



# Extraction of the light quark mass ratio from heavy quarkonia transitions

# Feng-Kun Guo

#### Helmholtz-Institut für Strahlen- und Kernphysik, Universität Bonn

Collaborators: Christoph Hanhart, Gang Li, Ulf-G. Meißner and Qiang Zhao

Strong interactoins: From methods to structures

Bad Honnef, Feb.12-16, 2011

Based on the following papers:

F.-K.G., Hanhart, Meißner, Phys.Rev.Lett.103(2009)082003; Phys.Rev.Lett.105(2010)162001

F.-K.G., Hanhart, Li, Meißner, Zhao, Phys. Rev. D82(2010)034025; Phys. Rev. D83(2011)034013

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 $m_u/m_d$  from heavy quarkonia transitions

# $m_u/m_d$ : $\psi' ightarrow J/\psi \pi^0(\eta)$ vs light meson masses

The decays  $\psi' \rightarrow J/\psi \pi^0$  and  $\psi' \rightarrow J/\psi \eta$  were widely used to extract light quark mass ratio. Ioffe (1979), loffe, Shifman (1980), Donoghue, Wyler (1992), Leutwyler (1996),...



 $\begin{array}{l} \text{QCD multipole expansion } (\lambda_{\text{gluon}} \gg r_{Q\bar{Q}}) \Rightarrow \\ R_{\pi^0/\eta} \equiv \frac{\Gamma\left(\psi' \rightarrow J/\psi \pi^0\right)}{\Gamma(\psi' \rightarrow J/\psi \eta)} = \left(\frac{\left\langle 0 \right| G\tilde{G} \right| \pi^0}{\left\langle 0 \right| G\tilde{G} \right| \eta} \right)^2 \frac{q_{\pi}^3}{q_{\eta}^3} \\ \text{axial anomaly} \Rightarrow \qquad \text{Donoghue, Wyler (1992)} \\ \left\langle 0 \left| G\tilde{G} \right| \pi^0 \right\rangle = \frac{3f^2}{2F_{\pi}}(m_u - m_d) + \mathcal{O}(p^4) \\ \left\langle 0 \left| G\tilde{G} \right| \eta \right\rangle = \frac{2f^2}{\sqrt{2F_{\pi}}}(\tilde{m} - m_s) + \mathcal{O}(p^4), \quad \tilde{m} \equiv \frac{m_u - m_d}{2} \end{array}$ 

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Large discrepancy, why?

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# Non-multipole effects

Intermediate loops: non-multipole effects:

Lipkin, Tuan, PLB206(1988)349 Moxhay, PRD39(1989)3497 Zhou, Kuang, PRD44(1991)756



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Many evidences for Importance of heavy meson loops in heavy quarkonia decays:

- the M1 radiative transitions between two charmonia
- the  $\psi(3770)$  non- $D\overline{D}$  decays
- the  $\Upsilon(5S)$  dipion transitions
- ..., see talk by Q. Zhao

Li, Zhao (2008)

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How to set up an EFT for heavy meson loops in heavy quarkonia transitions?

Li, Zhao (2008)

Liu, Zhang, Li (2009), Zhang, Li, Zhao (2009)

Meng, Chao (2008)

# **Charmed meson loops**





F.-K.G., Hanhart, Meißner, PRL102(2009)242004; F.-K.G., Hanhart, Li, Meißner, Zhao, PRD83(2011)034013

# Lagrangians

 $\begin{array}{l} J = \vec{\psi} \cdot \vec{\sigma} + \eta_c \text{:} & \text{field for the } S \text{ wave charmonia } J/\psi \text{ and } \eta_c \\ H_a = \vec{V}_a \cdot \vec{\sigma} + P_a \text{:} & \text{field for the charmed mesons } D_{(s)} \text{ and } D^*_{(s)} \\ \bar{H}_a = -\vec{V}_a \cdot \vec{\sigma} + \bar{P}_a \text{: field for the anti-charmed mesons} \end{array}$ 

The coupling of charmonia to the charmed and anti-charmed mesons:

Colangelo et al. (2004), F.-K.G., Hanhart, Meißner (2009)

$$\mathcal{L}_{\psi} = i \frac{g_2}{2} \operatorname{Tr} \left[ J^{\dagger} H_a \vec{\sigma} \cdot \stackrel{\leftrightarrow}{\partial} \bar{H}_a \right] + \text{h.c.}$$

The coupling of the charmed mesons to the Goldstone bosons:

Burdman, Donoghue (1992), Wise (1992), Yan et al. (1992), Hu, Mehen (2006)

$$\mathcal{L}_{\phi} = -\frac{g}{2} \operatorname{Tr} \left[ H_{a}^{\dagger} H_{b} \vec{\sigma} \cdot \vec{u}_{ba} \right], \qquad \vec{u}_{ba} = -\sqrt{2} \frac{\partial \phi_{ba}}{F} + \dots$$

Heavy quark spin symmetry relates the couplings for the heavy mesons within the same spin multiplet.

 $2M_D - M_{c\bar{c}} \sim \Lambda_{\rm QCD} \ll M_D \Rightarrow$  Nonrelativistic in charmed meson velocity  $v \sim \sqrt{\frac{|2M_D - M_{c\bar{c}}|}{M_D}}$ 



 $v \approx$  0.5: charmed meson velocity

Including scaling of the coupling constants does not spoil the picture.

### **Tree-level**



LO chiral Lagrangian for the charmonia and Goldstone bosons 

Casalbuoni et al. (1993)

$$\mathcal{L}_{SS} = \frac{\gamma}{4} \left( \operatorname{Tr} \left[ J' \sigma^{i} J^{\dagger} \right] - \operatorname{Tr} \left[ J^{\dagger} \sigma^{i} J' \right] \right) \partial^{i} (\chi_{-})_{aa}$$

$$= \frac{4A}{F} \epsilon^{ijk} \psi^{\prime j} \psi^{k\dagger} \partial^{i} \left[ \frac{3}{2} B_{0} (m_{d} - m_{u}) \pi^{0} + \frac{2}{\sqrt{3}} B_{0} (m_{s} - \bar{m}) \eta \right] + \dots$$

$$J = \vec{\psi} \cdot \vec{\sigma} + \eta_{c}, \ J' = \vec{\psi'} \cdot \vec{\sigma} + \eta'_{c}, \ \text{and} \ \chi_{-} = u^{\dagger} \chi u^{\dagger} - u \chi^{\dagger} u.$$
Heavy quark spin symmetry breaking, isospin / SU(3) breaking  $(\pi^{0} - \eta \text{ mixing included}$ 
QCDME result reproduced.

### **Tree-level**



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Amplitude:  $\mathcal{M}(\psi' \to J/\psi\pi^{0}) \propto (m_{d} - m_{u})q_{\pi}$ 

Loops:  $\frac{1}{v}\Delta q_{\pi}$ ,  $\Delta = M_{D^+} - M_{D^0} \sim m_d - m_u$ . Loops are enhanced by a factor of  $\frac{1}{v}!$ 

Mass differences of the intermediate charmed mesons give isospin / SU(3) breaking.

• For  $\psi' \to J/\psi\eta$ , SU(3) breaking, charged, neutral and strange charmed mesons contribute:

$$\mathcal{M}(\psi' 
ightarrow {J}/\psi \eta) \propto \epsilon^{ijk} {m q}^i_\eta arepsilon^j_{\psi'} arepsilon^k_{J/\psi} rac{1}{\sqrt{3}} ({\it l_c}+{\it l_n}-2{\it l_s}),$$

Loop functions  $I_c$ ,  $I_n$  and  $I_s$  are for the charged, neutral and strange charmed mesons, respectively. Spin symmetry also broken.

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• For  $\psi' \to J/\psi \pi^0$ , isospin breaking, charged and neutral charmed mesons contribute, and  $\pi^0 - \eta$  mixing also contributes:

$$\mathcal{M}(\psi' \to J/\psi\pi^0) \propto \epsilon^{ijk} q^i_{\pi} \varepsilon^j_{\psi'} \varepsilon^k_{J/\psi} \left[ (I_c - I_n) + \frac{\epsilon_{\pi^0\eta}}{\sqrt{3}} (I_c + I_n - 2I_s) \right],$$

 $\epsilon_{\pi^0\eta}:\pi^0-\eta$  mixing angle

# **Results**

Can we get sensible results considering only the contribution from the meson loops?

• Comparing with data. Our result

$$egin{aligned} R_{\pi^0/\eta} &= rac{\Gamma\left(\psi' 
ightarrow J/\psi\pi^0
ight)}{\Gamma\left(\psi' 
ightarrow J/\psi\eta
ight)} = 0.11 \pm 0.06 \end{aligned}$$

Data	$R_{\pi^0/\eta}$
CLEO(2008)	$(3.88 \pm 0.23 \pm 0.05)\%$
BES(2004)	$(4.8 \pm 0.5)\%$
PDG(2008) fit	$(4.0\pm0.3)\%$

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Comparing the extracted coupling constant with models

PDG:  $\Gamma(\psi' \rightarrow J/\psi\pi^0) = 0.40 \pm 0.03 \text{ keV}$  $\Gamma(\psi' \rightarrow J/\psi\eta) = 10.0 \pm 0.4 \text{ keV}$ 

 $\Rightarrow \sqrt{g_{\psi DD}g_{\psi' DD}} = 6...8$ 

Models	$g_{\psi DD}$	Refs.
QCD sum rules	$8.2\pm1.3$	Matheus et al (2002)
VMD	7.7	Matinyan, Müller (1998)
VMD	$8.0 \pm 0.5$	Deandrea et al (2003)

Solution of the puzzle:

The value of  $m_u/m_d$  extracted from the  $\psi' \rightarrow J/\psi \pi^0(\eta)$  is NOT reliable since it suffers from very large meson loop contributions!

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• Role of the charmed loops in other charmonia transitions?

# Charmonia transitions with the emission of one pion / eta

F.-K.G., Hanhart, Li, Meißner, Zhao, PRD83(2011)034013



- ♡ SS transitions Enhancement of loops
- ♡ PP transitions Enhancement of loops
- ♡ SP transitions Process dependent, sometimes high suppression

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 $m_u/m_d$  from heavy quarkonia transitions

*PP* transitions: Loops enhanced by  $1/v^3$ !

Ratios of decay widths  $R_{mn12} \equiv \frac{\Gamma(\chi'_{cm} \to \chi_{cn} \pi^0)}{\Gamma(\chi'_{c1} \to \chi_{c2} \pi^0)}$ : free of any parameter.

Comparison of the loop results with the tree-level results - testable



F.-K.G., Hanhart, Li, Meißner, Zhao, PRD82(2010)034025; PRD83(2011)034013

• 
$$J^{PC}(\psi') = 1^{--}, J^{PC}(h_c) = 1^{+-}, S$$
-wave decay:

Tree-level amplitude  $\propto (m_d - m_u)$ 

F.-K.G., Hanhart, Li, Meißner, Zhao, PRD82(2010)034025; PRD83(2011)034013

- $J^{PC}(\psi') = 1^{--}, J^{PC}(h_c) = 1^{+-}, S$ -wave decay: Tree-level amplitude  $\propto (m_d - m_u)$
- Charmed meson loops:



Charmed meson loops are highly suppressed here, confirmed by explicit calculation.

F.-K.G., Hanhart, Meißner, PRL105(2010)162001

 $\Upsilon(4S)$ : radial excitation of the S-wave vector bottomonium  $M_{\Upsilon(4S)} = 10.579 \text{ GeV}$ 

*h<sub>b</sub>*: *P*-wave ground state 1<sup>+-</sup>  $b\bar{b}$ , still missing  $M_{h_b} = \frac{1}{9}(M_{\chi_{b0}} + 3M_{\chi_{b1}} + 5M_{\chi_{b2}}) = 9.900 \text{ GeV}$ 

See, e.g., Godfrey, Rosner (2002)

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For  $\Upsilon(4S) \to h_b \pi^0(\eta)$ ,  $v \approx 0.3$ , there are two different suppressions:

- $q_{\pi(\eta)}^2/(v^3 M_B^2) \approx 0.6(0.2)$
- $\Delta = M_{B^0} M_{B^+} = 0.33 \pm 0.06 \text{ MeV} \ll m_d m_u$

This is due to the destructive interference between the e.m. and strong contributions F-K.G., Hanhart, Meißner, JHEP09(2008)136

 $\Upsilon(4S) \rightarrow h_b \pi^0(\eta)$  can be used to extract the light quark mass ratio!

• Multipole contribution dominates  $\Rightarrow$ 

$$\frac{\Gamma(\Upsilon(4S) \to h_b \pi^0)}{\Gamma(\Upsilon(4S) \to h_b \eta)} = r_{G\tilde{G}}^2 \left| \frac{\vec{q}_{\pi}}{\vec{q}_{\eta}} \right| \qquad \text{with } r_{G\tilde{G}} \equiv \frac{\langle 0|G\tilde{G}|\pi^0 \rangle}{\langle 0|G\tilde{G}|\eta \rangle}$$

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From CHPT with U(1)<sub>A</sub> anomaly, the NLO expressions for (0|GG
 <sup>(η)</sup>) have been worked out.
 Donoghue, Wyler (1992)

Extracting the combined light quark mass ratio:

$$\frac{m_d - m_u}{m_d + m_u} \frac{m_s + \hat{m}}{m_s - \hat{m}} = \frac{4}{3\sqrt{3}} r_{G\tilde{G}} \frac{F_{\pi}}{F_{\eta}} \frac{F_{\kappa}^2 M_{\kappa}^2 - F_{\pi}^2 M_{\pi}^2}{F_{\pi}^2 M_{\pi}^2} (1 - \delta_{\text{GMO}}) \left[ 1 + \frac{4L_{14}}{F_{\pi}^2} (M_{\eta}^2 - M_{\pi}^2) \right]$$

 $\mathcal{O}(p^4)$  Deviation from Gell-Mann–Okubo relation:  $\delta_{\text{GMO}} = -0.06$ Resonance saturation  $\Rightarrow L_{14} = (2.3 \pm 1.1) \times 10^{-3}$ 

# Theoretical uncertainty due to loops can be reduced

Considering only the bottom meson loops,

$$\Gamma(\Upsilon(4S) \rightarrow h_b \eta)^{\text{loop}} = 0.16g_{1b}^2 \text{ keV}$$

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• How to measure  $g_{1b}^2$ :

$$\begin{split} R_{01} &\equiv \ \frac{\Gamma(\chi_{b0}(4P) \to \chi_{b1}\eta)}{\Gamma(\chi_{b0}(4P) \to B^{+}B^{-})}, \quad R_{1J} \equiv \frac{\Gamma(\chi_{b1}(4P) \to \chi_{bJ}\eta)}{\Gamma(\chi_{b1}(4P) \to B^{+}B^{*-})}, \ [J = 0, 1, 2], \\ R_{2J} &\equiv \ \frac{\Gamma(\chi_{b2}(4P) \to \chi_{bJ}\eta)}{\Gamma(\chi_{b2}(4P) \to B^{*+}B^{*-})}, \ [J = 1, 2]. \end{split}$$

#### All the ratios are proportional to $g_{1b}^2$ .



# Summary and outlook

- Having available an EFT that allows one to study both direct transitions as well as those mediated via heavy loops
- The charmed meson loops play an important role in the decays  $\psi' \rightarrow J/\psi \pi^0(\eta)$ . Hence the previous extraction of light quark mass ratio from these decays is not reliable.
- $m_u/m_d$  can be extracted from the  $\Upsilon(4S) \rightarrow h_b \pi^0(\eta)$

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#### Outlook:

- Radiative transitions of heavy quarkonia
- Dipion transitions between two heavy quarkonia
- Higher orders
- To be tested at BES-III, PANDA, LHC-b, ...

If taking into account the scaling of coupling constants



For details, see Guo et al, PRD83(2011)034013