

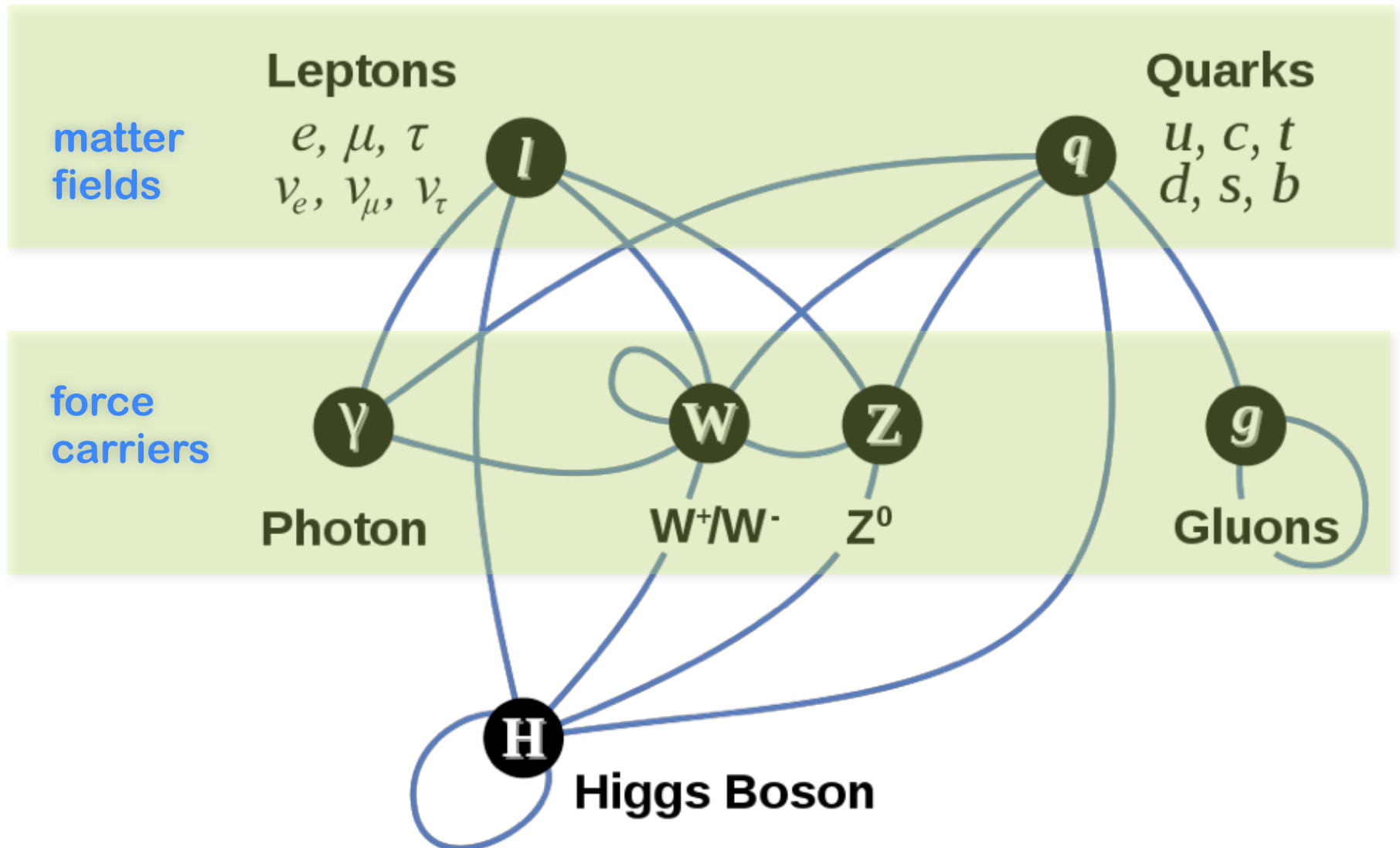
Chiral dynamics: From hadrons to nuclei

Outline

- Introduction
- Chiral perturbation theory
- Nuclear forces and light nuclei
- Few-N physics with external probes
- Nuclear dynamics on the lattice: the Hoyle state
- Summary & outlook

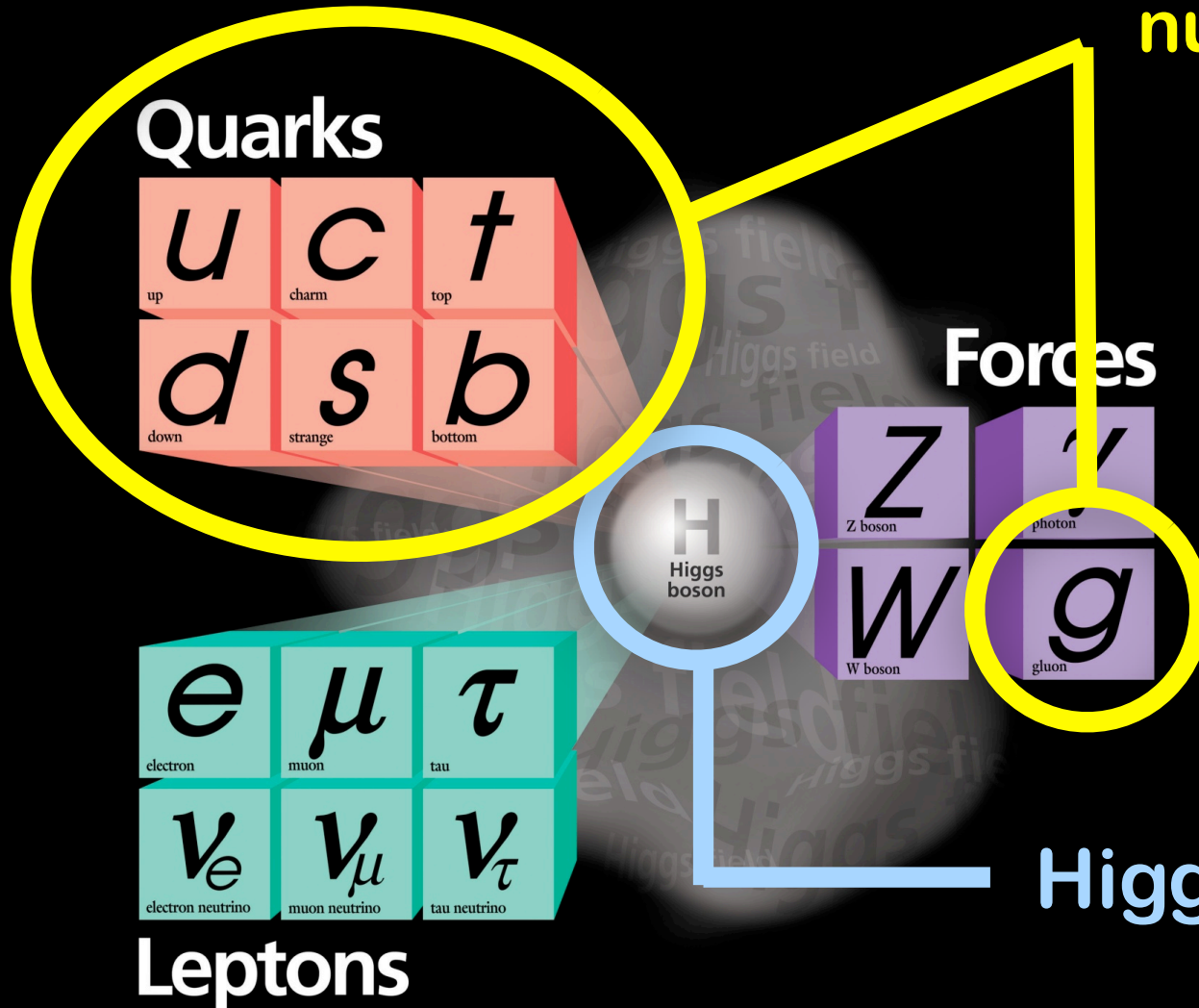


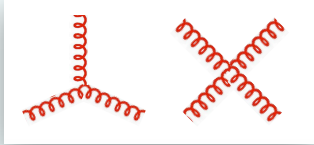
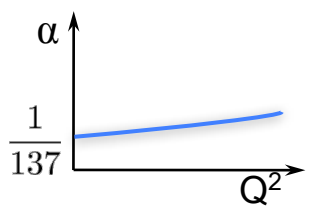
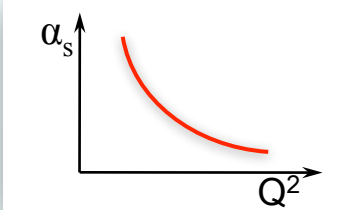
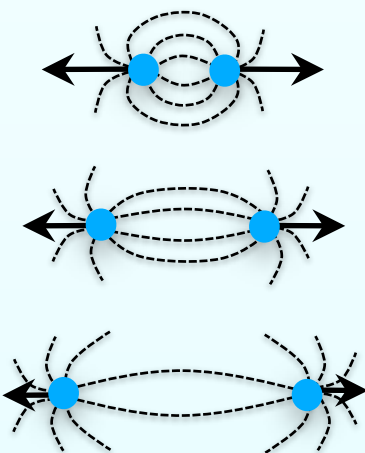
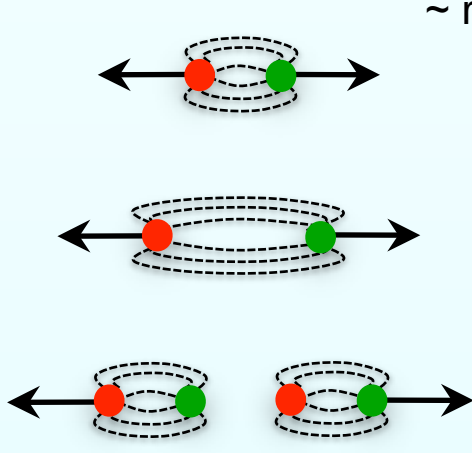
The Standard Model



Open questions within the SM

QCD \leftrightarrow hadron & nuclear physics



| | QED | QCD |
|--------------------|--|---|
| matter particles | leptons (e, μ , τ) | quarks (u, d, s, c, b, t) |
| force couples to | electromagnetic charge | 3 color charges (r,g,b) |
| exchange particles | photons (uncharged) | gluons (charged)  |
| coupling constant | increases as energy grows  | decreases as energy grows  |
| observed particles | leptons, photons | hadrons (bound states of quarks and gluons) |
| energy density |  $\sim 1/r$ |  $\sim r$ |

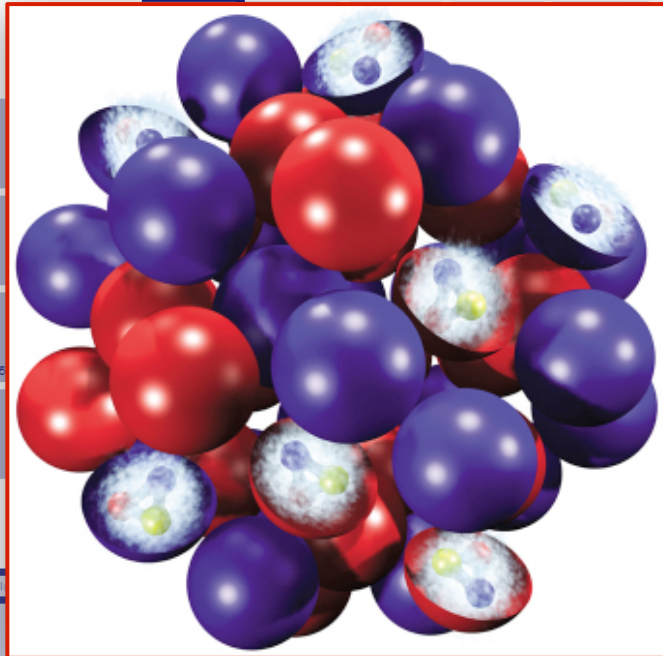
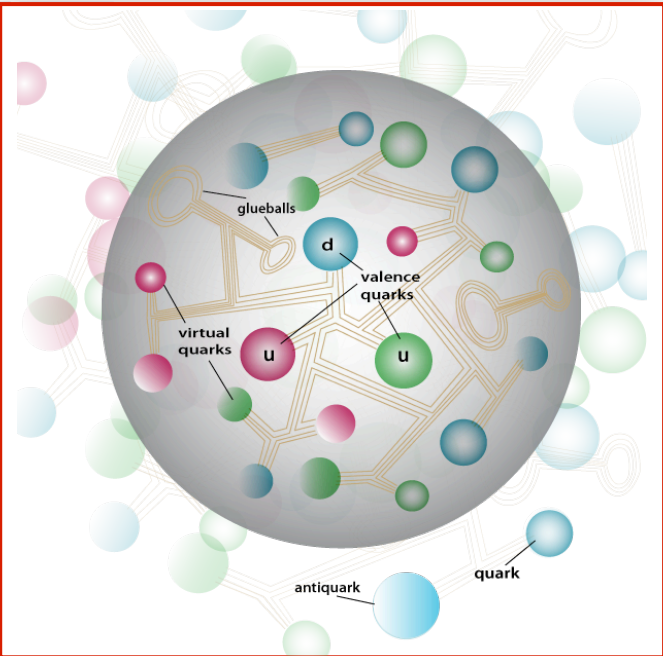
Quantum Chromodynamics (QCD)

Periodensystem der Elemente

Legend:

- Alkalimetalle
- Erdalkalimetalle
- Übergangsmetalle
- Lanthanoide
- Actinoide
- Metalle
- Nichtmetalle
- Edelgase
- C** Solid
- Br** Liquid
- H** Gas
- Tc** Synthetic

| | | | | | | | | | | | | | | | | |
|----------------------------------|----------------------------------|-------------------------|----------------------------------|----------------------------------|---------------------------------|-------------------------------|-----------------------------|--|--|--|--|--|--|--|--|-------------|
| 1 IA | New Original | | | | | | | | | | | | | | | 18 VIIIA |
| 1 H Wasserstoff 1.00784 | 2 He Helium 4.002602 | | | | | | | | | | | | | | | |
| 3 Li Lithium 6.941 | 4 Be Beryllium 9.012182 | | | | | | | | | | | | | | | |
| | | 13 IIIA | 14 IVA | 15 VA | 16 VIA | 17 VIIA | | | | | | | | | | |
| | | 5 B Bor 10.811 | 6 C Kohlenstoff 12.0107 | 7 N Stickstoff 14.00674 | 8 O Sauerstoff 15.9994 | 9 F Fluor 18.9984032 | 10 Ne Neon 20.1797 | | | | | | | | | |
| 11 Na Natrium 22.989770 | | | | | | | | | | | | | | | | 18 VIIIA |
| | | | | | | | | | | | | | | | | |
| 19 K Kalium 39.0983 | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | |
| 37 Rb Rubidium 85.4678 | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | |
| 55 Cs Cäsium 132.90545 | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | |
| 87 Fr Francium (223) | | | | | | | | | | | | | | | | |



Note: The subscripts numbers 1-18 in 1984 by the International Union of Pure and Applied Chemistry. The names of elements 112-118 are the Latin equivalents of those numbers.

nucleon

nucleus

Effective Field Theories

What is effective?

Effective (field) theories = approximate theories to describe phenomena which occur at a chosen length/energy range.

Example: multipole expansion for electric potentials

Electric potential from a localized charge distribution:

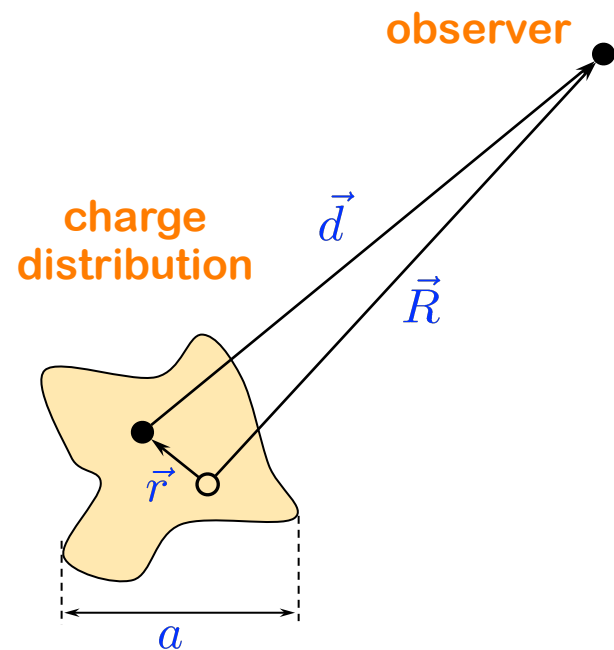
$$V(\vec{R}) \propto \int d^3r \frac{\rho(\vec{r})}{|\vec{R} - \vec{r}|}$$

Only moments of $\rho(\vec{r})$ are needed to determine $V(\vec{R})$ at large distances ($a \ll R$):

$$V(\vec{R}) = \frac{q}{R} + \frac{1}{R^3} \sum_i R_i P_i + \frac{1}{6R^5} \sum_{ij} (3R_i R_j - \delta_{ij} R^2) Q_{ij} + \dots$$

with the moments („low-energy constants”):

$$q = \int d^3r \rho(\vec{r}), \quad P_i = \int d^3r \rho(\vec{r}) r_i, \quad Q_{ij} = \int d^3r \rho(\vec{r}) (3r_i r_j - \delta_{ij} r^2).$$



Scales in nuclear physics

The EFT „recipe“

1. Most general effective Lagrangian for the relevant DOF
Symmetries!
2. Compute observables via expansion in $\Lambda_{\text{soft}} / \Lambda_{\text{hard}}$

hard scales

m_N

$m_{\rho,\omega}$

chiral EFT (DOF: π , N, Δ)

$m_\Delta - m_N$

M_π

B_{deut}

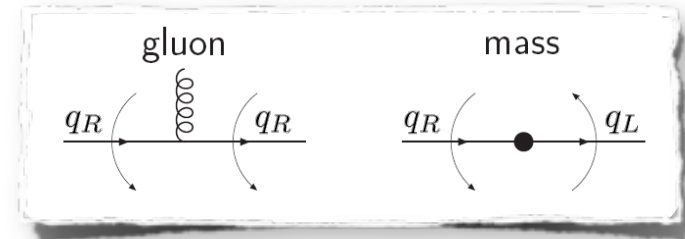
pionless EFT (DOF: N)

ChPT (DOF: π , N)

Chiral perturbation theory

QCD and chiral symmetry

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}G_{\mu\nu}G^{\mu\nu} + \underbrace{\bar{q}_L i \not{D} q_L + \bar{q}_R i \not{D} q_R}_{\text{SU}(2)_L \times \text{SU}(2)_R \text{ invariant}} - \underbrace{\bar{q}_L \mathcal{M} q_R - \bar{q}_R \mathcal{M} q_L}_{\text{break chiral symmetry}}$$



Light quark masses ($\overline{\text{MS}}, \mu = 2 \text{ GeV}$):

$$\begin{aligned} m_u &= 1.5 \dots 3.3 \text{ MeV} \\ m_d &= 3.5 \dots 6.0 \text{ MeV} \end{aligned} \ll \Lambda_{\text{QCD}} \sim 220 \text{ MeV}$$

→ \mathcal{L}_{QCD} is approx. $\text{SU}(2)_L \times \text{SU}(2)_R$ invariant

spontaneous breakdown to $\text{SU}(2)_V \subset \text{SU}(2)_L \times \text{SU}(2)_R$ → Goldston Bosons (pions)

Chiral perturbation theory

- Ideal world [$m_u = m_d = 0$], zero-energy limit: non-interacting massless GBs (+ strongly interacting massive hadrons)
- Real world [$m_u, m_d \ll \Lambda_{\text{QCD}}$], low energy: weakly interacting light GBs (+ strongly interacting massive hadrons)

→ expand about the ideal world (ChPT)

Chiral perturbation theory

Effective Lagrangian for hadronic DOF (π , N, ...) Chiral symmetry!

pion decay constant (in the chiral limit)
 $F_\pi \sim 94 \text{ MeV}$

pion fields

quark mass matrix

$$\mathcal{L}_\pi^{(2)} = \frac{F_\pi^2}{4} \left[\text{Tr}(\partial_\mu U \partial^\mu U^\dagger) + \text{Tr}(U\chi + U^\dagger\chi) \right], \quad \text{where } \chi = 2BM.$$

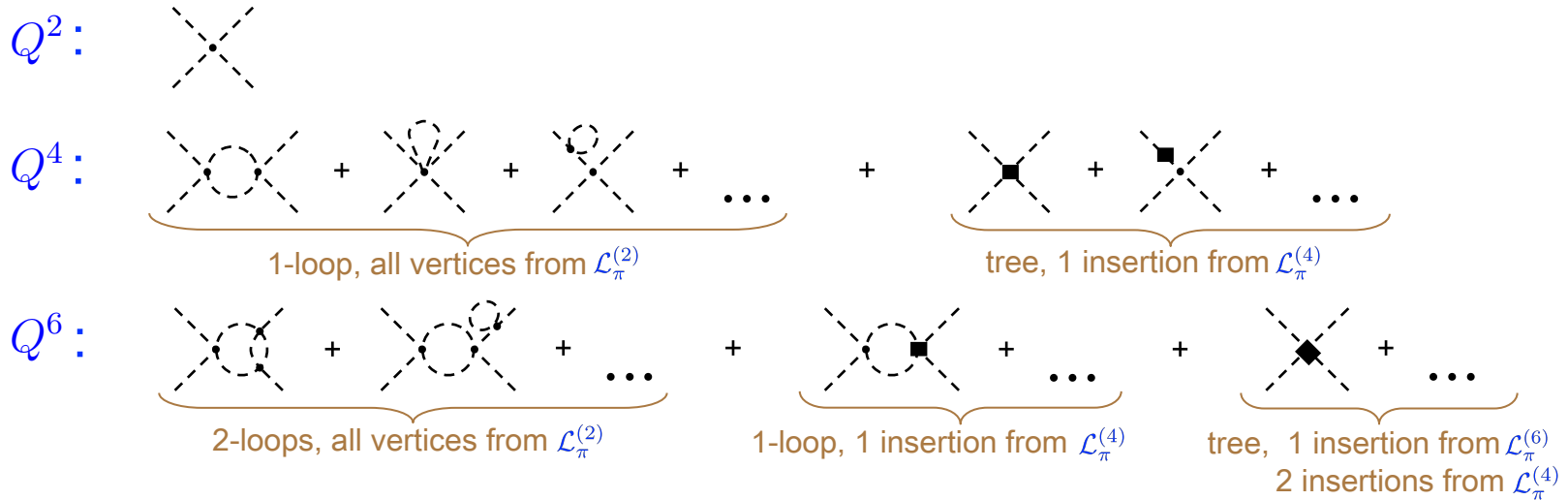
$$\mathcal{L}_\pi^{(4)} = L_1 [\text{Tr}(\partial_\mu U^\dagger \partial^\mu U)]^2 + L_2 \text{Tr}(\partial_\mu U^\dagger \partial_\nu U) \text{Tr}(\partial^\mu U^\dagger \partial^\nu U) + \dots + L_8 \text{Tr}(\chi U \chi U + \chi U^\dagger \chi U^\dagger)$$

low-energy constants

Gasser, Leutwyler '84

- Low-energy observables computable via a **perturbative expansion** in $Q = \frac{p \sim M_\pi}{\Lambda_\chi}$
Weinberg '79
hard scale that enters L_i
- At any order Q^n , a **finite number of (unknown) LECs** contribute

Pion scattering lengths in ChPT



Predictive power?

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\pi}^{(2)} + \mathcal{L}_{\pi}^{(4)} + \mathcal{L}_{\pi}^{(6)} + \dots$$

of LECs increasing...

S-wave $\pi\pi$ scattering length

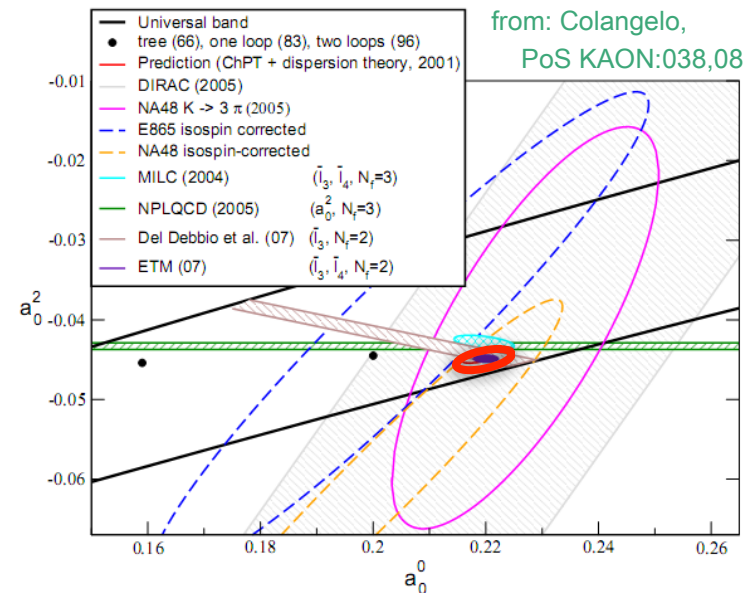
LO: $a_0^0 = 0.16$ (Weinberg '66)

NLO: $a_0^0 = 0.20$ (Gasser, Leutwyler '83)

NNLO: $a_0^0 = 0.217$ (Bijnens et al. '95)

NNLO + disp. relations: (Colangelo et al.)

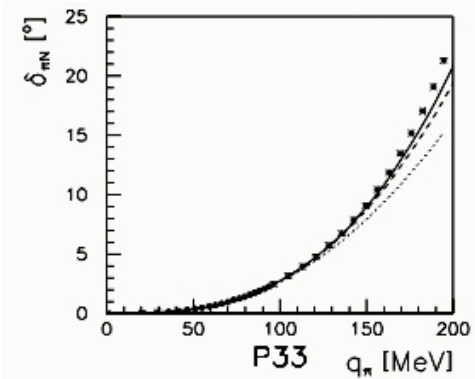
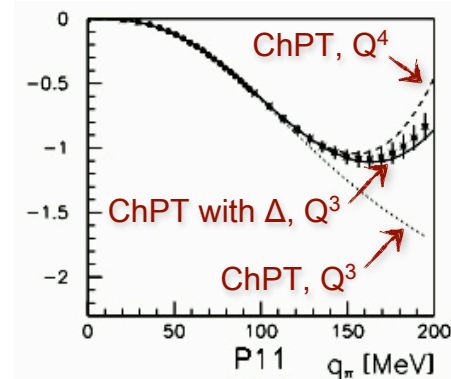
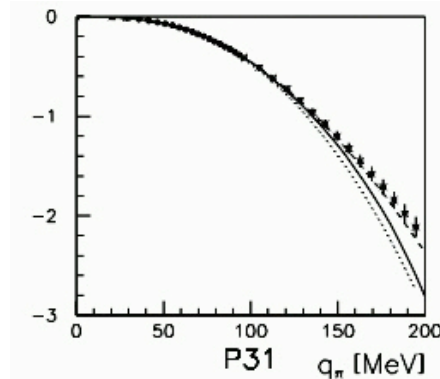
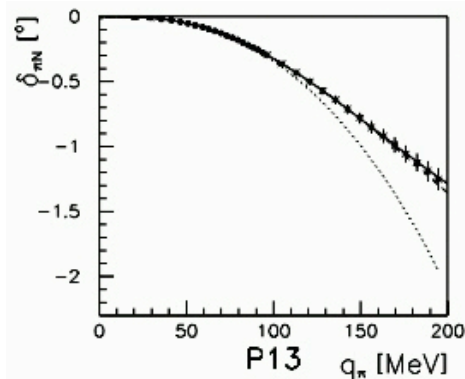
$a_0^0 = 0.217 \pm 0.008$ (exp) ± 0.006 (th)



Pion-nucleon scattering

Pion-nucleon scattering in heavy-baryon ChPT

Fettes, Meißner '01

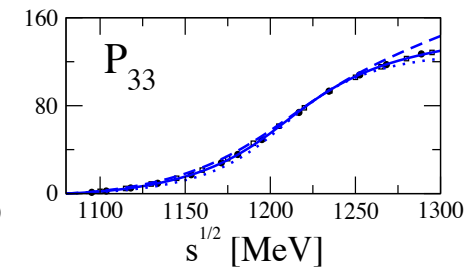
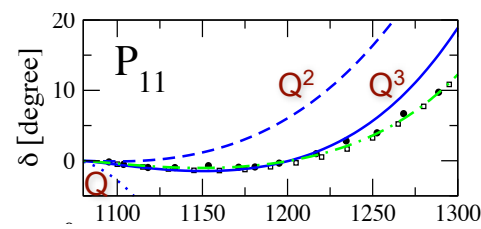


Some recent developments

- ChEFT with explicit $\Delta(1232)$ DOF
Hemmert, Meißner, Pascalutsa, EE, Krebs, ...
- covariant formulations
Alarcon, Camalich, Oller, ...
- unitarized ChPT
Gasparyan, Lutz

πN scattering in Unitarized ChPT

Gasparyan, Lutz '11



Few nucleons

Low-energy NN interaction is strong (shallow bound states) \rightarrow need nonperturbative methods

Simplification: nonrelativistic problem ($|\vec{p}_i| \sim M_\pi \ll m_N$) \rightarrow the QM A-body problem...

Weinberg '91,'92

$$\left[\left(\sum_{i=1}^A \frac{\vec{\nabla}_i^2}{2m_N} + \mathcal{O}(m_N^{-3}) \right) + \underbrace{V_{2N} + V_{3N} + V_{4N} + \dots}_{\text{derived within in ChPT}} \right] |\Psi\rangle = E|\Psi\rangle$$

Derivation methods:

- matching to the amplitude Kaiser, van Kolck, Friar, Higa, Robilotta, ...
- decoupling of pions & nucleons via a UT EE, Glöckle, Meissner, Krebs, Bernard

Chiral expansion of the nuclear Hamiltonian:

$$V_{2N} = V_{2N}^{(0)} + V_{2N}^{(2)} + V_{2N}^{(3)} + V_{2N}^{(4)} + \dots \quad \leftarrow \langle V_{2N} \rangle \sim 20 \text{ MeV/pair}$$

$$V_{3N} = V_{3N}^{(3)} + V_{3N}^{(4)} + \dots \quad \leftarrow \langle V_{3N} \rangle \sim 1 \text{ MeV/triplet}$$

$$V_{4N} = V_{4N}^{(4)} + \dots \quad \leftarrow \langle V_{4N} \rangle \sim 0.1 \text{ MeV/quartet}$$

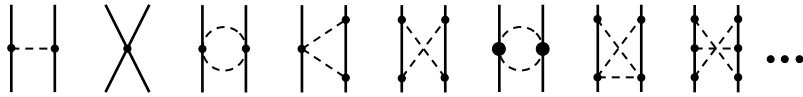
(from Pudliner et al., PRL 74 (95) 4396)

Nucleon-nucleon potential

Ordóñez et al. '94; Friar & Coon '94; Kaiser et al. '97; E.E. et al. '98, '03; Kaiser '99-'01; Higa, Robilotta '03; ...

State of the art: $N^3\text{LO}$ (Q^4) in the χ expansion

Entem-Machleidt, EE-Glöckle-Meissner



- Long-range part: 1π , 2π and 3π exchange (parameter-free: all LECs from πN scattering)
- Short-range part: 24 short-range operators, LECs fixed from NN data
- Isospin-breaking corrections

Further details in recent review articles:

EE, Prog. Part Nucl. Phys. 57 (06) 654

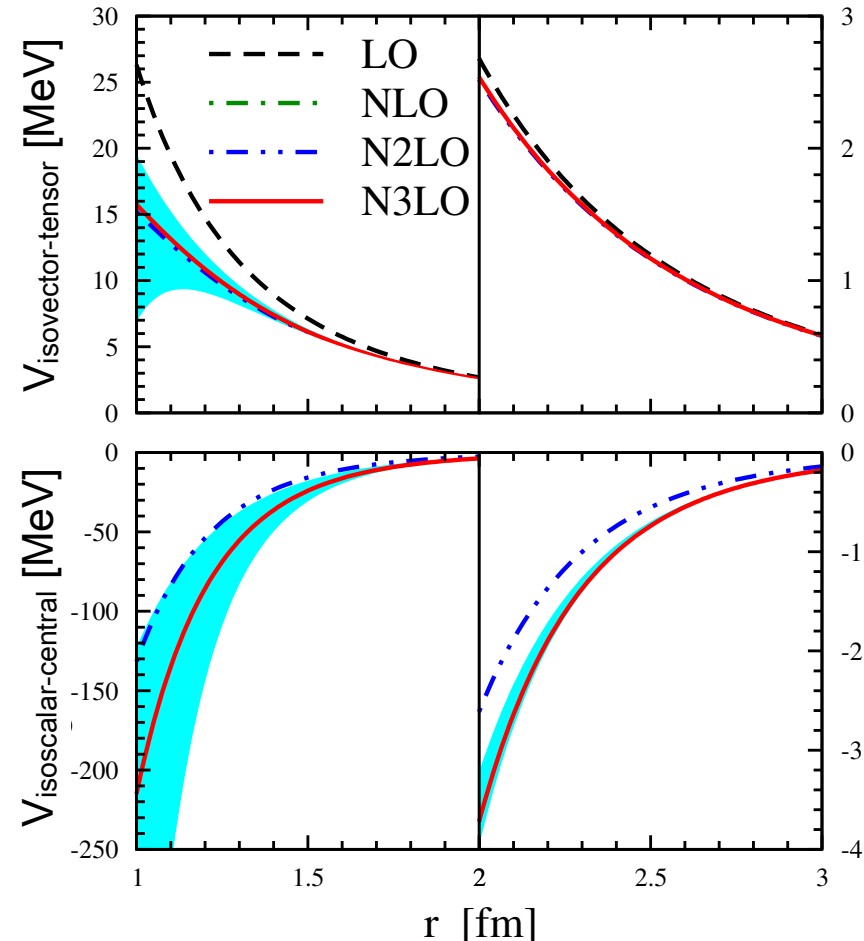
EE, Hammer, Meißner, Rev. Mod. Phys. 81 (09) 1773

Entem, Machleidt, Phys. Rept. 503 (11) 1

EE, Meißner, arXiv:1201.2136,

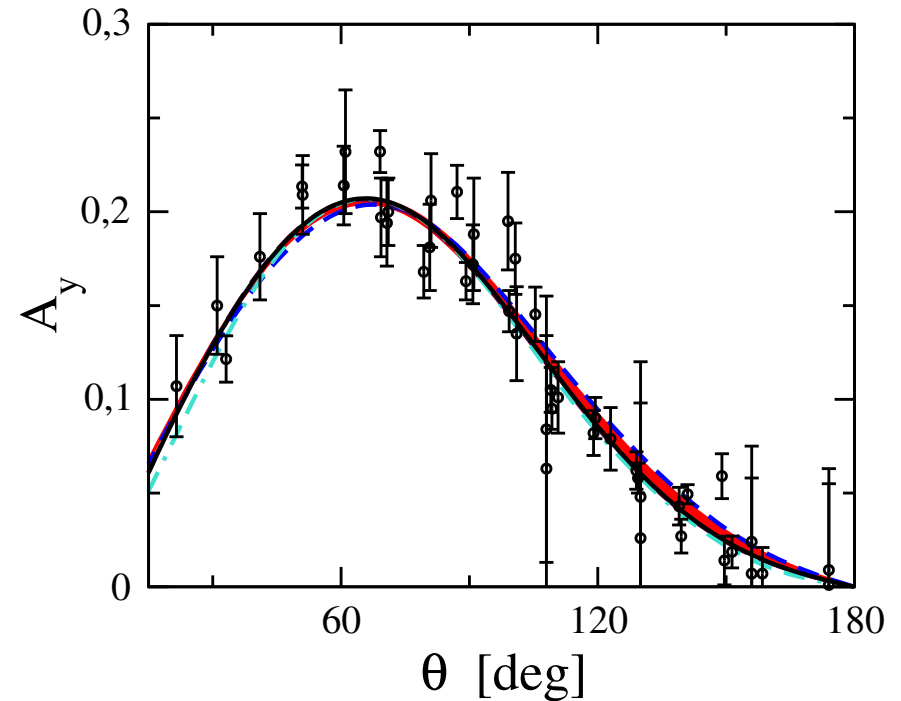
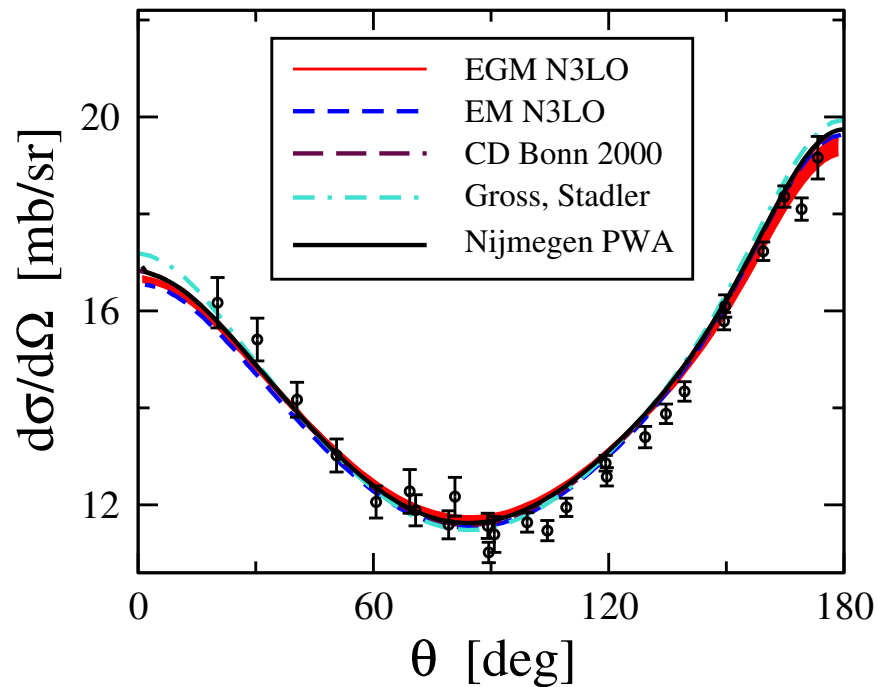
submitted to Ann. Rev. Nucl. Part. Sci.

Chiral expansion of the long-range two-nucleon potential



Nucleon-nucleon scattering

Neutron-proton differential cross section and analyzing power at
 $E_{\text{lab}} = 50 \text{ MeV}$



accurate description of data up to $E_{\text{lab}} \sim 200 \text{ MeV}$ at $N^3\text{LO}$ is
comparable to modern phenomenological potentials

Three-nucleon force

JUNE 15, 1939

PHYSICAL REVIEW

VOLUME 55

Many-Body Interactions in Atomic and Nuclear Systems

H. PRIMAKOFF, *Polytechnic Institute of Brooklyn, Brooklyn, New York*

AND

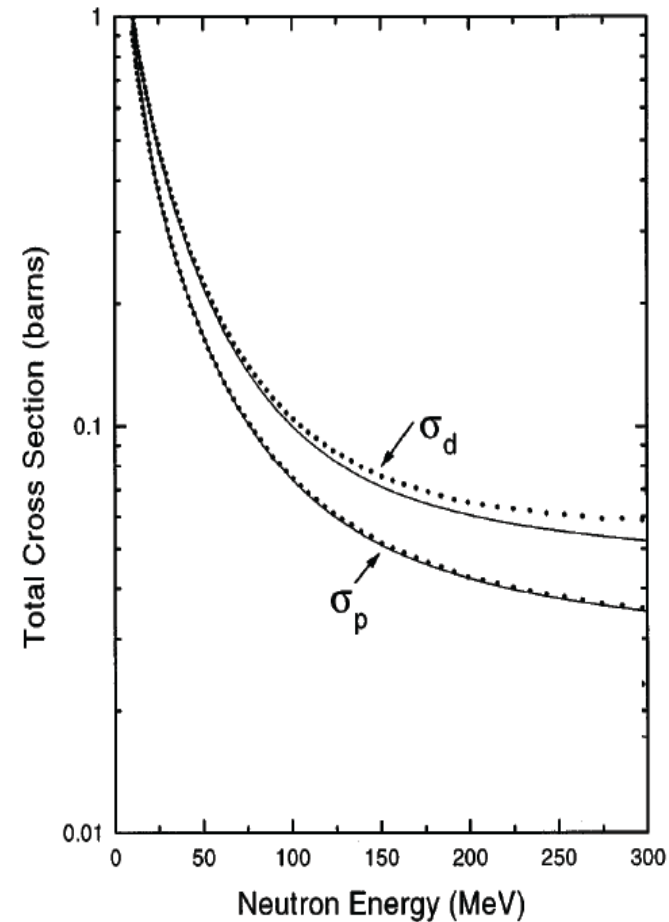
T. HOLSTEIN,* *New York University, University Heights, New York, New York*

(Received March 28, 1938)

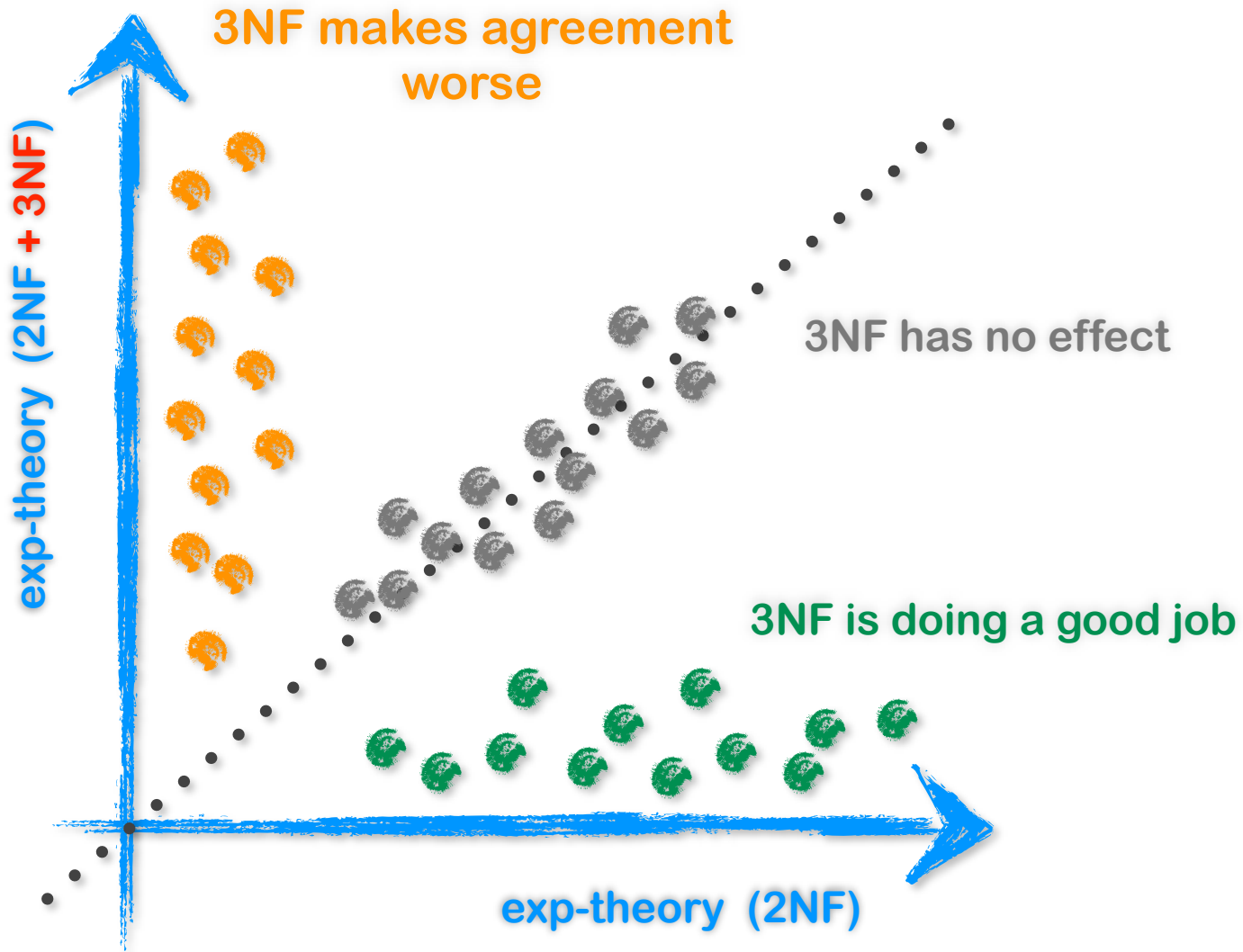
„ ...replacement of field interactions by two-body action-at-a-distance potentials is a poor approximation in nuclear physics.“

Some indications of the 3NF

- ^3H binding energy calculated based on V_{NN} is typically underbound by ~ 1 MeV
- Three-nucleon continuum...

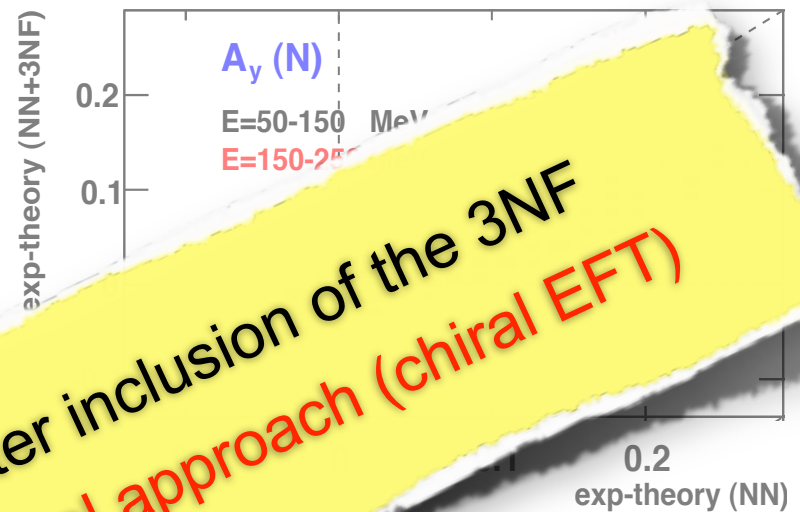
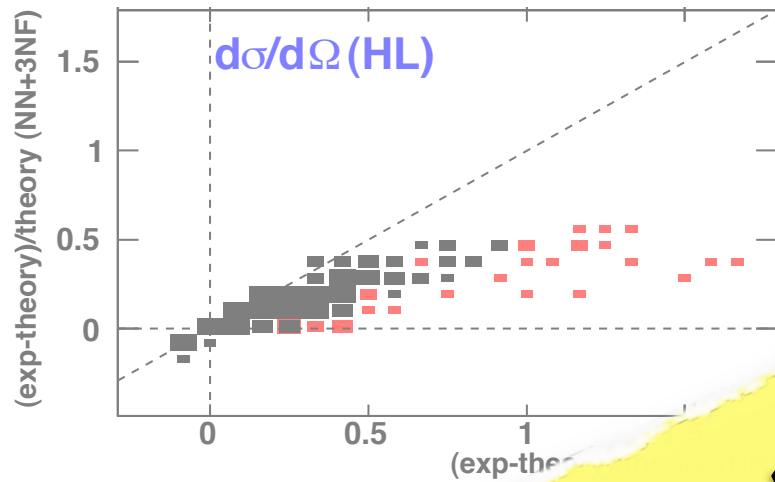


Three-nucleon force

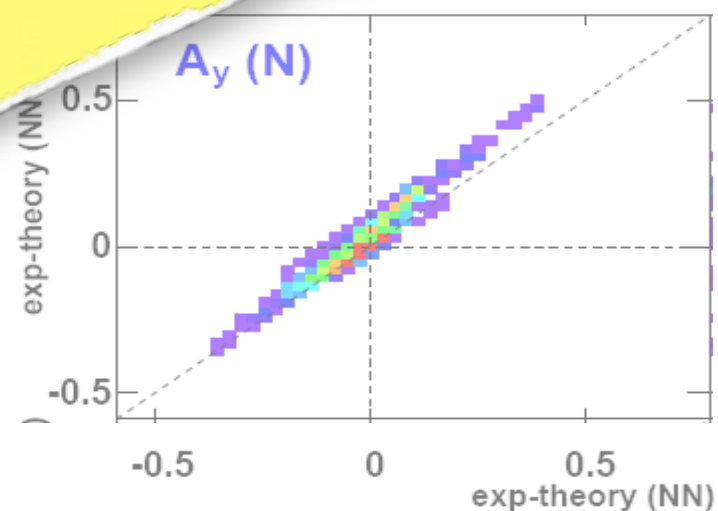
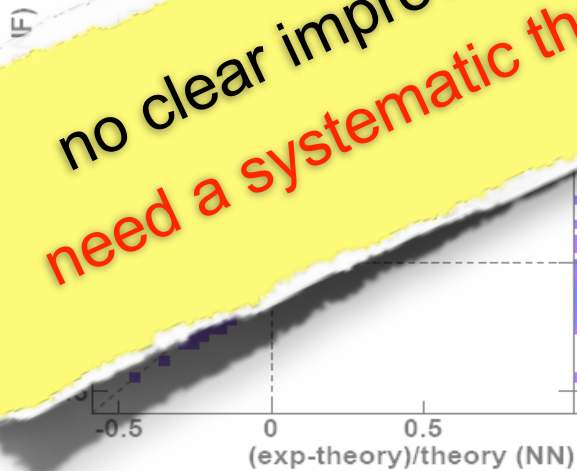


Three-nucleon force

Elastic nucleon-deuteron scattering



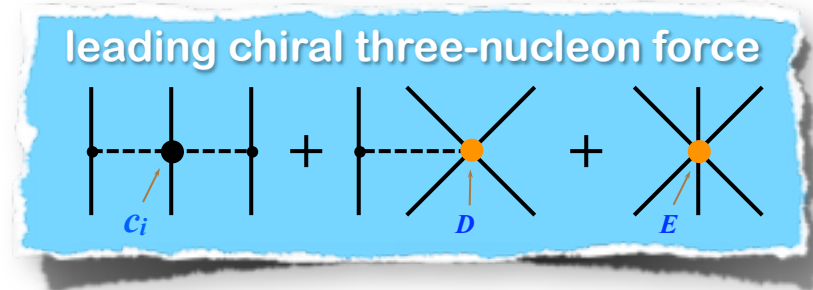
no clear improvement after inclusion of the 3NF
need a systematic theoretical approach (chiral EFT)



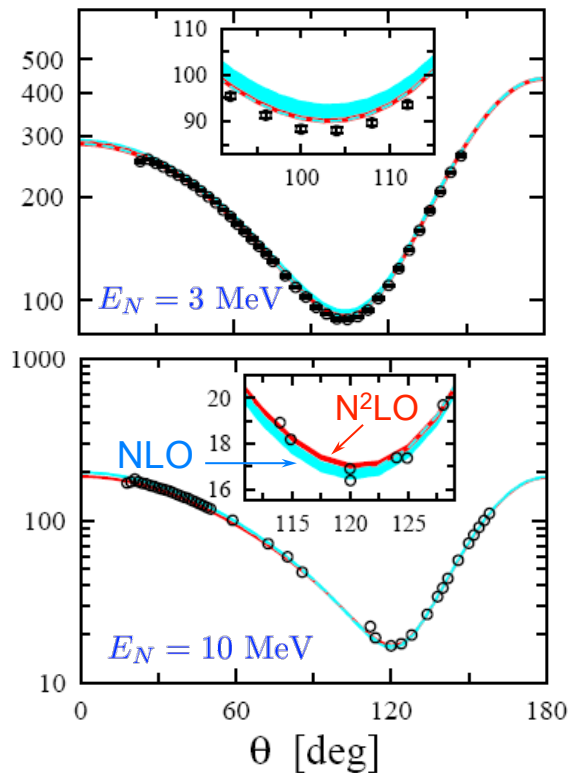
Chiral three-nucleon force

3NF first appears at N²LO

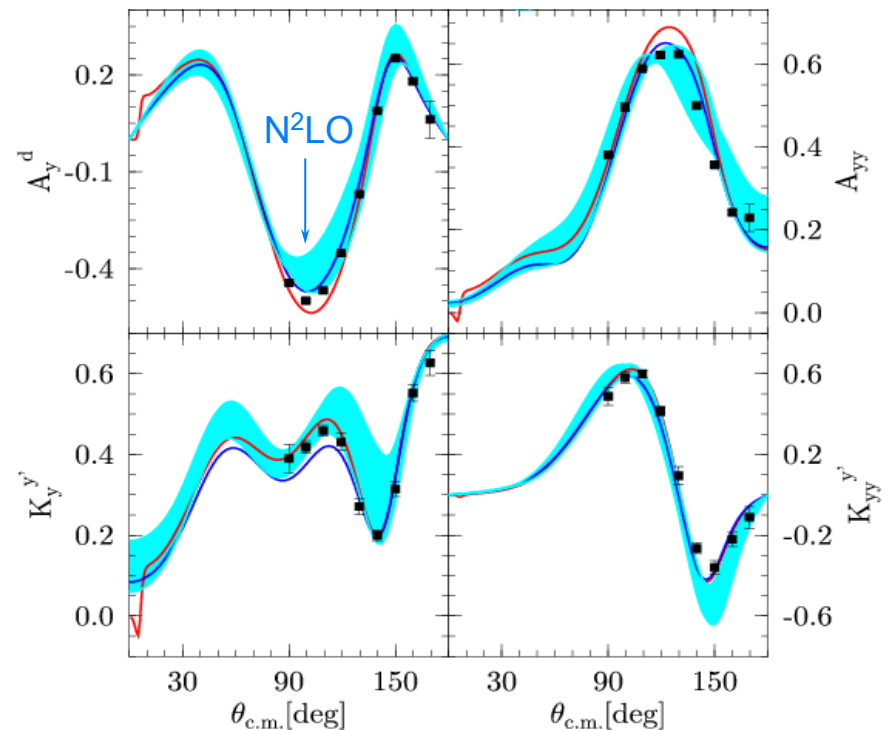
The LECs D, E can be fixed e.g. from ${}^3\text{H}$ BE and nd doublet scattering length [EE, Nogga et al.](#)



Nd elastic cross sections at low energies



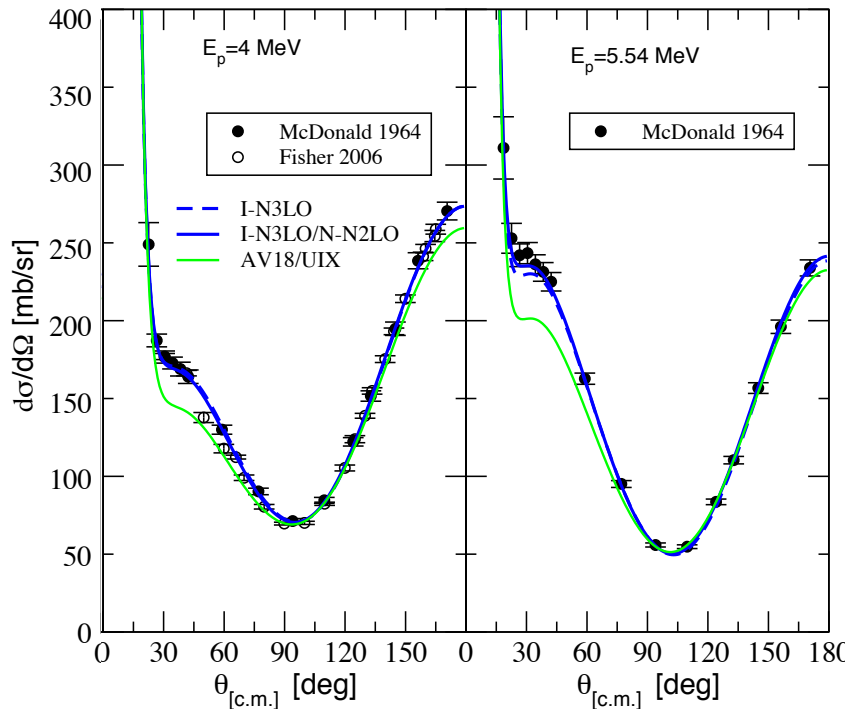
Nd elastic scattering at $E_N = 90 \text{ MeV}$



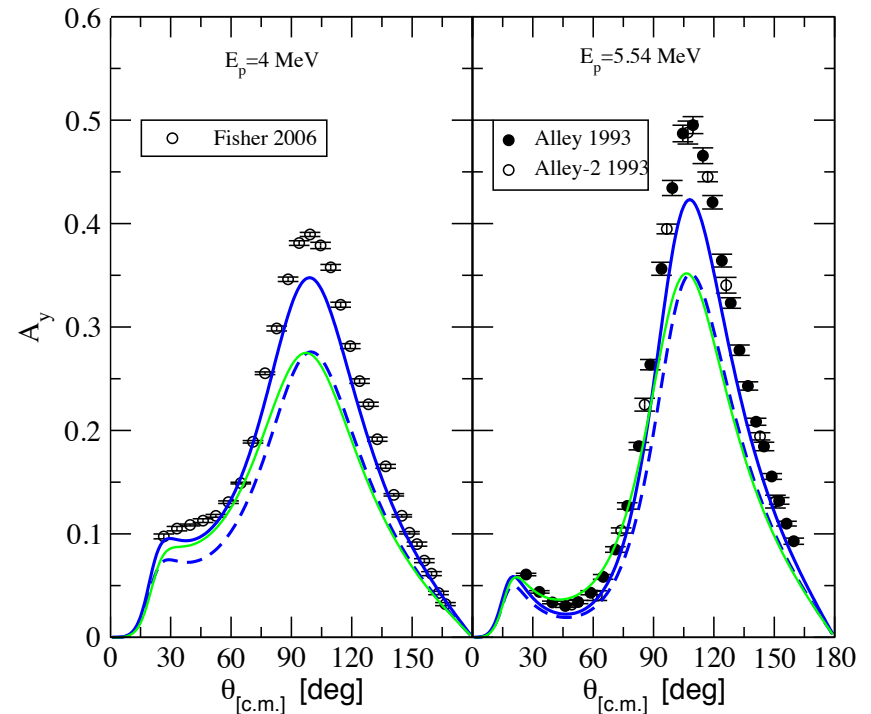
Chiral 3NF effects in 4N scattering

Viviani, Girlanda, Kievsky, Marcucci, Rosatti arXiv:1004.1306

p - ^3He differential cross section



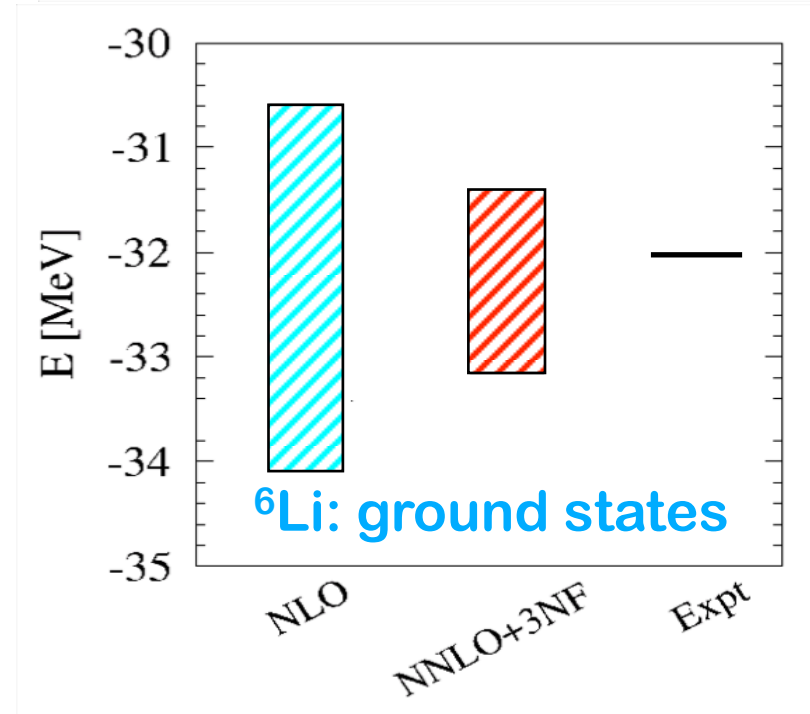
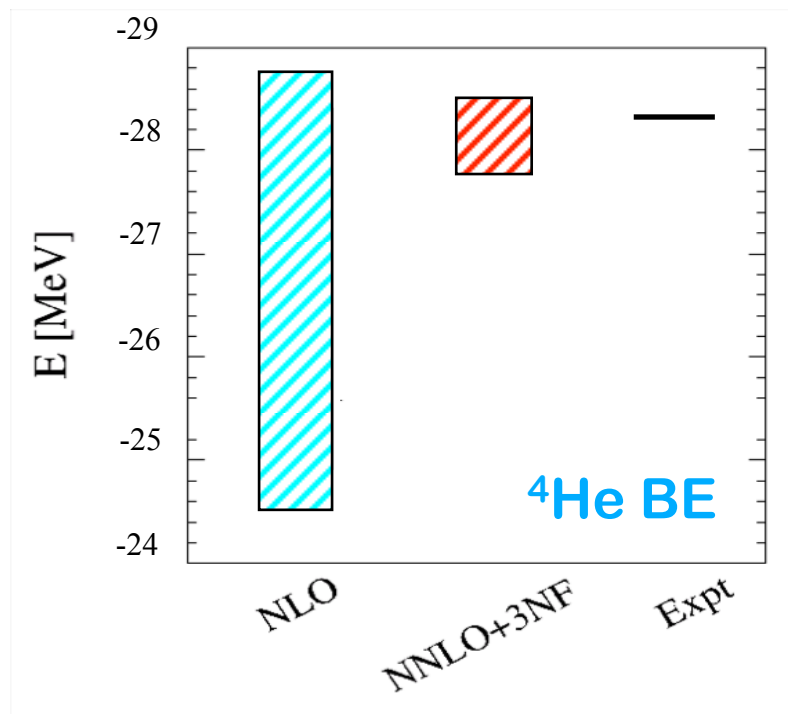
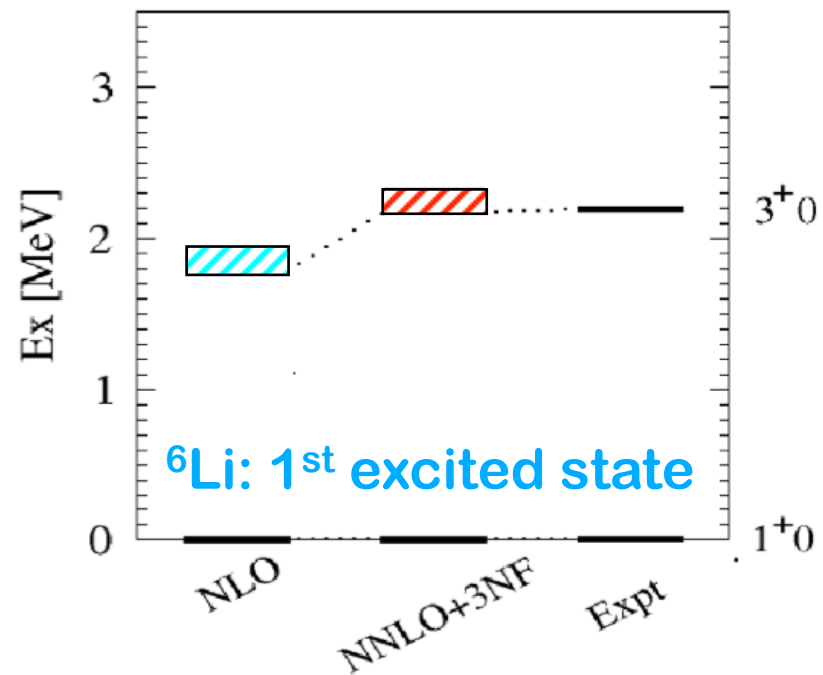
A_y -puzzle in p - ^3He elastic scattering



(the LECs D,E are tuned to the ^3H and ^4He binding energies)

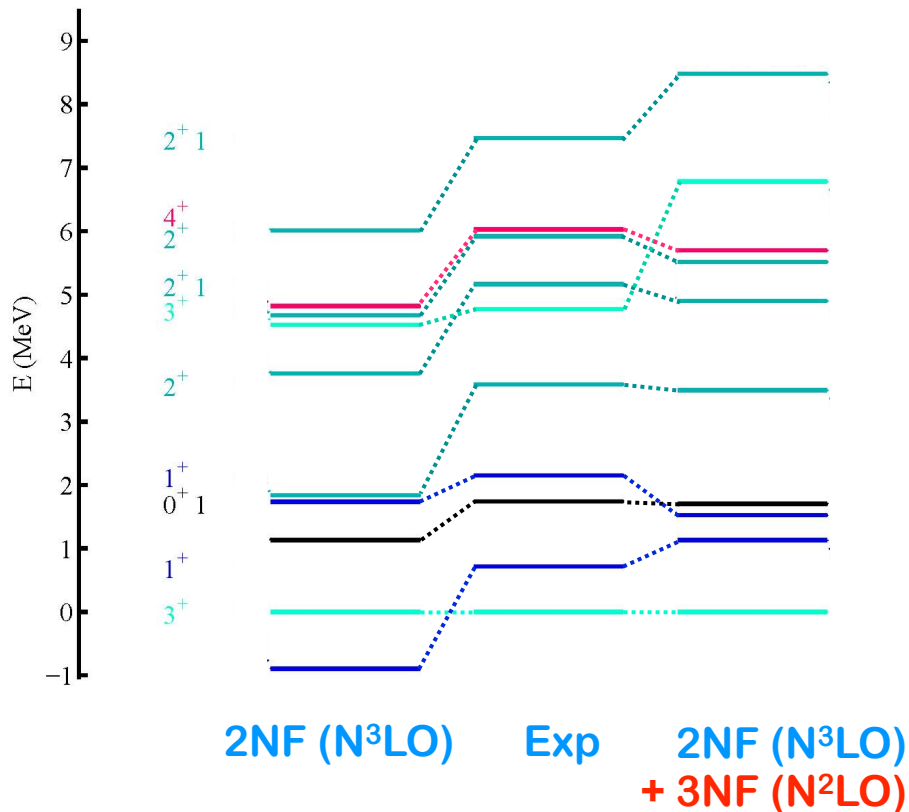
Light nuclei from chiral forces

Nogga et al.



Nuclear structure with chiral forces

^{10}B



Navratil et al., PRL 99
(2007) 042501

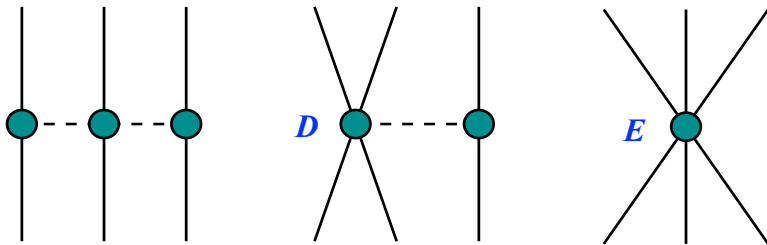
Chiral 3NF at N²LO are also found to play important role in

- explaining the long lifetime of ^{14}C [Holt, Kaiser, Weise '10](#)
- constraining the properties of neutron-rich matter & neutron star radii [Hebeler et al.'10](#)
- explaining the structure of Ca isotopes [Holt, Otsuka, Schwenk, Suzuki '10](#)

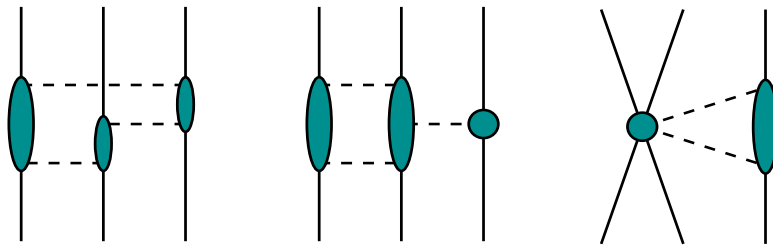
Chiral 3NF beyond N²LO

The first corrections to the leading 3NF are available!

Ishikawa, Robilotta, PRC76 (07); Bernard, EE, Krebs, Meißner, PRC77 (08); PRC84 (11)



- start contributing at N²LO
- fairly restricted operator structure
- also included in various models



- first appear at N³LO
- very rich operator structure
- parameter-free
- effects in Nd scatt., nuclear structure ?



$$V = \frac{2}{3} \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_2 \cdot \hat{r}_{12} \vec{\sigma}_3 \cdot \hat{r}_{13} f_1(r_{12}, r_{13}, r_{23}) + \left[2 + \frac{2}{3} (\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 + \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 + \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3) \right] f_2(r_{12}, r_{13}, r_{23}) + \dots$$



at large distances completely determined by chiral symmetry & experimental π N data,
highly nontrivial benchmarks with lattice QCD...

Few-nucleon physics with external probes

Pion-deuteron scattering

Pion-nucleon amplitude at threshold (in the isospin limit): $T_{\pi N}^{ba} \propto [\delta^{ab} a^+ + i\epsilon^{bac} \tau^c a^-]$

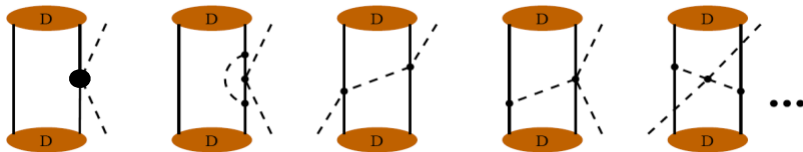
Recent data on hadronic atoms:

πH : $\epsilon_{1s} = (-7.120 \pm 0.012) \text{ eV}$, $\Gamma_{1s} = (0.823 \pm 0.019) \text{ eV}$ Gotta et al., Lect. Notes. Phys. 745 (08) 165

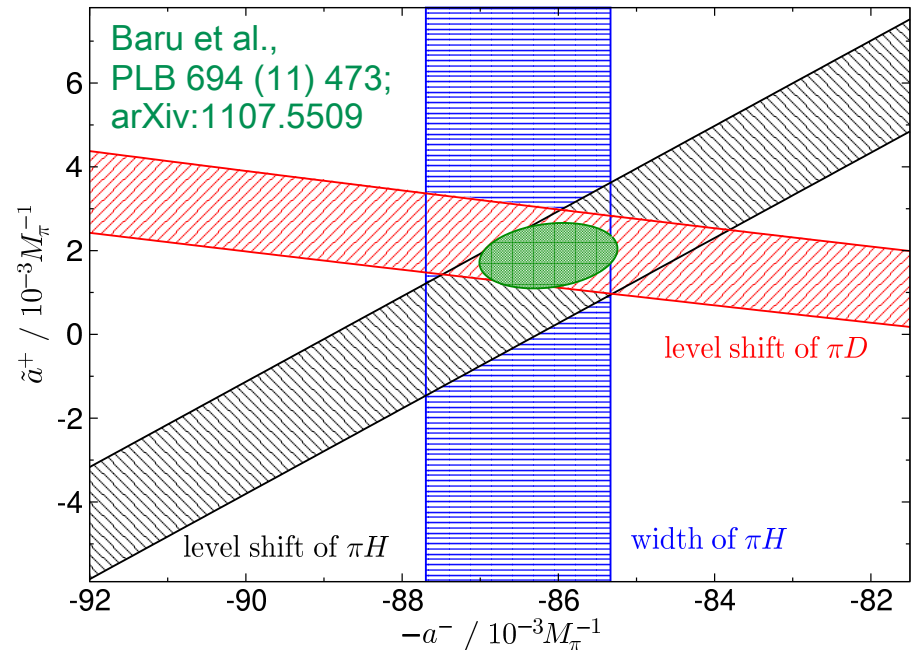
πD : $\epsilon_{1s}^D = (2.356 \pm 0.031) \text{ eV}$ Strauch et al., Eur. Phys. J A47 (11) 88

Use chiral EFT to extract information on a^+ and a^- from $a_{\pi d}$

Weinberg; Beane, Bernard, Lee, Meißner, EE, Phillips;
Baru, Liebig, Hoferichter, Hanhart, Nogga, ...



- careful analysis of IB effects
- radiative corrections included



Isospin breaking & few-N systems

Origin of isospin breaking in the Standard Model: $m_u \neq m_d$, photons

- Manifestation in the hadron spectrum: **mass splittings**

$$M_{\pi^\pm} = 139.57 \text{ MeV}, \quad M_{\pi^0} = 134.98 \text{ MeV} \quad \leftarrow \text{mainly of electromagnetic origin}$$

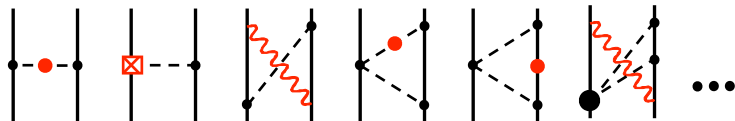
$$m_p = 938.27 \text{ MeV}, \quad m_n = 939.57 \text{ MeV} \quad \leftarrow \text{both strong and electromagnetic}$$

$$\delta m_N^{\text{str}} \equiv (m_n - m_p)^{\text{str}} = 2.05 \pm 0.3 \text{ MeV} \quad \text{Gasser, Leutwyler '82 (Cottingham sum rule)}$$

$$\delta m_N^{\text{em}} \equiv (m_n - m_p)^{\text{em}} = -0.76 \pm 0.3 \text{ MeV}$$

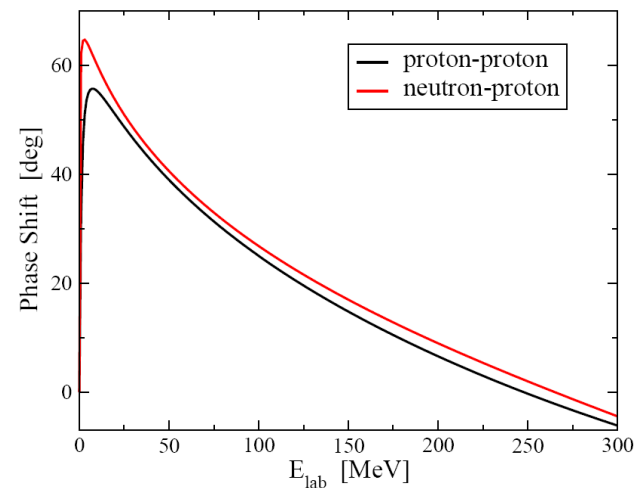
- Different (strong) forces between nn, np and pp

van Kolck, Friar, Niskanen, Kaiser, EE, Meißner, ...



Some manifestations

- differences in NN phase shifts,
- BE differences in mirror nuclei (CSB)



Isospin breaking & few-N systems

The challenge: can we extract the strong nucleon mass shift from hadronic reactions?

- $dd \rightarrow \alpha\pi^0$ cross section measurement at IUCF @ 228.5 / 231.8 MeV
Stephenson et al. '03

$$\sigma = 12.7 \pm 2.2 / 15.1 \pm 3.1 \text{ pb}$$

Theoretical analysis challenging; first estimations yield the right order of magnitude.

Gardestig et al. '04; Nogga et al. '06

- forward-backward asymmetry in $np \rightarrow d\pi^0$ @ 279.5 MeV (TRIUMF)
Opper et al. '03

$$A_{\text{fb}} = \frac{\int [d\sigma/d\Omega(\theta) - d\sigma/d\Omega(\pi - \theta)] d[\cos\theta]}{\int [d\sigma/d\Omega(\theta) + d\sigma/d\Omega(\pi - \theta)] d[\cos\theta]} = \left[17.2 \pm 8(\text{stat}) \pm 5.5(\text{sys}) \right] \times 10^{-4}$$

np \rightarrow d π^0 & the np mass difference

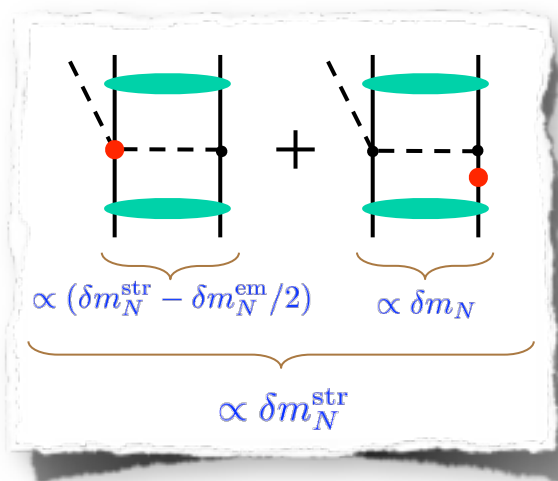
Bolton, Miller '09; Filin, Baru, E.E., Haidenbauer, Hanhart, Kudryavtsev, Meißner '09

$$\frac{d\sigma}{d\Omega} = A_0 + \underbrace{A_1 P_1(\cos\theta_\pi)}_{\text{gives rise to } A_{fb}} + A_2 P_2(\cos\theta_\pi) + \dots \quad \longrightarrow \quad A_{fb} \simeq \frac{A_1}{2A_0}$$

- A_0 can be determined from the pionic deuterium lifetime measurement @ PSI:

$$\sigma(np \rightarrow d\pi^0) = \frac{1}{2}\sigma(nn \rightarrow d\pi^-) = \frac{1}{2} \times 252_{-11}^{+5} \eta \text{ [\mu b]} \quad \longrightarrow \quad A_0 = 10.0_{-0.4}^{+0.2} \eta \text{ [\mu b]}$$

- A_1 at LO in chiral EFT $\longrightarrow A_{fb}^{LO} = (11.5 \pm 3.5) \times 10^{-4} \delta m_N^{str}/\text{MeV}$ Baru et al.'09



Experiment: $A_{fb} = \left[17.2 \pm 8(\text{stat}) \pm 5.5(\text{sys}) \right] \times 10^{-4}$

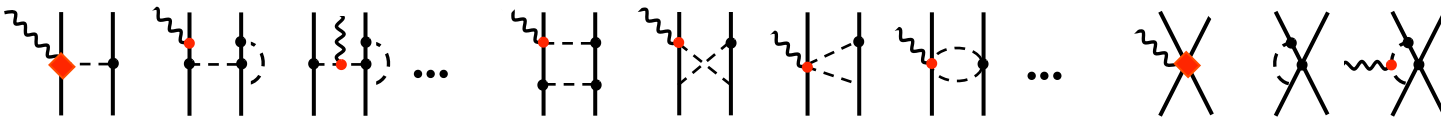
$\longrightarrow \delta m_N^{str} = 1.5 \pm 0.8(\text{exp.}) \pm 0.5(\text{th.}) \text{ MeV}$

Lattice: $\delta m_N^{str} = 2.26 \pm 0.57 \pm 0.42 \pm 0.10 \text{ MeV}$ Beane et al.'07

Cottingham SR: $\delta m_N^{str} = 2.05 \pm 0.3 \text{ MeV}$ Gasser, Leutwyler '82

Photon-induced reactions

Order eQ^{-1} :  well known since decades Chemtob, Rho, Friar, Riska, Adam, ...

Order eQ : 

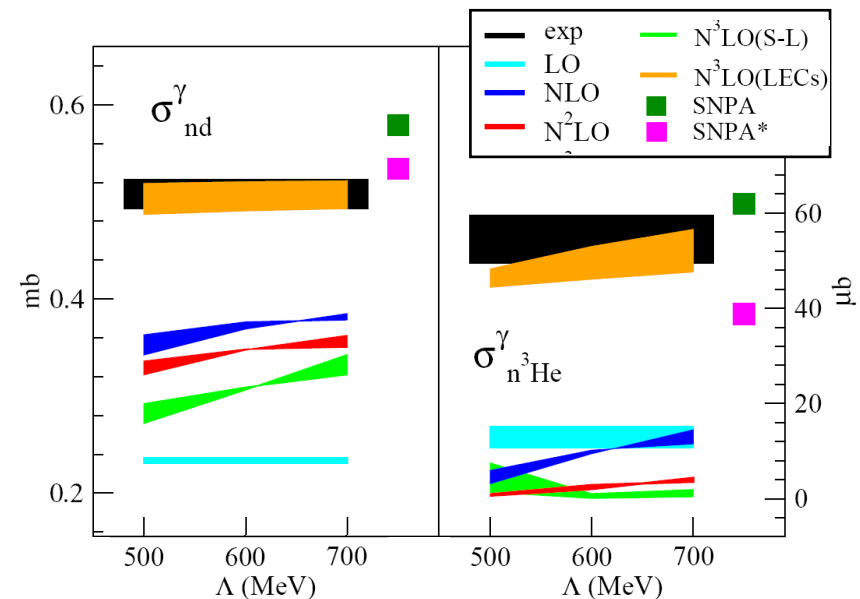
● Threshold kinematics Park, Min, Rho '95; Park, Kubodera, Min, Rho; Song, Lazauskas, Park, Min, ...

Application to $np \rightarrow d\gamma$ at threshold: $\sigma_{1N} = 306.6 \text{ mb} \longrightarrow \sigma_{1N+2N} = 334 \pm 3 \text{ mb}$
 to be compared with $\sigma_{\text{exp}} = 334.2 \pm 0.5 \text{ mb}$

● General kinematics Pastore, Schiavilla, Girlanda, Viviani, '08-'11; Kölling, Krebs, EE, Meißner, '09-'11

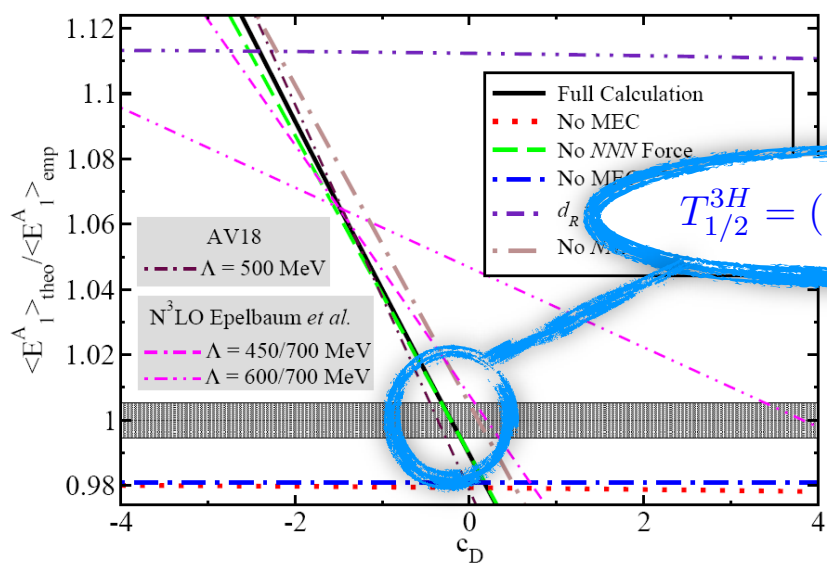
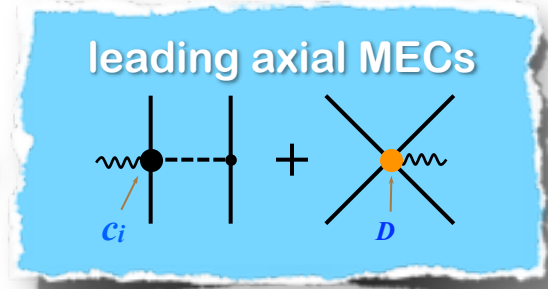
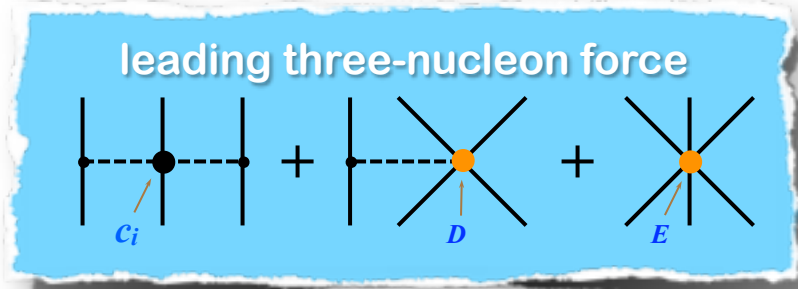
Application: Radiative capture of light nuclei

- LECs fixed assuming Δ -dominance and magnetic moments of ${}^2\text{H}$, ${}^3\text{H}$, ${}^3\text{He}$ + σ_{np}^γ
- predictions for nd , $n{}^3\text{He}$ radiative capture reactions for thermal neutrons (MEC dominated)

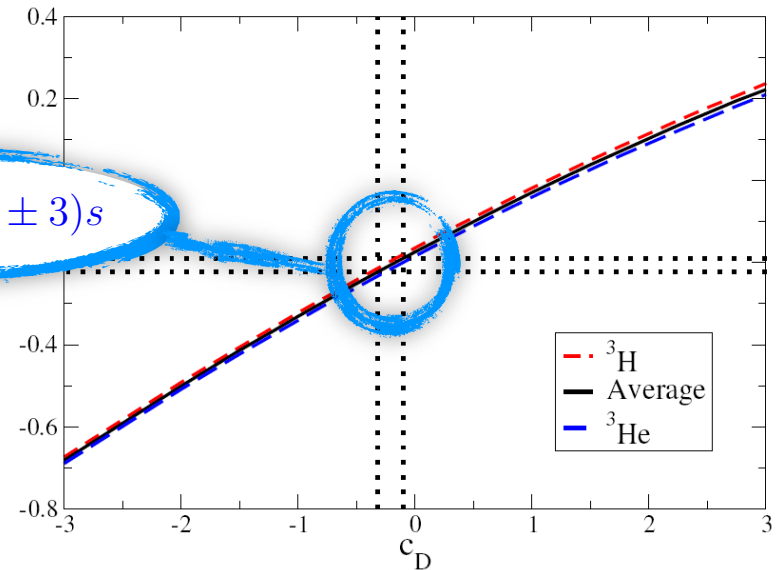


3N force & axial currents

Gazit, Quaglioni, Navratil, PRL 103 (2009) 102502



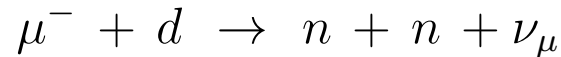
$T_{1/2}^{3\text{H}} = (1129.6 \pm 3) \text{ s}$



| | ${}^3\text{H}$ | | ${}^3\text{He}$ | | ${}^4\text{He}$ | |
|--------|-------------------|-------------------------------|-------------------|-------------------------------|-------------------|-------------------------------|
| | $E_{\text{g.s.}}$ | $\langle r_p^2 \rangle^{1/2}$ | $E_{\text{g.s.}}$ | $\langle r_p^2 \rangle^{1/2}$ | $E_{\text{g.s.}}$ | $\langle r_p^2 \rangle^{1/2}$ |
| NN | -7.852(4) | 1.651(5) | -7.124(4) | 1.847(5) | -25.39(1) | 1.515(2) |
| NN+NNN | -8.473(4) | 1.605(5) | -7.727(4) | 1.786(5) | -28.50(2) | 1.461(2) |
| Expt. | -8.482 | 1.60 | -7.718 | 1.77 | -28.296 | 1.467(13) |

3N force & axial currents

The determined value of D can be used to compute the muon doublet capture rate in

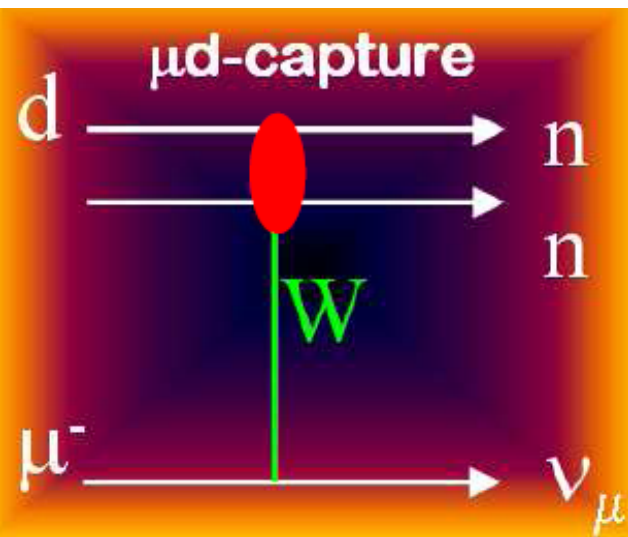


→ $\Lambda_{1/2} = (405.5 \pm 4.3) s^{-1}$ Adam, Tater, Truhlik, EE, Machleidt, Ricci '11
(a somewhat different value reported by Marcucci et al.'11)

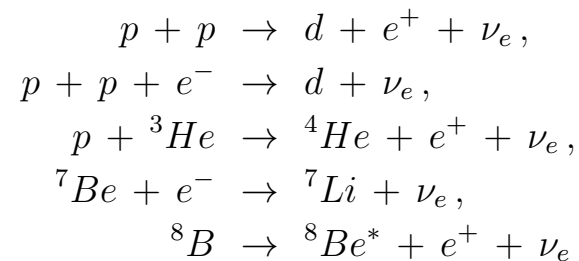
Exp: $\Lambda_{1/2} = (470.0 \pm 29) s^{-1}$ Martino '86

$\Lambda_{1/2} = (409.0 \pm 40) s^{-1}$ Cargnelli et al., '86, '87

Ongoing measurement by the MuSun Collaboration @ PSI: **1.5% accuracy for $\Lambda_{1/2}$**



-
- Test chiral EFT
 - Precision calculation of weak nuclear reactions

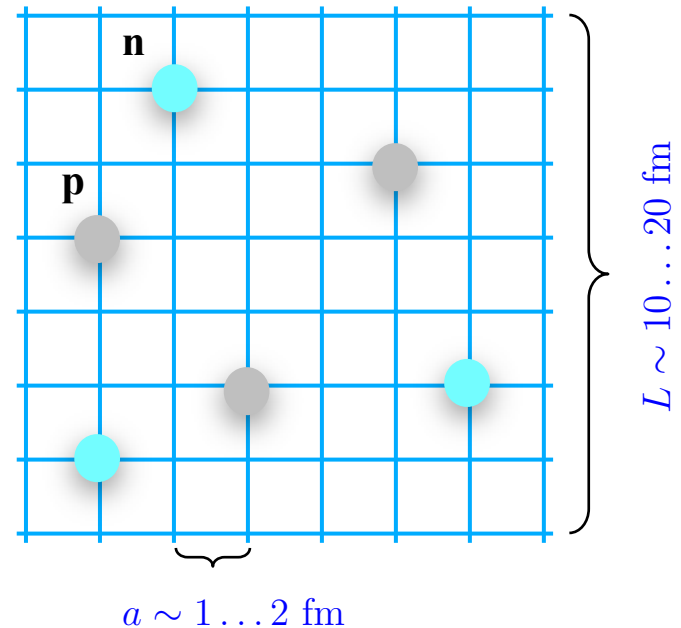


Nuclear Lattice Simulations

In collaboration with:

Dean Lee (North Carolina), Hermann Krebs (Bochum), Ulf-G. Meißner (Bonn/Jülich)

Borasoy, E.E., Krebs, Lee, Meißner, Eur. Phys. J. A31 (07) 105,
Eur. Phys. J. A34 (07) 185,
Eur. Phys. J. A35 (08) 343,
Eur. Phys. J. A35 (08) 357,
E.E., Krebs, Lee, Meißner, Eur. Phys. J A40 (09) 199,
Eur. Phys. J A41 (09) 125,
Phys. Rev. Lett 104 (10) 142501,
Eur. Phys. J. 45 (10) 335,
Phys. Rev. Lett. 106 (11) 192501

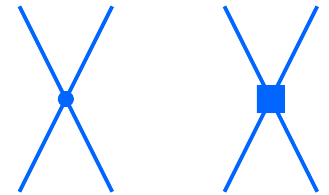


Calculation strategy

Lattice action (improved to minimize discr. errors, accurate to Q^3)

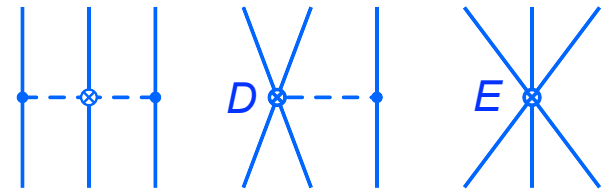
↓ Lanczos method

Solve $2N$ Schröd. Eq. with the spherical wall boundary cond. → phase shifts → **fix** the LO and NLO (perturbatively) **contact terms**



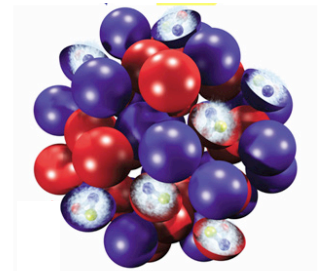
↓ projection Monte Carlo (with auxiliary fields)

Determine the LECs D , E from ${}^3\text{H}$ and ${}^4\text{He}$ BEs → the nuclear Hamiltonian completely fixed up to NNLO (Q^3)



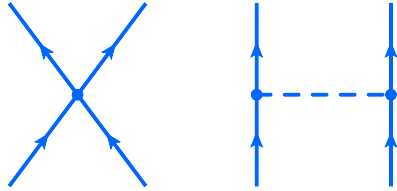
↓ (Multi-channel) projection Monte Carlo with auxiliary fields

Simulate the ground (and excited) states of **light nuclei**



Lattice actions

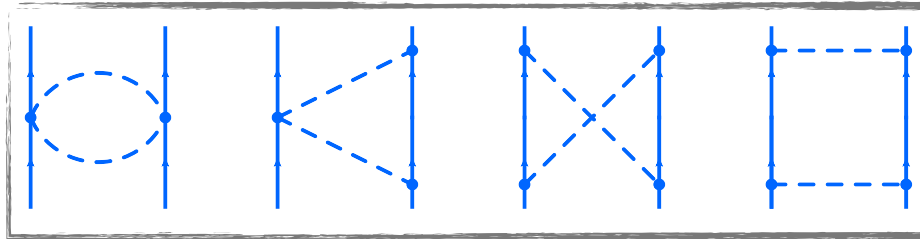
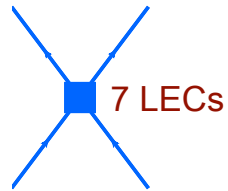
Q^0



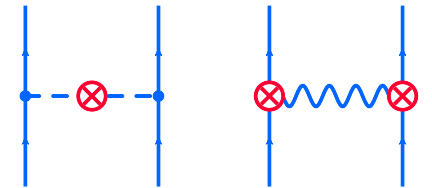
Different actions employed
 LO1: no smearing,
 LO2: smearing in all waves,
 LO3: smearing in even-l waves

used in the simulation

Q^2

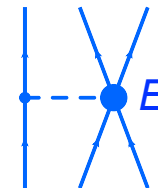
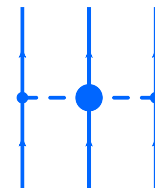
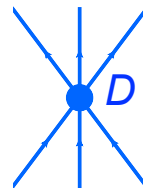
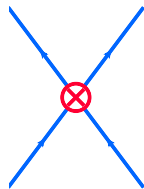
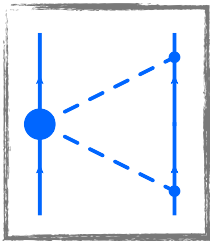


inserted perturbatively



for a ~ 2 fm ($\Lambda \sim 314$ MeV) can well be represented by contact terms

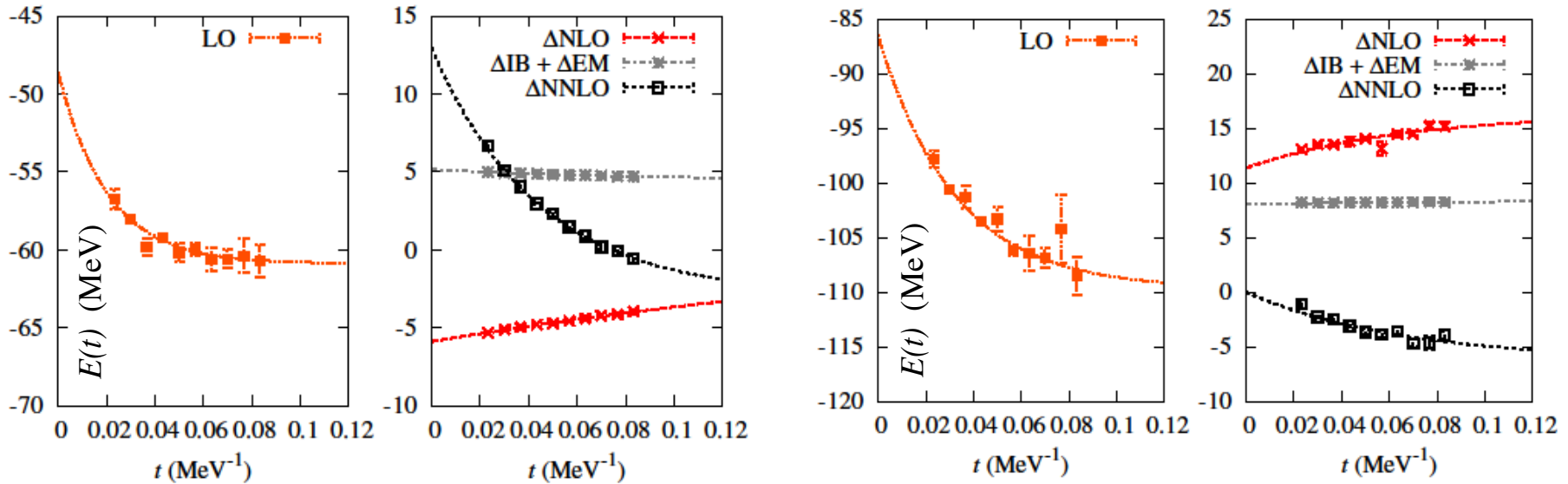
Q^3



Ground states of ${}^8\text{Be}$ and ${}^{12}\text{C}$

E.E., Krebs, Lee, Meißner, PRL 106 (11) 192501

Simulations for ${}^8\text{Be}$ and ${}^{12}\text{C}$, $L=11.8$ fm



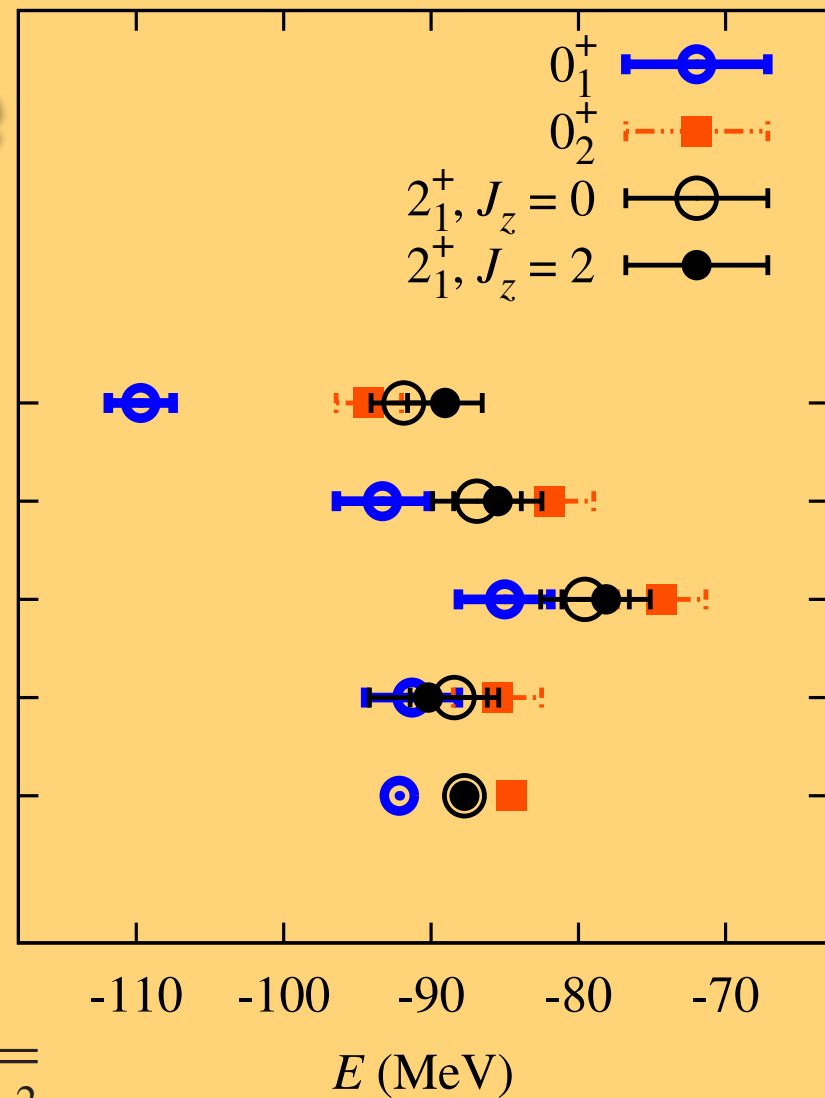
Various contributions to ${}^4\text{He}$, ${}^8\text{Be}$ and ${}^{12}\text{C}$

| | ${}^4\text{He}$ | ${}^8\text{Be}$ | ${}^{12}\text{C}$ |
|----------------------|-----------------|-----------------|-------------------|
| LO [$O(Q^0)$] | -24.8(2) | -60.9(7) | -110(2) |
| NLO [$O(Q^2)$] | -24.7(2) | -60(2) | -93(3) |
| IB + EM [$O(Q^2)$] | -23.8(2) | -55(2) | -85(3) |
| NNLO [$O(Q^3)$] | -28.4(3) | -58(2) | -91(3) |
| Experiment | -28.30 | -56.50 | -92.16 |

The Hoyle state

E.E., Krebs, Lee, Meißner, PRL 106 (11) 192501

LO [$O(Q^0)$]
 NLO [$O(Q^2)$]
 IB + EM [$O(Q^2)$]
 NNLO [$O(Q^3)$]
 Experiment



| | 0_2^+ | $2_1^+, J_z = 0$ | $2_1^+, J_z = 2$ |
|----------------------|---------|------------------|------------------|
| LO [$O(Q^0)$] | -94(2) | -92(2) | -89(2) |
| NLO [$O(Q^2)$] | -82(3) | -87(3) | -85(3) |
| IB + EM [$O(Q^2)$] | -74(3) | -80(3) | -78(3) |
| NNLO [$O(Q^3)$] | -85(3) | -88(3) | -90(4) |
| Experiment | -84.51 | -87.72 | |

Summary & outlook

Nuclear chiral EFT enters precision era:

- accurate nuclear potentials at N³LO
- detailed analyses of electroweak currents
- high-precision determination of π N scatt. lengths
- precision calculations of the radiative/muon capture reactions, ...

Time to address unsolved problems:

- e.g. the structure of the 3NF (work in progress...)

New trends/directions:

- combining EFT with ab-initio many-body methods \longrightarrow access to light nuclei
- bridging strong, weak and e.m. few-N reactions, ...

Further topics (not covered in the talk):

- nuclear parity violation
- hypernuclear physics
- few-N systems and physics beyond the Standard Models (e.g. neutron EDM), ...