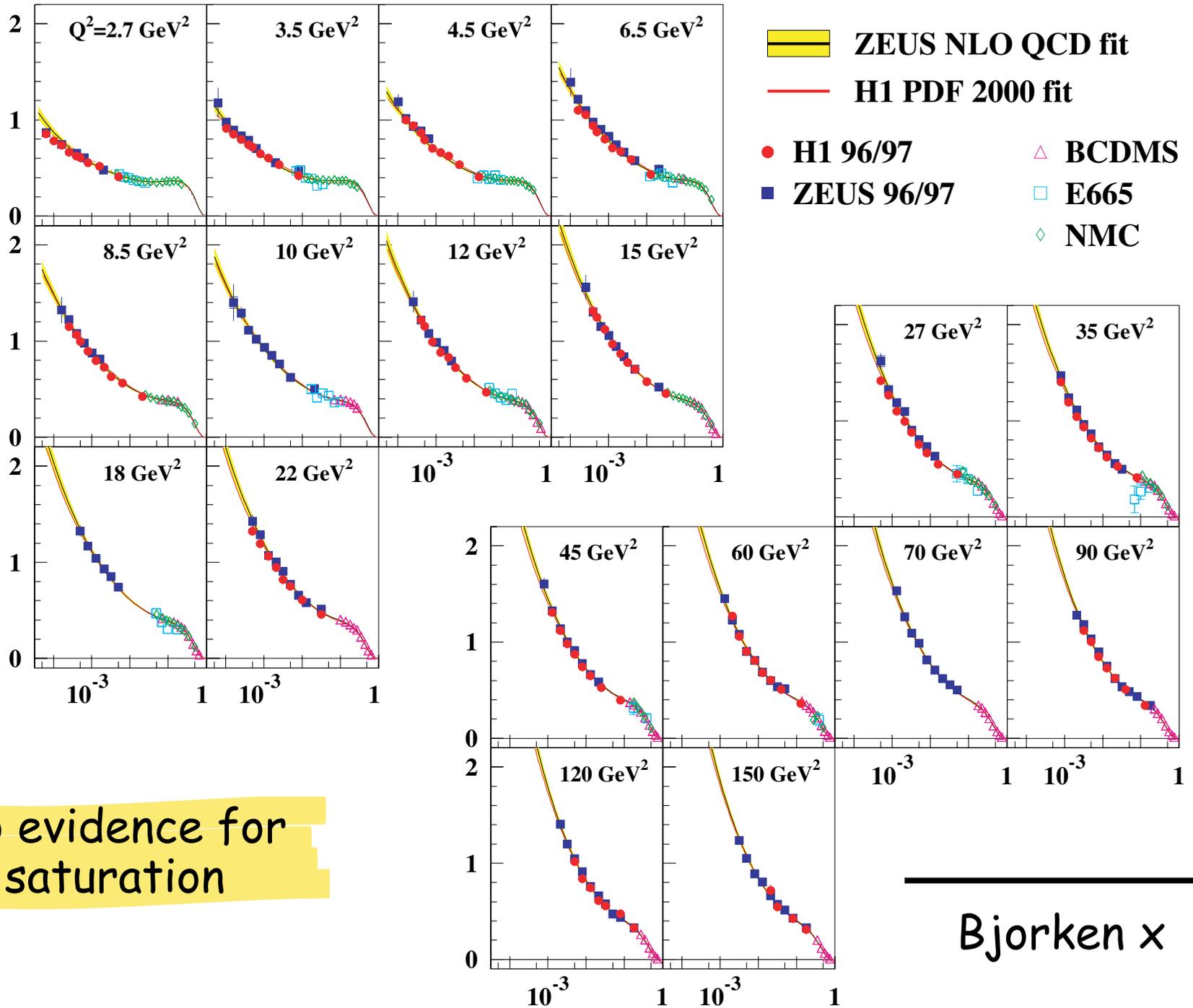
Expectation:

At some point number of gluons  
is so large that recombination  
becomes important

Possible observation:

Taming of the rise of  $F_2$  at low  $x$

Structure Function  $F_2$

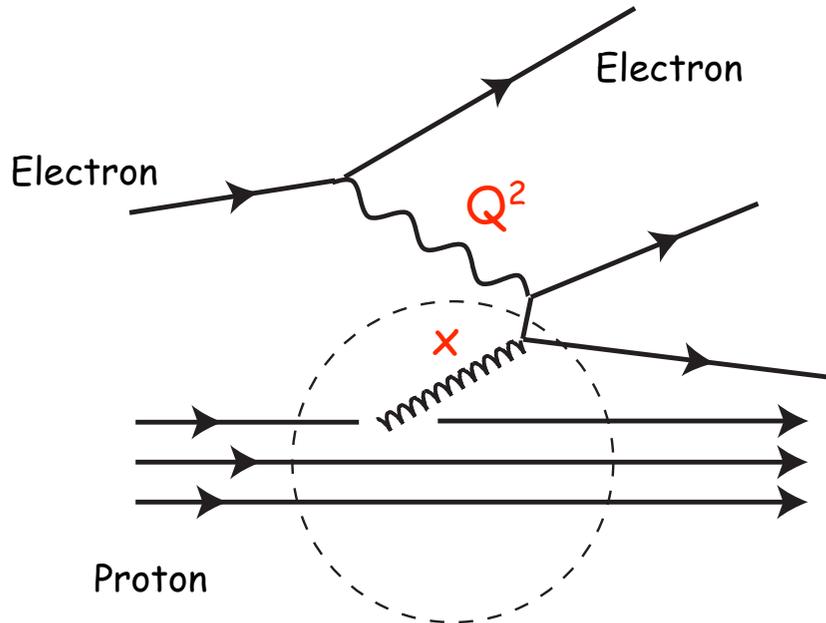


No evidence for saturation

Bjorken  $x$

# ep-Scattering - Alternative Pictures

Infinite momentum frame



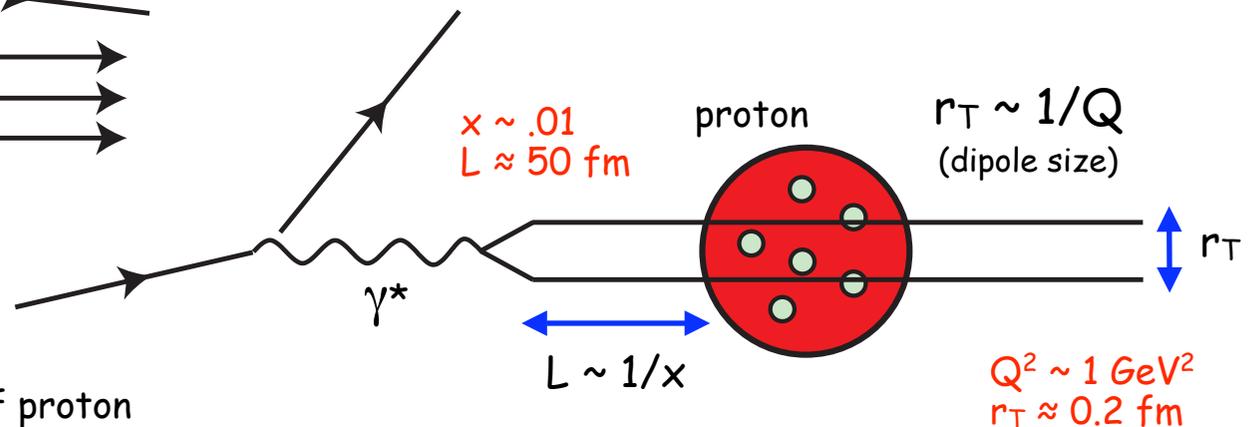
Electron interacts with quark of proton  
Parton content described by  $F_2$

Proton rest frame

A colour dipole of variable size  $r_T \sim 1/Q$   
interacts with the proton at high CM energy

$$s^{\gamma^*p} = W^2 = Q^2/x$$

[ low  $x$  = high energy scattering! ]



$$F_2(x, Q^2) = F_2(W^2, Q^2) \approx 4\pi\alpha^2 \cdot Q^2 \cdot \sigma^{\gamma^*p}(s^{\gamma^*p}, Q^2)$$

# The Saturation Model

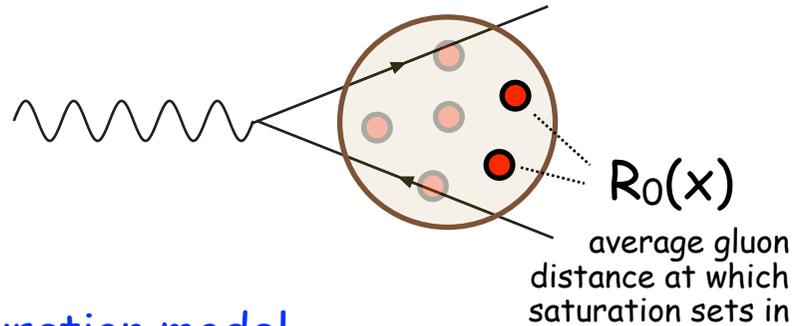
Dipole model  
 $\gamma^*p$  cross section  
 [for small  $x$ ]

$$\sigma_{T,L}^{\gamma^*p}(x, Q^2) = \int d^2r dz \psi_{T,L}^*(Q, r, z) \hat{\sigma}(x, r) \psi_{T,L}(Q, r, z)$$

dipole proton x-section  $\searrow$   
 dipole wave function  $\swarrow$

Saturation model à la GBW:

$$\hat{\sigma}(x, r) = \sigma_0 \left\{ 1 - \exp\left(-r^2/4R_0^2(x)\right) \right\}$$

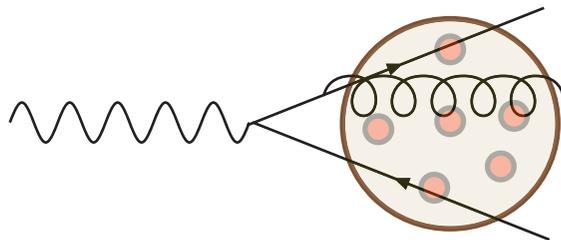


$$R_0^2(x) = \frac{1}{\text{GeV}^2} \left( \frac{x}{x_0} \right)^\lambda$$

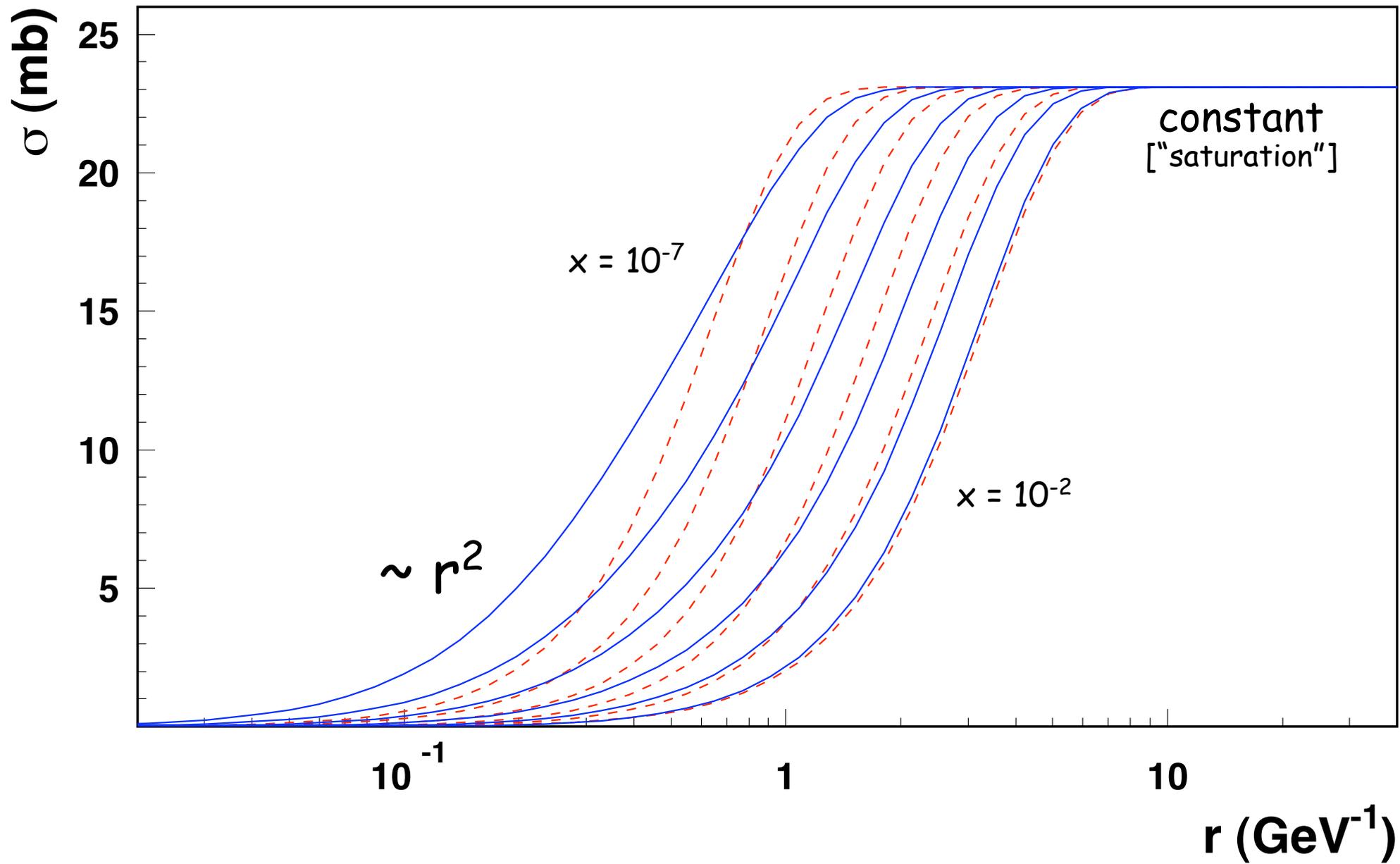
Saturation model including gluon evolution:

DGLAP [for small  $r$ ]:

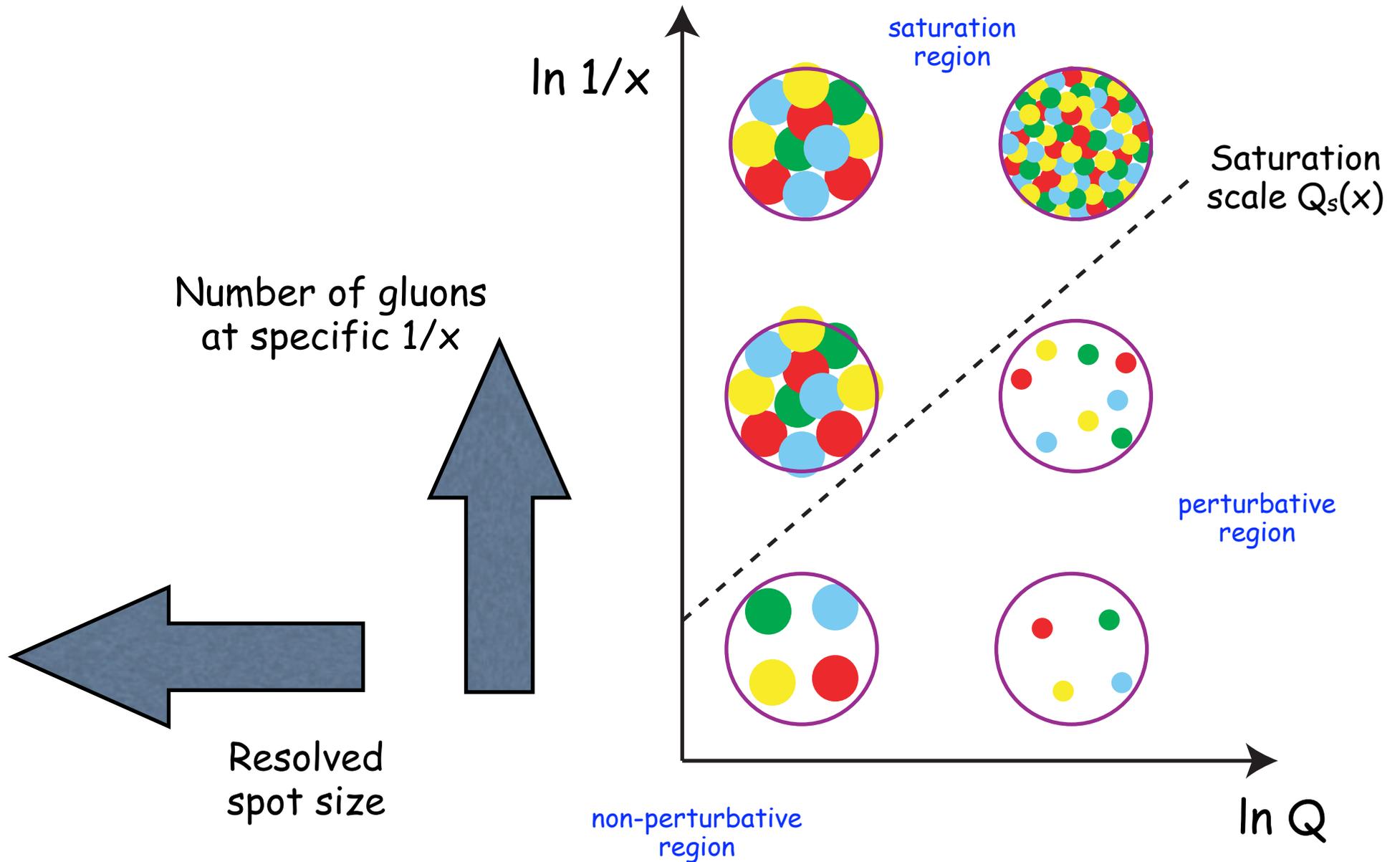
$$\left[ \hat{\sigma}(x, r) \simeq \frac{\pi^2}{3} r^2 \alpha_s x g(x, \mu^2) \right]$$

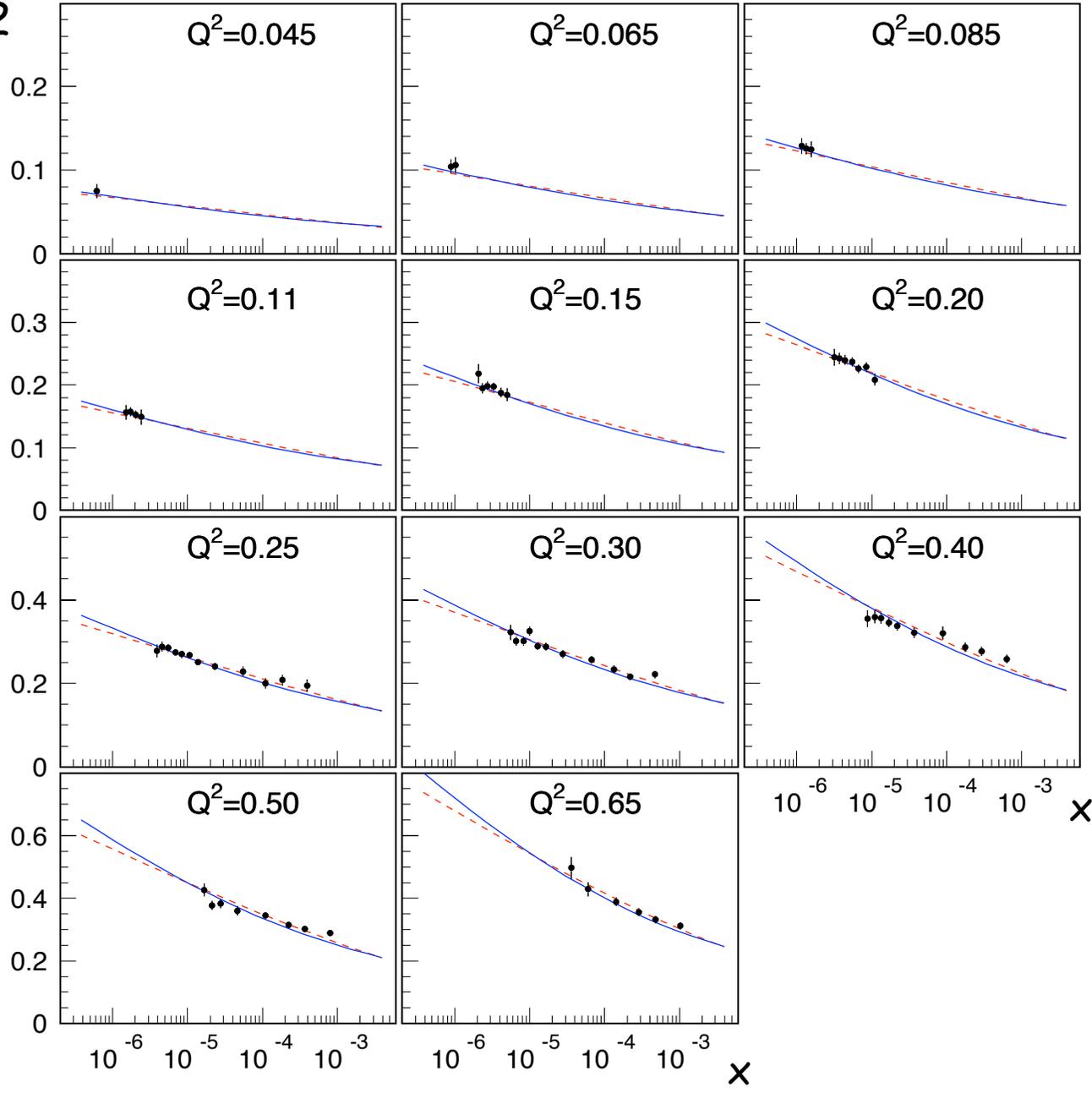


$$\hat{\sigma}(x, r) = \sigma_0 \left\{ 1 - \exp\left(-\frac{\pi^2 r^2 \alpha_s(\mu^2) x g(x, \mu^2)}{3 \sigma_0}\right) \right\}$$



# Parton Saturation



$F_2$ 

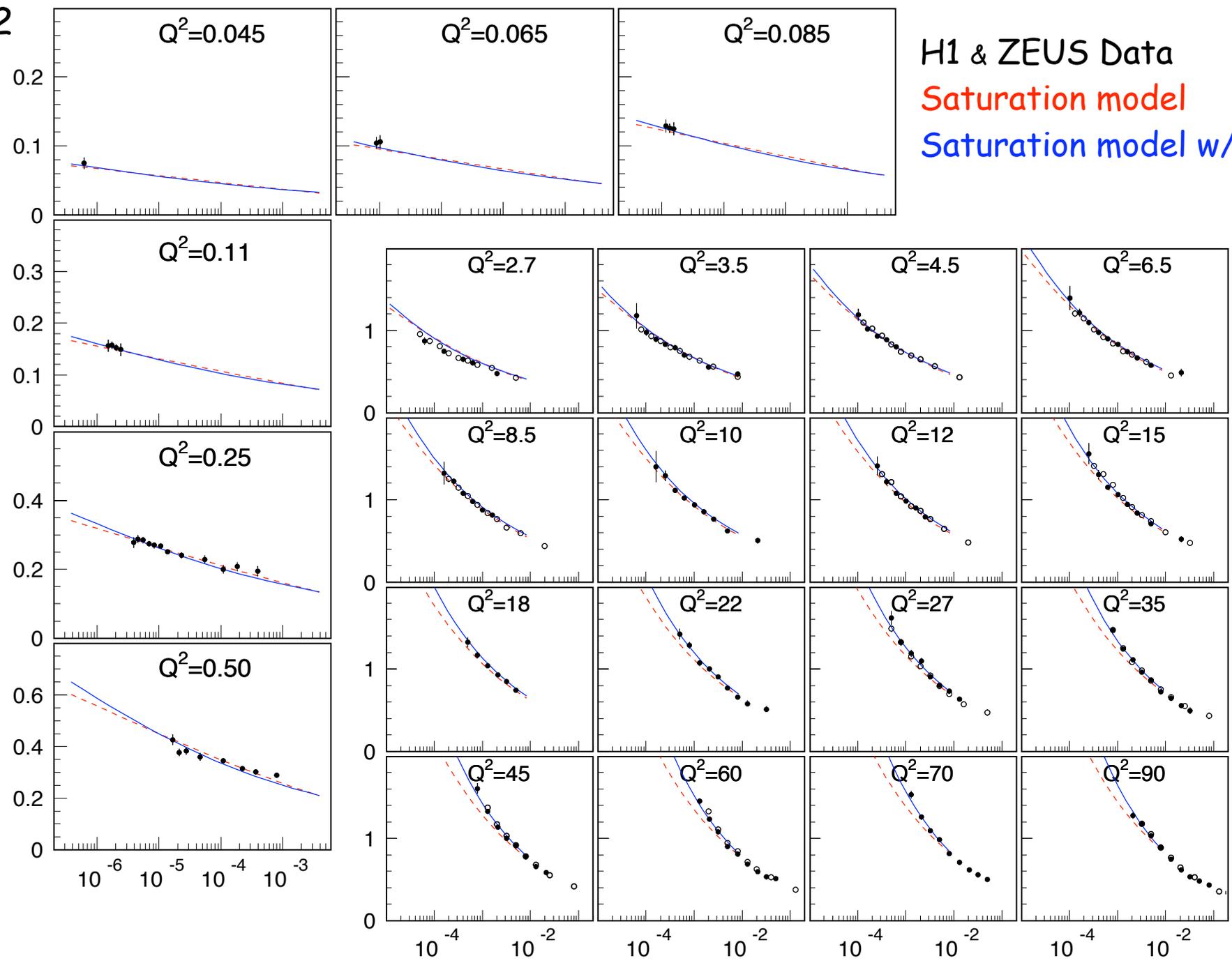
H1 & ZEUS Data  
Saturation model  
Saturation model w/ DGLAP

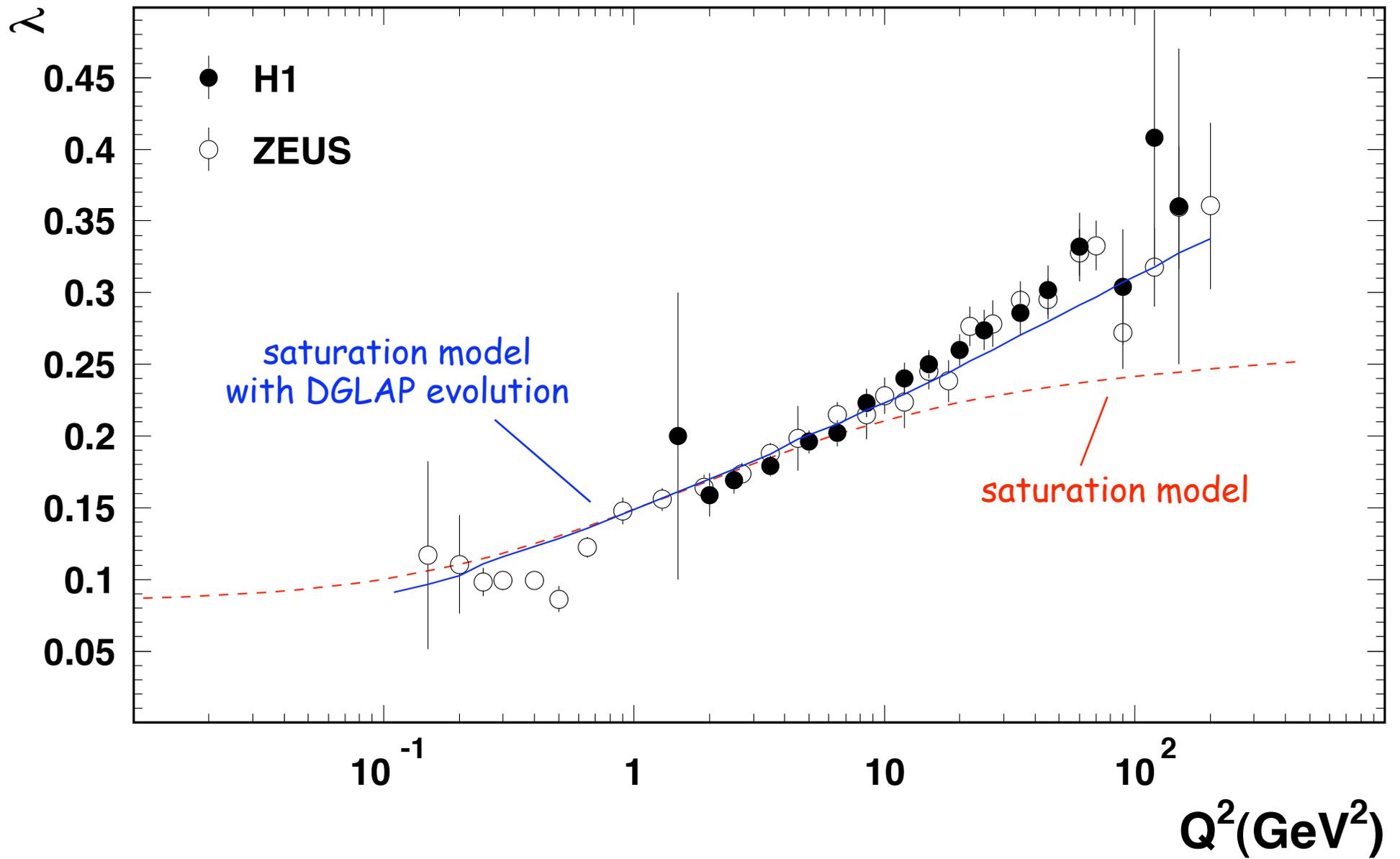
Three parameters fit  
[ $\sigma_0, x_0, \lambda$ ]  
Five parameters fit  
[ $\sigma_0, g(x)$  parameterization]



$F_2$ 

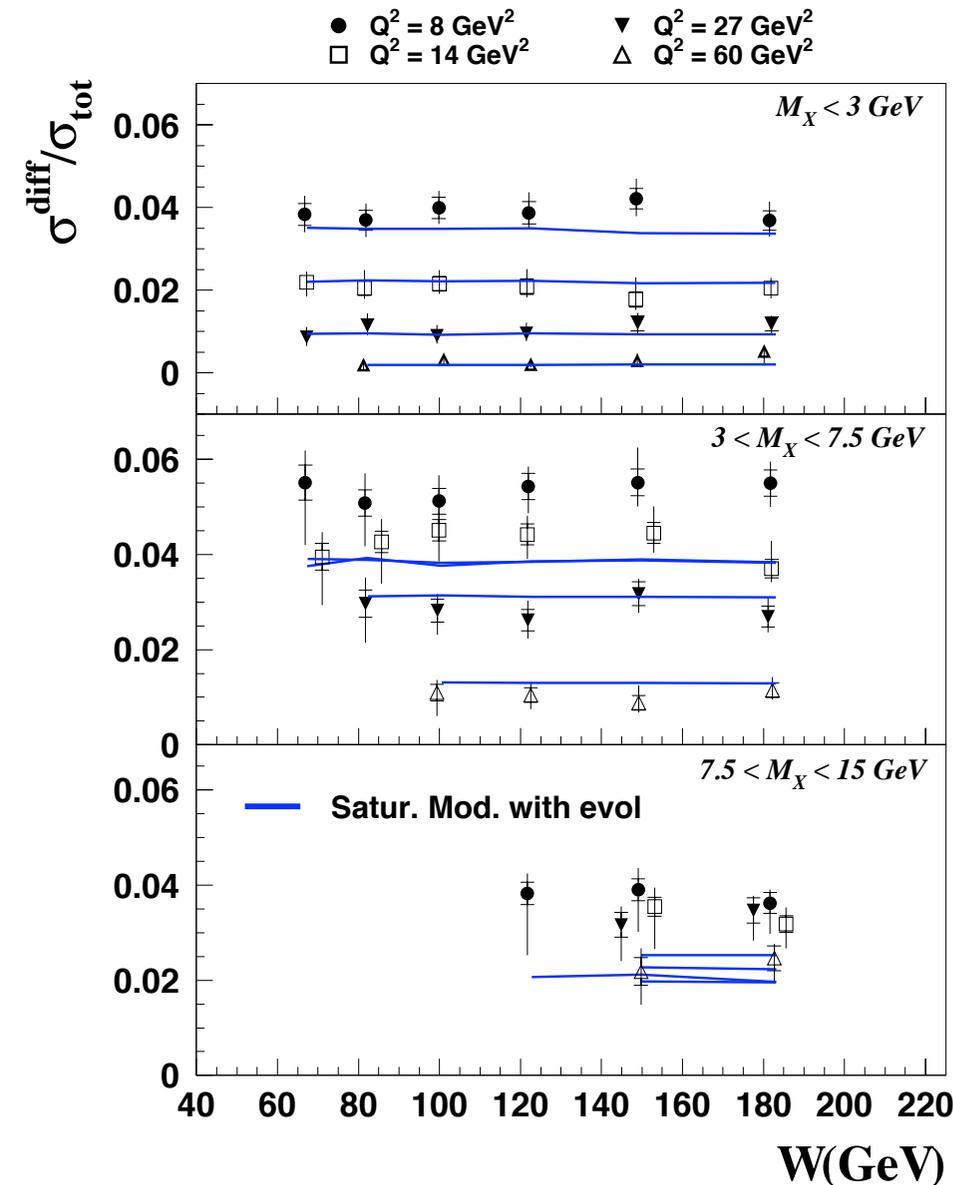
H1 & ZEUS Data  
Saturation model  
Saturation model w/ DGLAP





Transition to soft physics described!

# Do we see saturation ?

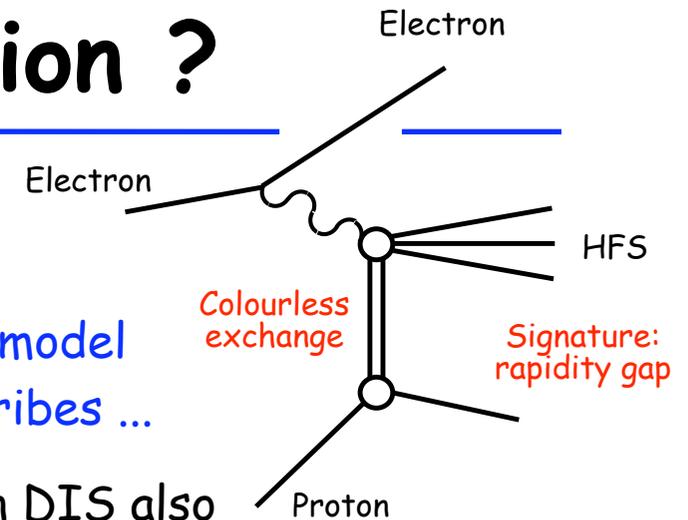


Dipole saturation model successfully describes ...

- describes  $F_2$  in DIS also at small  $x$  and low  $Q^2$  (Fit!)
- predicts details of diffractive processes
- predicts diffractive DIS/DIS = constant
- ...

No proof of saturation, but ...

- several independent effects described
- very appealing
- also very much discussed also within Heavy Ion community (Color Glass Condensate)
- more theoretical work needed ...



# Concluding Remarks

HERA provides the decisive information about parton distributions, especially the gluon content of the proton

HERA has delivered data which guide theory to describe low energy QCD, e.g. the transition from hard to soft physics

However, despite of large theoretical progress regarding saturation, dynamic QCD evolution, understanding of diffraction ...

... low energy QCD is still not understood

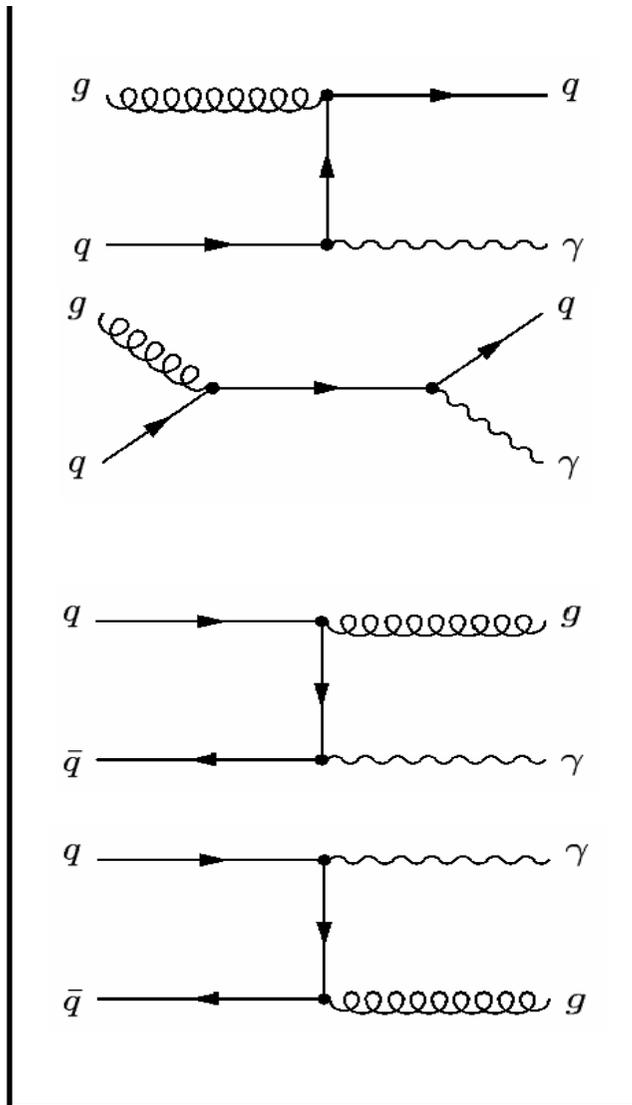
# Epilogue

How to constrain PDFs at LHC

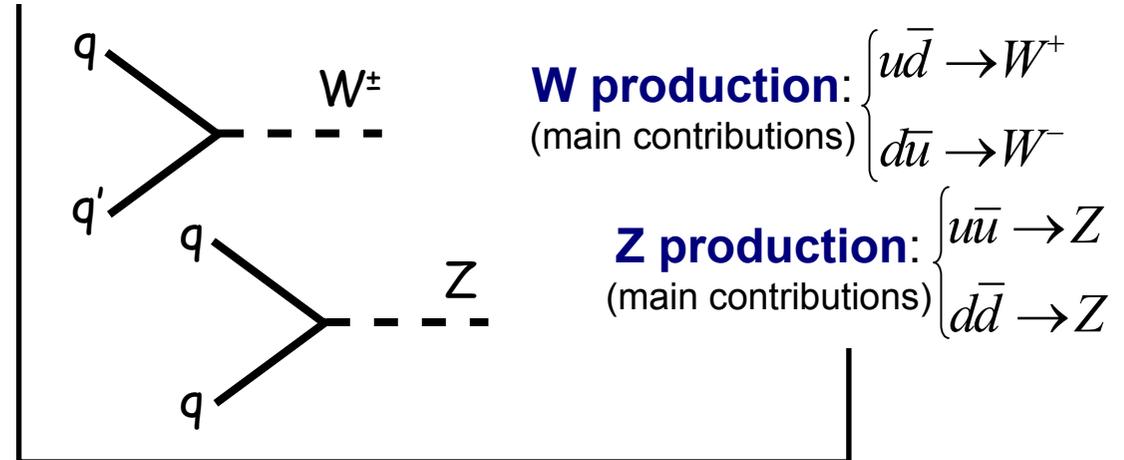
[some examples]

# Vector Boson Production

Direct  $\gamma$ -production:

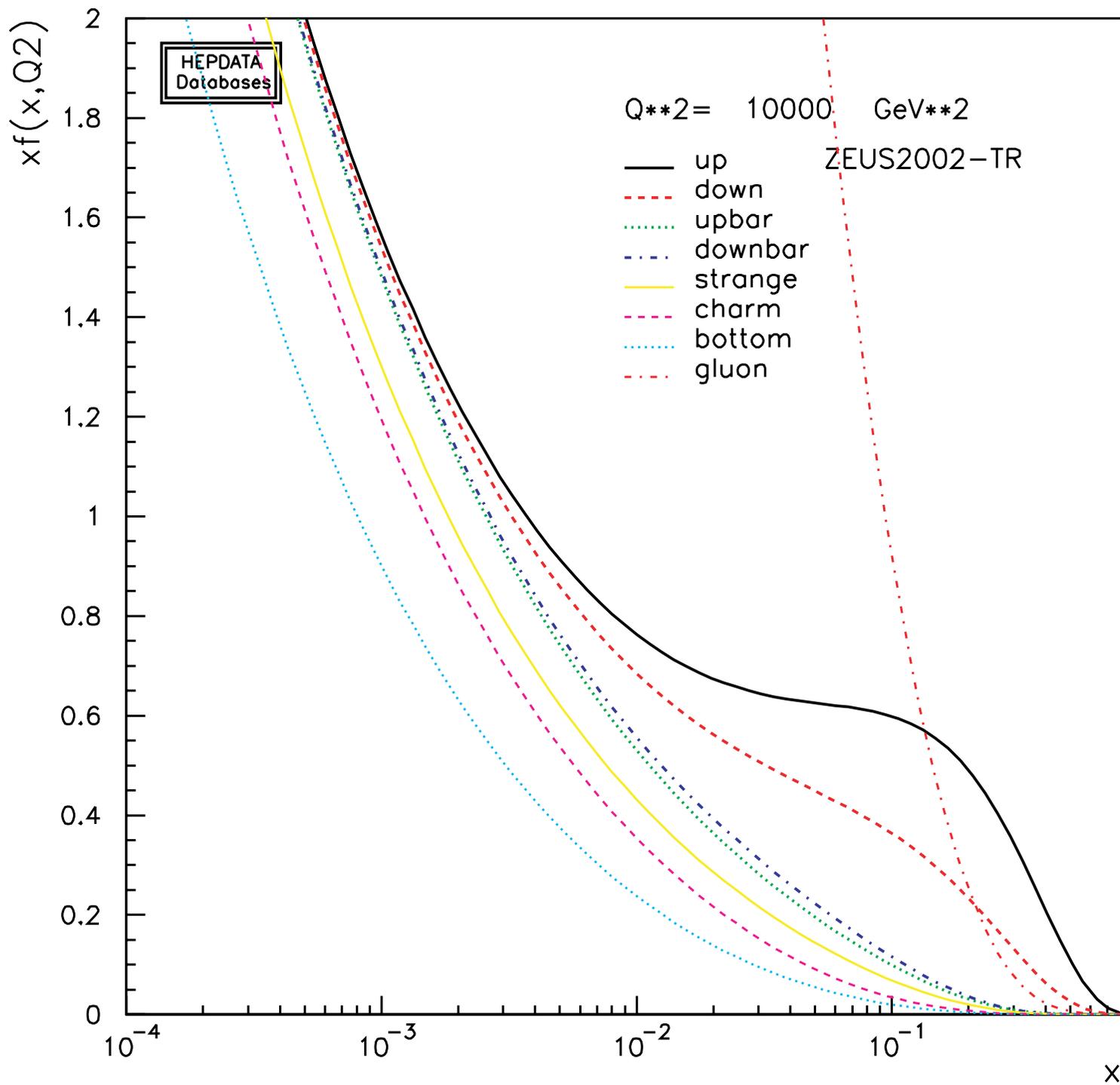


Singlet W/Z production:



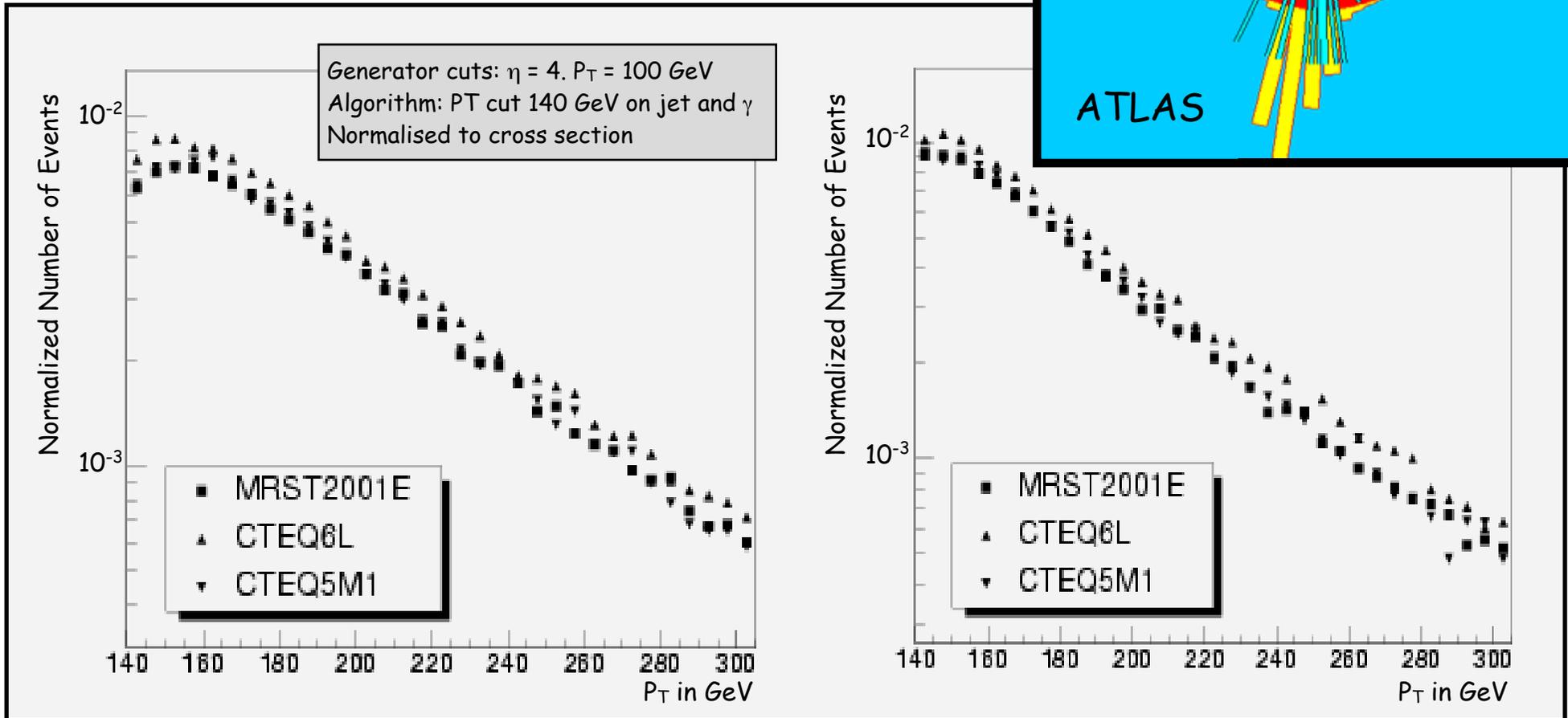
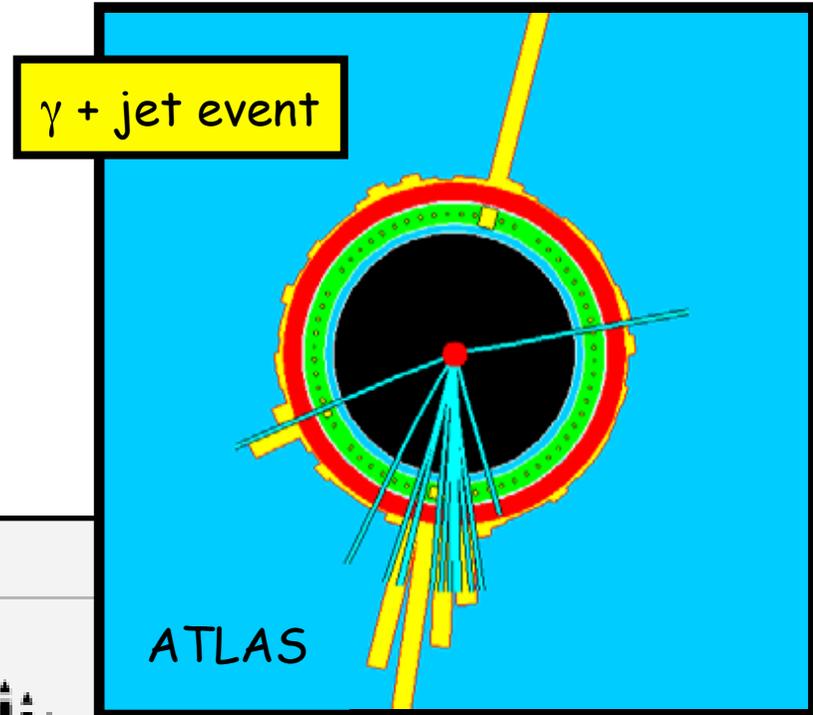
- At LHC energies these processes take place at low values of Bjorken- $x$
- Only sea quarks and gluons are involved
- At EW scales sea is driven by the gluon, i.e. x-sections dominated by gluon uncertainty

➔ Constraints on sea and gluon distributions

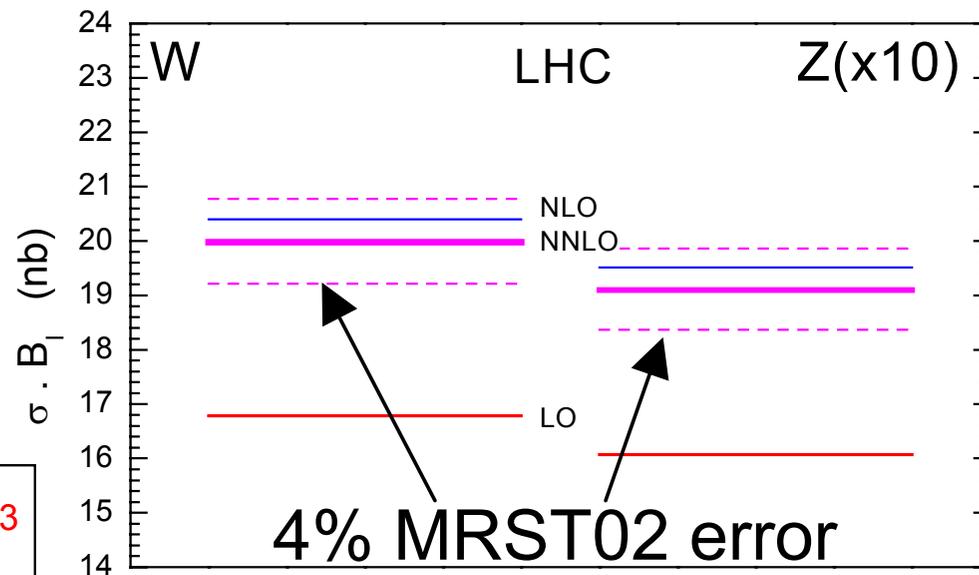
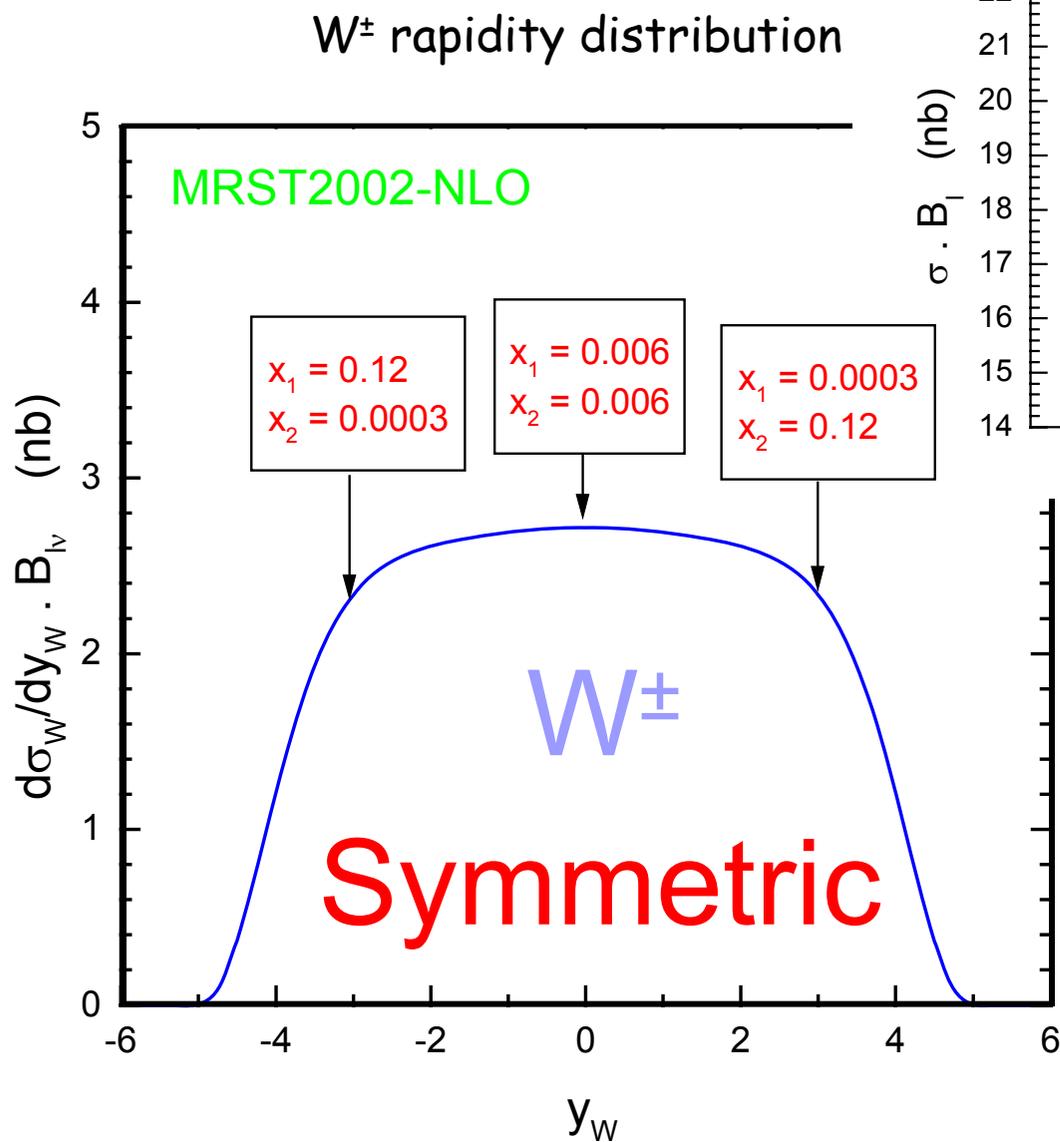


# Direct $\gamma$ Production

Sensitive to PDF differences  
CTEQ - MRST:  $\pm 16$  -18 % disagreement  
Needs good understanding of detector



# Single W and Z Production

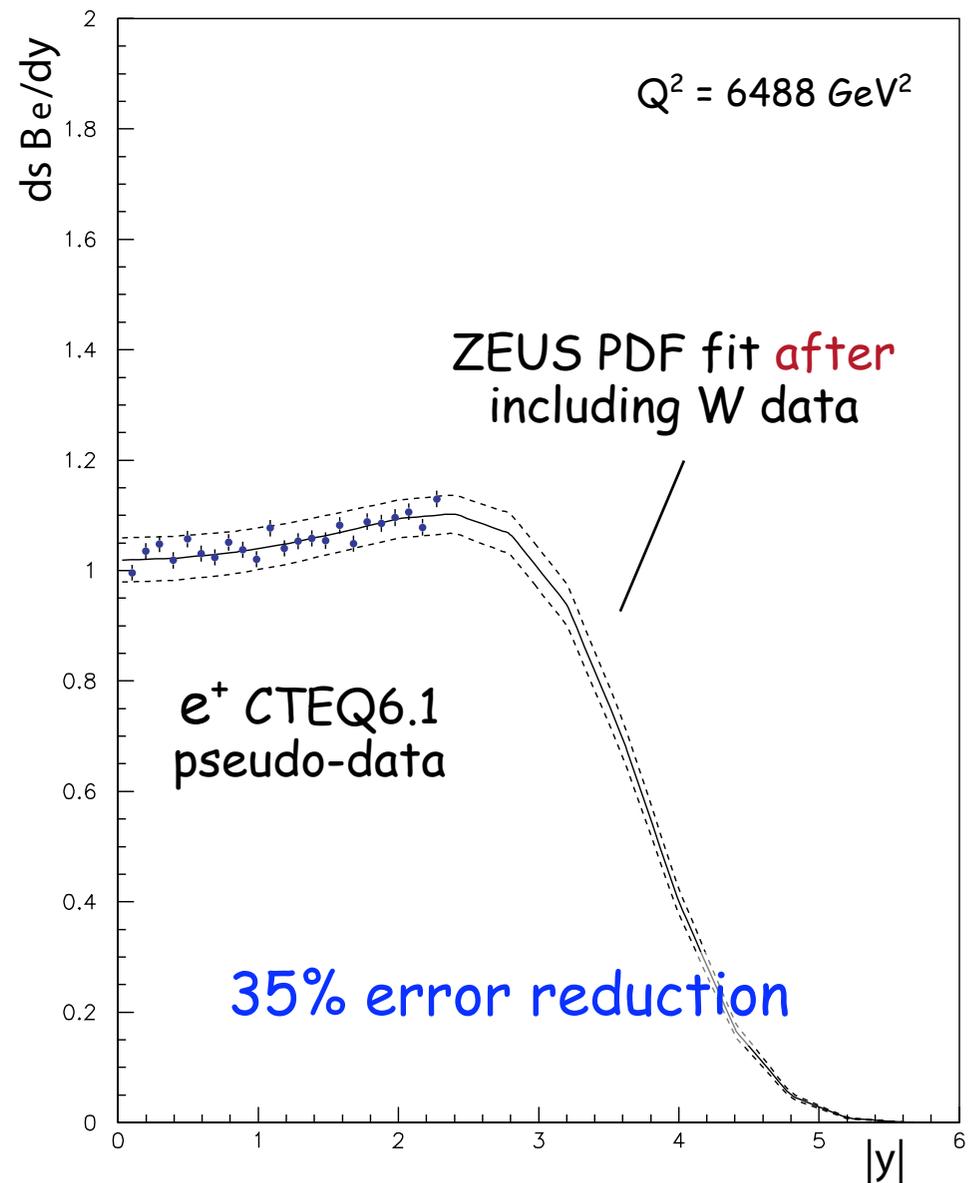
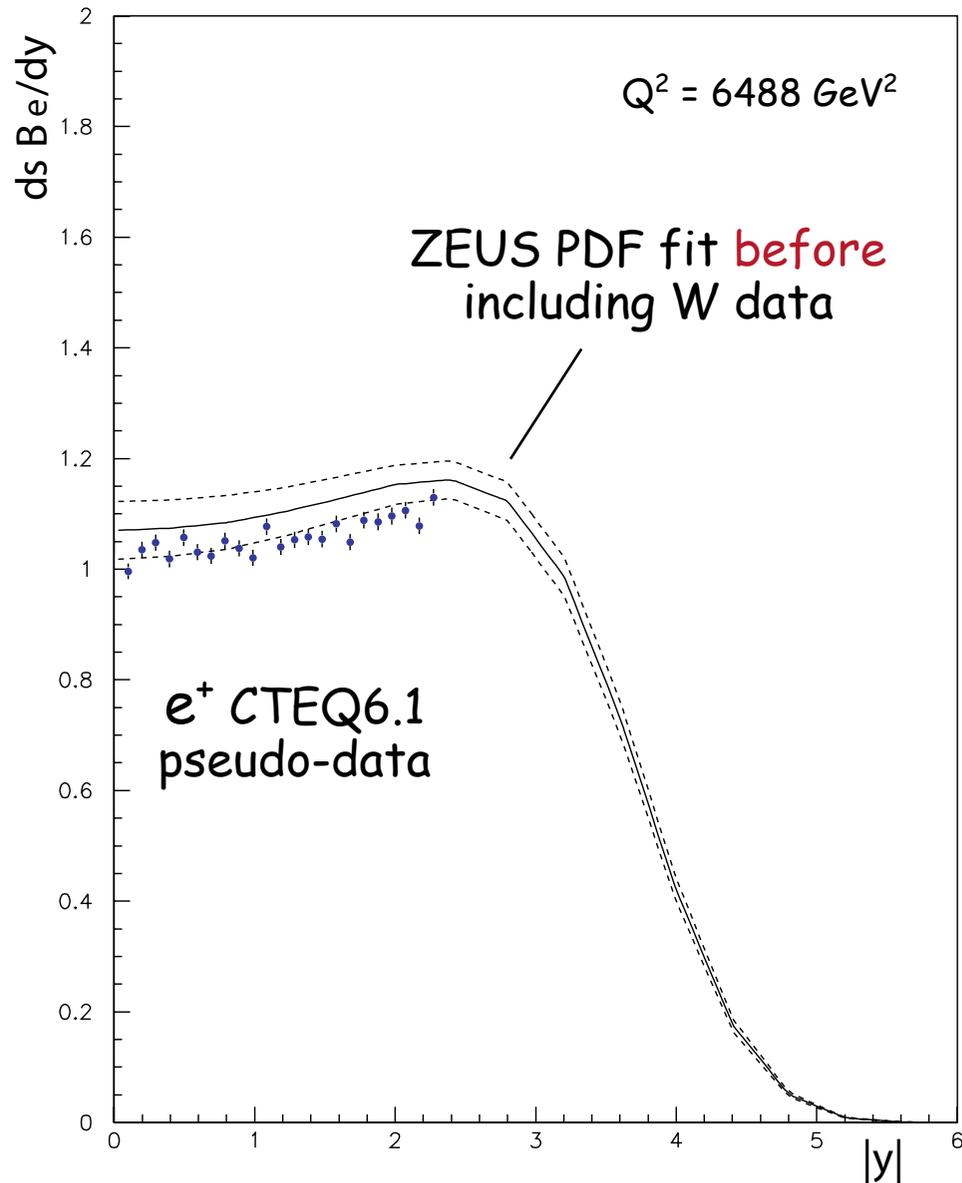


$W^\pm$  total cross section

Theoretical uncertainty  
dominated by PDFs

Extra input from  
LHC measurements

# Effect on PDFs of LHC W data



# Data Included in CTEQ Fits

